

# Muon Physics

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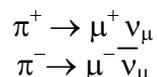
## Introduction

This experiment permits you to measure the charge averaged mean muon lifetime in plastic scintillator, to measure the relative flux of sea-level muons as a function of height above sea-level and to demonstrate the time dilation effect of special relativity. The instrument also provides a source of genuinely random numbers that can be used for experimental tests of standard probability distributions.

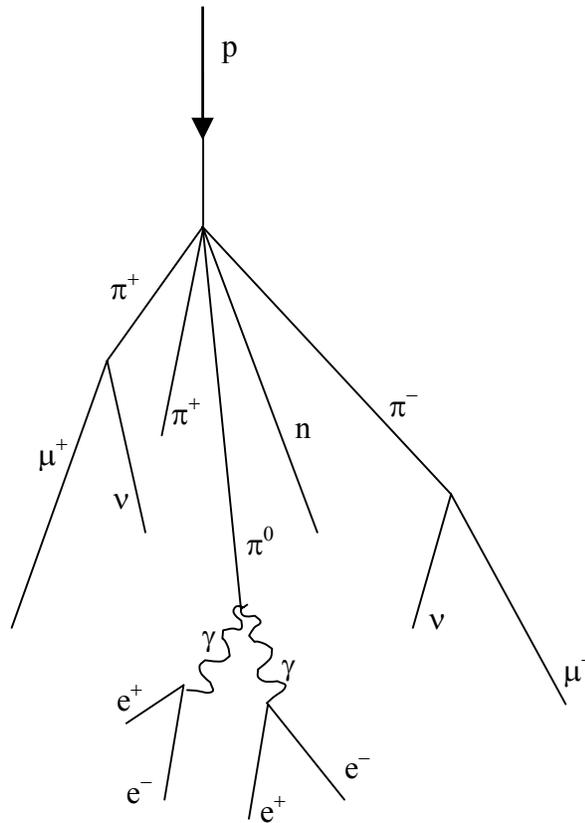
## Our Muon Source

The top of earth's atmosphere is bombarded by a flux of high energy charged particles produced in other parts of the universe by mechanisms that are not yet fully understood. The composition of these "primary cosmic rays" is somewhat energy dependent but a useful approximation is that 98% of these particles are protons or heavier nuclei and 2% are electrons. Of the protons and nuclei, about 87% are protons, 12% helium nuclei and the balance are still heavier nuclei that are the end products of stellar nucleosynthesis. See Simpson for more details.

The primary cosmic rays collide with the nuclei of air molecules and produce a shower of particles that include protons, neutrons, pions (both charged and neutral), kaons, photons, electrons and positrons. These secondary particles then undergo electromagnetic and nuclear interactions to produce yet additional particles in a cascade process. Figure 1 indicates the general idea. Of particular interest is the fate of the charged pions produced in the cascade. Some of these will interact via the strong force with air molecule nuclei but others will spontaneously decay via the weak force into a muon plus a neutrino or antineutrino.



The muon does not interact with matter via the strong force but only through the weak and electromagnetic forces. It travels a relatively long instance while losing its kinetic energy and decays by the weak force into an electron plus a neutrino and antineutrino. We will detect the decays of some of the muons produced in the cascade. (Our detection probability for the neutrinos and antineutrinos is utterly negligible.)



**Figure 1.** Cosmic ray cascade induced by a cosmic ray proton striking an air molecule nucleus.

Not all of the particles produced in the cascade in the upper atmosphere survive all the way down to sea-level due to their interaction with atmospheric nuclei and their own spontaneous decay. The flux of sea-level muons is approximately 1 per minute per  $\text{cm}^2$  (see <http://pdg.lbl.gov> for more precise numbers) with a mean kinetic energy of about 4 GeV.

Careful study [pdg.lbl.gov] shows that the mean production height of the muons detected at sea-level is approximately 15 km. Travelling at the speed of light, the transit time from production point to sea-level is then 50  $\mu\text{sec}$ . Since the lifetime of at-rest muons is more than a factor of 20 smaller, the appearance of an appreciable sea-level muon flux is evidence for the time dilation effect of special relativity.

### Muon Decay Time Distribution

The decay times for muon decays are easily described mathematically. Suppose at some time  $t$  we have  $N(t)$  muons. If the probability that a muon decays in some small time interval  $dt$  is  $\lambda dt$ , where  $\lambda$  is a constant “decay rate” that characterizes how rapidly a muon decays, then the change  $dN$  in our population of muons is just  $dN = -N(t)\lambda dt$ . Integrating, we have  $N(t) = N_0 \exp(-\lambda t)$ , where  $N(t)$  is the number of surviving muons at

some time  $t$  and  $N_0$  is the number of muons at  $t=0$ . The "lifetime"  $\tau$  of a muon is the reciprocal of  $\lambda$ ,  $\tau = 1/\lambda$ . This simple exponential relation is typical of radioactive decay.

Now, we do not have a single clump of muons whose surviving number we can easily measure. Instead, we detect muon decays from muons that enter our detector at essentially random times, typically one at a time. It is still the case that their decay time distribution has a simple exponential form of the type described above. By decay time distribution  $D(t)$ , we mean that the time-dependent probability that a muon decays in the time interval between  $t$  and  $t + dt$  is given by  $D(t)dt$ . If we had started with  $N_0$  muons, then the fraction  $-dN/N_0$  that would on average decay in the time interval between  $t$  and  $t + dt$  is just given by differentiating the above relation:

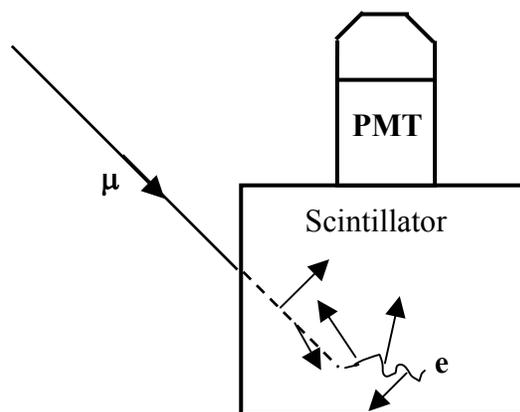
$$\begin{aligned} -dN &= N_0 \lambda \exp(-\lambda t) dt \\ -dN/N_0 &= \lambda \exp(-\lambda t) dt \end{aligned}$$

The left-hand side of the last equation is nothing more than the decay probability we seek, so  $D(t) = \lambda \exp(-\lambda t)$ . This is true regardless of the starting value of  $N_0$ . That is, the distribution of decay times, for each new muon entering our detector, is also exponential with the very same exponent used to describe the surviving population of muons. Again, what we call the muon lifetime is  $\tau = 1/\lambda$ .

## Detector Physics

The active volume of the detector is a plastic scintillator in the shape of a right circular cylinder of 15 cm diameter and 12.5 cm height placed at the bottom of the black anodized aluminum alloy tube. Plastic scintillator is a transparent, aromatic ring containing base material doped uniformly with one or more fluors. A charged particle passing through the scintillator will lose some of its kinetic energy by ionization and atomic excitation of the base material molecules. Some of this deposited energy is then transferred to the fluor molecules whose electrons are then promoted to excited states. Upon radiative de-excitation, light in the blue and near-UV portion of the electromagnetic spectrum is emitted with a typical decay time of a few nanoseconds. A typical photon yield for a plastic scintillator is 1 optical photon emitted per 100 eV of deposited energy. The properties of the polyvinyltoluene-based scintillator used in the muon lifetime instrument are summarized in table 1.

To measure the muon's lifetime, we are interested in muons that enter, slow, stop and then decay inside the plastic scintillator. The cartoon below summarizes this process. Such muons have a maximum kinetic energy of only about 150 MeV as they enter the tube. As a muon slows to a stop, the excited scintillator emits light that is detected by a photomultiplier tube (PMT), eventually producing a logic signal that triggers a timing clock. (See the electronics section below for more detail.) A stopped muon, after a bit, decays into an electron, a neutrino and an anti-neutrino. (See the next section for an important qualification of this statement.) Since the electron mass is so much smaller than the muon mass,  $m_\mu/m_e \sim 210$ , the electron tends to be very energetic and to produce scintillator light essentially all along its pathlength. The neutrino and anti-neutrino also share some of the muon's total energy but they entirely escape detection. This second burst of scintillator light is also seen by the PMT and used to trigger the timing clock. The distribution of time intervals between successive clock triggers for a set of muon decays is the physically interesting quantity used to measure the muon lifetime.



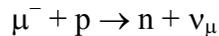
**Figure 2.** Schematic showing the generation of the two light pulses used in determining the muon lifetime. One light pulse is from the slowing muon and the other is from its decay into an electron (or positron).

Table 1. General Scintillator Properties

Mass density	1.032 g/cc
Refractive index	1.58
Base material	Polyvinyltoluene
Rise time	0.9 ns
Fall time	2.4 ns
Wavelength of Maximum Emission	423 nm

### Interaction of $\mu^-$ 's with matter

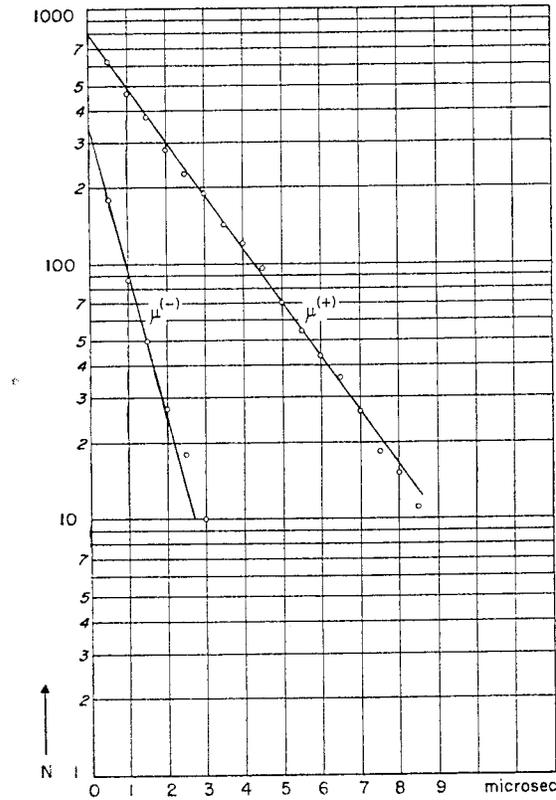
The muons whose lifetime we measure necessarily interact with matter. Negative muons that stop in the scintillator can bind to the scintillator's carbon and hydrogen nuclei in much the same way as electrons do. Since the muon is not an electron, it is not prevented by the Pauli exclusion principle from occupying an atomic orbital already filled with electrons. Such bound muons can interact with protons



before they spontaneously decay. Since there are now two ways for a negative muon to disappear, the effective lifetime of negative muons in matter is somewhat less than the lifetime of positively charged muons, which do not have this second interaction mechanism. Experimental evidence for this effect is shown in figure 3 where "disintegration" curves for positive and negative muons in aluminum are shown. (See Rossi, 1952) The abscissa is the time interval  $t$  between the arrival of a muon in the aluminum target and its decay. The ordinate, plotted logarithmically, is the number of muons greater than the corresponding abscissa. These curves have the same meaning as curves representing the survival population of radioactive substances. The slope of the curve is a measure of the effective lifetime of the decaying substance. The muon lifetime we measure with this instrument is an average over both charge species so the mean lifetime of the detected muons will be somewhat less than the free space value  $\tau = 2.19703 \pm 0.00004 \mu\text{sec}$ .

The probability for nuclear absorption of a stopped *negative* muon by one of the scintillator nuclei is proportional to  $Z^4$ , where  $Z$  is the atomic number of the nucleus [Rossi]. A stopped muon captured in an atomic orbital will make transitions down to the K-shell on a time scale short compared to its time for spontaneous decay [Wheeler]. Its Bohr radius is roughly 200 times smaller than that for an electron due to its much larger mass, increasing its probability for being found in the nucleus. From our knowledge of hydrogenic wavefunctions, the probability density for the bound muon to be found inside

the nucleus is proportional to  $Z^3$ . Once inside the nucleus, a muon's probability for encountering a proton is proportional to the number of protons there and so scales like  $Z$ . The net effect is for the overall absorption probability to scale like  $Z^4$ . Again, this effect is relevant only for negatively charged muons.



**Figure 3.** Disintegration curves for positive and negative muons in aluminum. The ordinates at  $t = 0$  can be used to determine the relative numbers of negative and positive muons that have undergone spontaneous decay. The slopes can be used to determine the decay time of each charge species. (From Rossi, 1952.)

## $\mu^+/\mu^-$ Charge Ratio at Ground Level

Our measurement of the muon lifetime in plastic scintillator is an average over both negatively and positively charged muons. We have already seen that  $\mu^-$ 's have a lifetime somewhat smaller than positively charged muons because of weak interactions between negative muons and protons in the scintillator nuclei. This interaction probability is proportional to  $Z^4$ , where  $Z$  is the atomic number of the nuclei, so the lifetime of negative muons in scintillator and carbon should be very nearly equal. This later lifetime  $\tau_c$  is measured to be  $\tau_c = 2.043 \pm 0.003 \mu\text{sec}$ . [Reiter]

From a measurement of the average muon lifetime  $\langle\tau\rangle$  in scintillator and the known lifetime of negative muons in carbon, we can deduce the relative abundance of positively charged muons at ground level. Let  $\tau_+$  and  $\tau_-$  be the lifetimes of positively and negatively charged muons in plastic scintillator, respectively. The measured muon lifetime will then be a flux weighted average for the two charges and the ratio  $\rho$  of positively charged to negatively muons is given by:

$$\begin{aligned}\langle\tau\rangle &= \frac{N_+\tau_+ + N_-\tau_-}{N_+ + N_-} \\ &= \frac{\rho\tau + \tau_-}{1 + \rho} \\ \Rightarrow \rho &= \frac{\langle\tau\rangle - \tau_-}{\tau - \langle\tau\rangle}\end{aligned}$$

Here  $\rho \equiv N_+/N_-$ , where  $N_+$  is the number of positively charged muons detected in some time interval and  $N_-$  is the corresponding number for negative muons. We have also used the excellent approximation that the lifetime of a positively charged muon in the scintillator equals the free space value,  $\tau_+ = \tau$ .

## Backgrounds

The detector responds to any particle that produces enough scintillation light to trigger its readout electronics. These particles can be either charged, like electrons or muons, or neutral, like photons, that produce charged particles when they interact inside the scintillator. Now, the detector has no knowledge of whether a penetrating particle stops or not inside the scintillator and so has no way of distinguishing between light produced by muons that stop and decay inside the detector, from light produced by a pair of through-going muons that occur one right after the other. This important source of background events can be dealt with in two ways. First, we can restrict the time interval during which we look for the two successive flashes of scintillator light characteristic of muon decay events. Secondly, we can estimate the background level by looking at large times in the decay time histogram where we expect few events from genuine muon decay.

## Fermi Coupling Constant $G_F$

Muons decay via the weak force and the Fermi coupling constant  $G_F$  is a measure of the strength of the weak force. To a good approximation, the relationship between the muon lifetime  $\tau$  and  $G_F$  is particularly simple:

$$\tau = \frac{192\pi^3 \hbar^7}{G_F^2 m^5 c^4}$$

where  $m$  is the mass of the muon and the other symbols have their standard meanings. Measuring  $\tau$  with this instrument and then taking  $m$  from, say, the Particle Data Group (<http://www.pdg.lbl.gov>) produces a value for  $G_F$ .

## Time Dilation Effect

A measurement of the muon stopping rate at two different altitudes can be used to demonstrate the time dilation effect of special relativity. Although the detector configuration is not optimal for such a demonstrating time dilation, a useful measurement can still be performed without additional scintillators or lead absorbers. Due to the finite size of the detector, only muons with a typical kinetic energy of about 160 MeV will stop inside the plastic scintillator. The stopping rate is measured from the total number of observed muon decays recorded by the instrument in some time interval. This rate in turn is proportional to the flux of muons with kinetic energy of about 160 MeV and this flux decreases with diminishing altitude as the muons descend and decay in the atmosphere. After measuring the muon stopping rate at one altitude, predictions for the stopping rate at another altitude can be made with and without accounting for the time dilation effect of special relativity. A second measurement at the new altitude distinguishes between competing predictions.

A comparison of the muon stopping rate at two different altitudes must account for the muon's energy loss as it descends into the atmosphere, variations with energy in the shape of the muon energy spectrum, and the varying zenith angles of the muons that stop in the detector. Since the detector stops only low energy muons, the stopped muons detected by the low altitude detector will, at the elevation of the higher altitude detector, necessarily have greater energy. This energy difference  $\Delta E(h)$  will depend on the pathlength between the two detector positions.

Vertically travelling muons at the position of the higher altitude detector that ultimately reach and are detected by the lower detector have an energy larger than those stopped and detected by the upper detector by an amount approximately equal to  $160 \text{ MeV} + \Delta E(h)$ . If the shape of the muon energy spectrum changes significantly with energy, then the relative muon stopping rates at the two different altitudes will reflect this difference in spectrum shape at the two different energies. (This is easy to see if you suppose muons do not decay at all.) This variation in the spectrum shape can be corrected for by calibrating the detector in a manner described below.

Like all charged particles, a muon loses energy through Coulombic interactions with the matter it traverses. The average energy loss rate in matter for singly charged particles traveling close to the speed of light is approximately  $2 \text{ MeV/g/cm}^2$ , where we measure the material thickness  $s$  in units of  $\text{g/cm}^2$ . Here,  $s = \rho x$ , where  $\rho$  is the mass density of the material, measured in  $\text{g/cm}^3$ , and the  $x$  is the particle's pathlength, measured in cm. A more accurate value can be determined from the Bethe-Bloch equation.

$$\begin{aligned}\frac{dE}{dx} &= -\frac{4\pi N_e^4}{mc^2\beta^2} z^2 \left( \ln \frac{2mc^2\beta^2\gamma^2}{I} - \beta^2 \right) \\ &= 0.3071 \left( \frac{\text{MeV}}{\text{g/cm}^2} \right) \frac{Z}{A} \rho \frac{1}{\beta^2} z^2 \left( \ln \frac{2mc^2}{I} \beta^2 \gamma^2 - \beta^2 \right)\end{aligned}$$

Here  $N$  is the number of electrons in the stopping medium per  $\text{cm}^3$ ,  $e$  is the electronic charge,  $z$  is the atomic number of the projectile,  $Z$  and  $A$  are the atomic number and weight, respectively, of the stopping medium. The velocity of the projectile is  $\beta$  in units of the speed  $c$  of light and its corresponding Lorentz factor is  $\gamma$ . The symbol  $I$  denotes the mean excitation energy of the stopping medium atoms. Approximately,  $I=AZ$ , where  $A \cong 13$  eV. More accurate values for  $I$  can be found in [Leo, p26] as well as corrections to the Bethe-Bloch equation.

A simple estimate of the energy lost  $\Delta E$  by a muon as it travels a vertical distance  $H$  is  $\Delta E = 2 \text{ MeV/g/cm}^2 * H * \rho_{\text{air}}$ , where  $\rho_{\text{air}}$  is the density of air, possibly averaged over  $H$  using the density of air according to the “standard atmosphere.” Here the atmosphere is assumed isothermal and the air pressure  $p$  at some height  $h$  above sea level is parameterized by  $p = p_0 \exp(-h/h_0)$ , where  $p_0 = 1030 \text{ g/cm}^2$  is the total thickness of the atmosphere and  $h_0 = 8.4 \text{ km}$ . The air density  $\rho$  is given by  $\rho = -dp/dh$ .

The transit time  $t'$  for a projectile of mass  $m$ , as seen in its *own rest frame*, to travel from some height  $H$ , measured in the lab frame, down to sea-level ( $H = 0$ ), is given by

$$t' = \int_H^0 \frac{dh}{c\beta(h)}$$

Here  $\beta$  and  $\gamma$  have their usual relativistic meanings for the projectile and are measured in the lab frame. We have also made the substitution  $dh = \beta c dt$ , where  $t$  is the time measured in the lab frame. Since relativistic muons lose energy at essentially a constant rate when travelling through a medium of mass density  $\rho$ ,  $dE/ds = C_0$ , so we have  $dE = \rho C_0 dh$ . Here  $C_0 = 2 \text{ MeV/(g/cm}^2)$ . Also, from the Einstein relation,  $E = \gamma mc^2$ ,  $dE = mc^2 d\gamma$ , so  $dh = (mc^2/\rho C_0) d\gamma$ . Hence,

$$\begin{aligned}t' &= \frac{mc}{\rho C_0} \int_{\gamma_1}^{\gamma_2} \frac{d\gamma}{\beta} \\ &= \frac{mc}{\rho C_0} \int_{\gamma_1}^{\gamma_2} \frac{\gamma d\gamma}{\sqrt{\gamma^2 - 1}}\end{aligned}$$

Here  $\gamma_1$  is the muon's gamma factor at height  $H$  and  $\gamma_2$  is its gamma factor just before it enters the scintillator. We can take  $\gamma_2 = 1.5$  since we want muons that stop in the scintillator and assume that on average stopped muons travel halfway into the scintillator, corresponding to a distance  $s = 10 \text{ g/cm}^2$ . The entrance muon momentum is then taken from range-momentum at the Particle Data Group WWW site and the corresponding  $\gamma_2$

computed. The lower limit of integration is given by  $\gamma_1 = E_1/mc^2$ , where  $E_1 = E_2 + \Delta E$ , with  $E_2 = 160$  MeV. The integral can be evaluated numerically. (See Internet site: [http://people.hofstra.edu/faculty/Stefan\\_Waner/RealWorld/integral/integral.html](http://people.hofstra.edu/faculty/Stefan_Waner/RealWorld/integral/integral.html))

Hence, the ratio  $R$  of muon stopping rates for the same detector at two different positions separated by a vertical distance  $H$ , and ignoring for the moment any variations in the shape of the energy spectrum of muons, is just  $R = \exp(-t'/\tau)$ , where  $\tau$  is the muon lifetime measured in its rest frame.

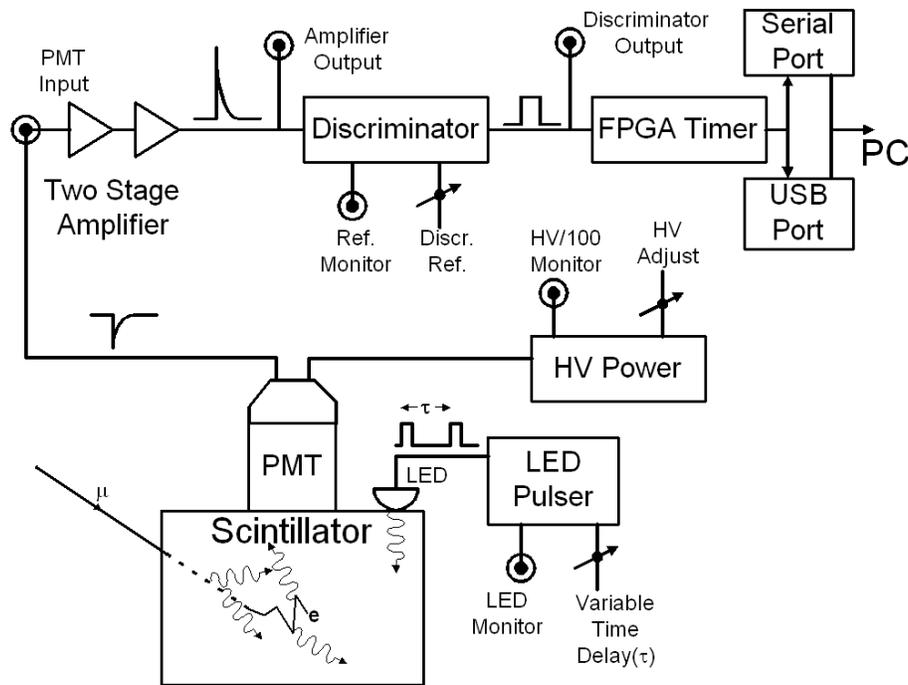
When comparing the muon stopping rates for the detector at two different elevations, we must remember that muons that stop in the lower detector have, at the position of the upper detector, a larger energy. If, say, the relative muon abundance grows dramatically with energy, then we would expect a relatively large stopping rate at the lower detector simply because the starting flux at the position of the upper detector was so large, and not because of any relativistic effects. Indeed, the muon energy spectrum does peak, at around  $E_{\mu} 600$  MeV or so, although the shape is not known with high precision. See figure muon\_spectrum.

Muons spectrum figure

We therefore need a way to correct for variations in the shape of the muon energy spectrum in the region from about 160 MeV – 800 MeV. We do this by first measuring the muon stopping rate at two different elevations ( $\Delta h = 3000$  meters between Taos, NM and Dallas, TX) and then computing the ratio  $R_{\text{raw}}$  of raw stopping rates. ( $R_{\text{raw}} = \text{Dallas/Taos} = 0.413$ .) Next, using the above expression for the transit time between the two elevations, we compute the transit time in the muon's rest frame ( $t' = 1.36\tau$ ) for vertically travelling muons and calculate the corresponding theoretical stopping rate ratio  $R = \exp(-t'/\tau) = 0.257$ . We then compute the double ratio  $R_0 = R_{\text{raw}}/R = 1.61$  of the measured stopping rate ratio to this theoretical rate ratio and interpret this as a correction factor to account for the increase in muon flux between about 160 MeV and 600 MeV. This correction is to be used in all subsequent measurements for any pair of elevations. To verify that the correction scheme works, we take a new stopping rate measurement at a different elevation ( $h = 2133$  meters a.s.l. at Los Alamos, NM), and compare a new stopping rate ratio measurement with our new, corrected theoretical prediction for the stopping rate ratio  $R_{\mu} = R_0 R = 1.61 \exp(-t'/\tau)$ . We find  $t' = 1.06\tau$  and  $R_{\mu} = 0.559$ . The raw measurements yield  $R_{\text{raw}} = 0.554$ , showing good agreement.

## Electronics

A block diagram of the readout electronics is shown in figure 4. The logic of the signal processing is simple. Scintillation light is detected by a photomultiplier tube (PMT) whose output signal feeds a two-stage amplifier. The amplifier output then feeds a voltage comparator (“discriminator”) with adjustable threshold. This comparator produces a TTL output pulse for input signals above threshold and this TTL output pulse triggers the timing circuit of the FPGA. A second TTL output pulse arriving at the FPGA input within a fixed time interval will then stop and reset the timing circuit. (The reset takes about 1 msec during which the detector is disabled.) The time interval between the start and stop timing pulses is the data sent to the PC via the communications module that is used to determine the muon lifetime. If a second TTL pulse does not arrive within the fixed time interval, the timing circuit is reset automatically for the next measurement.



**Figure 4.** Block diagram of the readout electronics. The amplifier and discriminator outputs are available on the front panel of the electronics box. The HV supply is inside the detector tube.

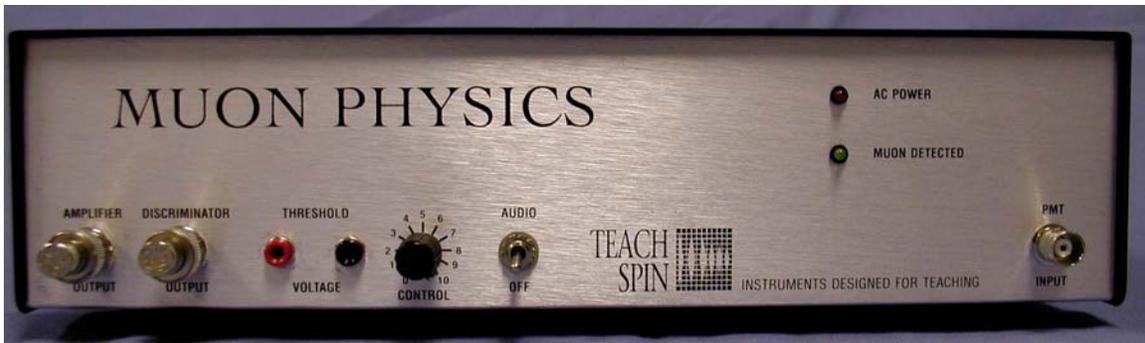
The front panel of the electronics box is shown in figures 5. The amplifier output is accessible via the BNC connector labeled *Amplifier output*. Similarly, the comparator output is accessible via the connector labeled *Discriminator output*. The voltage level against which the amplifier output is compared to determine whether the comparator

triggers can be adjusted using the “Threshold control” knob. The threshold voltage is monitored by using the red and black connectors that accept standard multimeter probe leads. The toggle switch controls a beeper that sounds when an amplifier signal is above the discriminator threshold. The beeper can be turned off.

The back panel of the electronics box is shown in figure 6. An extra fuse is inside the power switch.

Figure 7 shows the top of the detector cylinder. DC power to the electronics inside the detector tube is supplied from the electronics box through the connector *DC Power*. The high voltage (HV) to the PMT can be adjusted by turning the potentiometer located at the top of the detector tube. The HV level can be measured by using the pair of red and black connectors that accept standard multimeter probes. The HV monitor output is a factor of 100 less than the HV applied to the PMT.

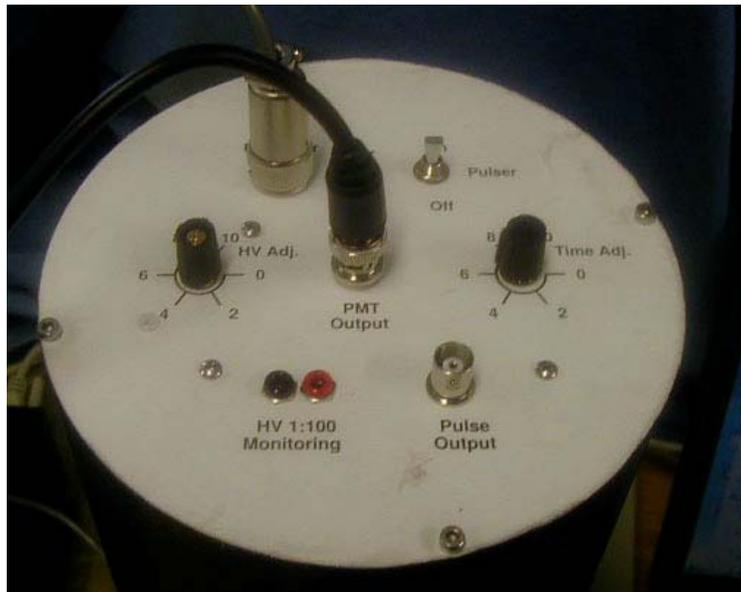
A pulser inside the detector tube can drive a light emitting diode (LED) imbedded in the scintillator when turned on by the toggle switch at the tube top. The pulser produces pulse pairs at a fixed frequency of 100 Hz while the time between pulses within a pair is adjusted by the knob labeled *Time Adj*. The pulser output voltage is accessible at the connector labeled *Pulse Output*.



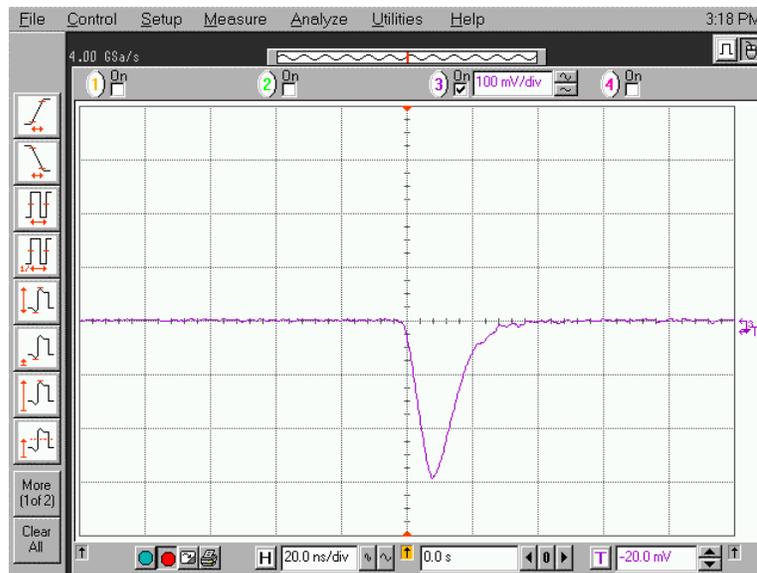
**Figure 5.** Front of the electronics box.



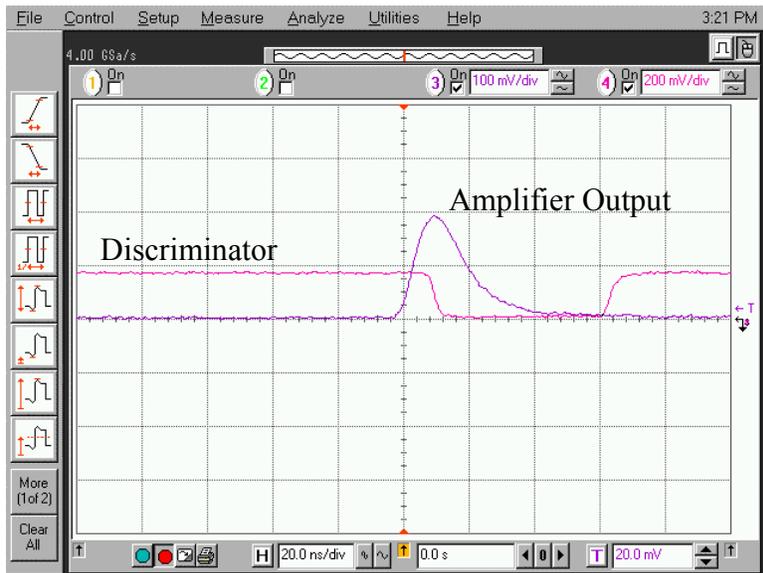
**Figure 6.** Rear of electronics box. The communications ports are on the left. Use only one.



**Figure 7.** Top view of the detector lid. The HV adjustment potentiometer and monitoring ports for the PMT are located here.



**Figure 8.** Output pulse directly from PMT into a  $50\Omega$  load. Horizontal scale is 20 ns/div and vertical scale is 100 mV/div.



**Figure 9.** Amplifier output pulse from the input signal from figure 45 and the resulting discriminator output pulse. Horizontal scale is 20 ns/div and the vertical scale is 100 mV/div (amplifier output) and 200 mV/div (discriminator output).

## Software and User Interface

Software is used to both help control the instrument and to record and process the raw data. There is also software to simulate muon decay data. All software is contained on the CD that accompanies the instrument and can also be freely downloaded from [www.muon.edu](http://www.muon.edu). (Both Microsoft and Linux operating systems are supported.) Source code for the user interface and the data fitting software is provided. It is written in the Tcl/Tk scripting language.

All of the software can be run from either CD or copied to disk. The muon decay simulation software can be run without any of the detector electronics present. Table 21 lists the software.

Table 2. Software

Program name	Description
Muonmain.exe	Main control program for Microsoft
Muonlinux	Main control program for Linux
muonmain.tcl	Tcl/Tk language support file for Microsoft
muonlinux.tcl	Tcl/Tk language support file for Linux
03-07-13-15-39.data	Data file
muon.data	
	Simulation program
Xyz.dll	support file

The program you will probably use the most is either muonmain or muonlinux, depending on whether you are using the Microsoft or Linux operating system, respectively. These are the principal data acquisition programs. This program stores its data in a file with the extension “data” with a main name derived from the year, month, day and time, in that order, when written in numerical form. (For example, the file 03-07-15:39 corresponds to a data file written 15 July 2003 at 3:39pm. Minutes and hours are written in 24-hour notation.)

Files with the extension “tcl” and “dll” are support programs that you do not need to modify for normal running. The Tcl files are however useful to read if you want to see how the user interface and our curve fitter are written in the Tcl/Tk scripting language.

The program “muonmain” (or muonlinux if Linux is your operating system) is the main data acquisition program. After you launch it, you will first see the user interface shown in figure fig\_user\_iface. The interface allows you to set port settings on your PC, to observe various data rates, to control how data is displayed on the PC, and to fit the collected data.

There are 5 sections to the main display panel:

- Control
- Muon Decay Time Histogram
- Monitor
- Rate Meter
- Muons through detector

## Control

The *Configure* menu is shown in figure fig\_config. This menu allows you to specify which communications port (com1, com2, com3 or com4) that you will connect to the electronics box. The maximum x-axis value for the histogram of the muon decay times and the number of data bins is set here. There are also controls for reading back all ready collected data. This is explained below in section ??? The blue colored Save/exit switch is used to finalize your selection(s).

The *Start* button initiates a measurement using the settings selected from the configure menu. After selecting it, you will see the “Rate Meter” and the “Muons through detector” graphs show activity.

The *Pause* button temporarily suspends data acquisition so that the three graphs stop being updated. Upon selection, the button changes its name to *Resume*. Data taking resumes when the button is selected a second time.

The *Fit* button when selected will prompt the use for a password. (The instructor can change the password.) If the correct password is entered, the data displayed in the decay time histogram is fit and the results displayed in the upper right hand side of the graph. Data continues to be collected and displayed. The fit curve drawn through the data points disappears once a new data point is collected but results of the fit remain.

The *View Raw Data* button opens a window that allows you to display the timing data for a user selected number of events, with the most recent events read in first. Here an event is any signal above the discriminator threshold so it includes data from both through going muons as well as signals from muons that stop and decay inside the detector. Each data record contains two fields of information.

The first field is the absolute time, as recorded by the PC, in the format year/month/day-hour: minute: second. For example, the field 03/07/14-15:55:24 corresponds to the time 3:55:24 PM on 14 July 2003.

The second field is an encoded positive integer that contains information about the time between successive signals that triggered the readout electronics, and possibly the number of decays in the one-second interval identified by the corresponding data in the first column. An integer **less** than 40000 is simply the number of clock cycles between successive signals and, background aside, identifies a muon decay. Multiplying this

integer by the timing circuit clock period of 20 nanosec converts it into an actual time. For example, the integer 300 corresponds to a time difference between successive signals of 6  $\mu$ sec. Only data of this type is entered automatically into the decay time histogram.

An integer **greater than or equal to 40000** corresponds to the situation where the time between successive signals exceeded the timing circuit's maximum number of 40000 clock cycles. A non-zero number in the units place indicates the number of times this "timeout" situation occurred in the particular second identified by the data in the first field. For example, the integer 40005 in the second field indicates that the readout circuit was triggered 5 times in a particular second but that each time the timing circuit reached its maximum number of clock cycles before the next signal arrived.

The *Quit* button stops the measurement and asks you whether you want to append the data. Answering *No* writes the data to a file that is named after the date and time the measurement was originally started, i.e., 03-07-13-17-26.dat.

### **Data file format**

Timing information about each signal above threshold is written to disk. For a measurement session can be written the raw data written to file. See the description in Control/View Raw Data.

### **Utility software**

We need to write something here ????????????????????

### **Monitor**

This panel shows rate-related information for the current measurement. The elapsed time of the current measurement is shown along with the accumulated number of times from the start of the measurement that the readout electronics was triggered (*Number of Triggers*). The *Trigger rate* is the number of times the readout electronics was triggered in the previous second. The number of pairs of successive signals where the time interval between successive signals is less than the maximum number of clock cycles of the timing circuit is labeled *Muon decay*, even though some of these events may be background events and not real muon decays. Finally, the number of muon decays per minute is displayed as *Decay rate*.

### **Rate Meter**

This continuously updated graph plots the number of signals above discriminator threshold versus time. It is useful for monitoring the overall trigger rate.

## Muons through Detector

This graph shows the time history of the number of signals above threshold. Its time scale is automatically adjusted and is intended to show time scales much longer than the rate meter. This graph is useful for long term monitoring of the trigger rate. Strictly speaking, it includes signals from not only through going muons but any source that might produce a trigger. The horizontal axis is time, indicated down to the second. The scale is sliding so that the far left-hand side always corresponds to the start of the measurement session. The bin width is indicated in the upper left-hand portion of the plot.

## Muon Decay Time Histogram

This plot is probably the most interesting one to look at. It is a histogram of the time difference between successive triggers and is the plot used to measure the muon lifetime. The horizontal scale is the time difference between successive triggers in units of microseconds. Its maximum displayed value is set by the *Configure* menu. (All time differences less than 20  $\mu\text{sec}$  are entered into the histogram but may not actually be displayed due to menu choices.) You can also set the number of horizontal bins using the same menu. The vertical scale is the number of times this time difference occurred and is adjusted automatically as data is accumulated. A button (*Change y scale Linear/Log*) allows you to plot the data in either a linear-linear or log-linear fashion. The horizontal error bars for the data points span the width of each timing bin and the vertical error bars are the square root of the number of entries for each bin.

The upper right hand portion of the plot shows the number of data points in the histogram. Again, due to menu selections not all points may be displayed. If you have selected the *Fit* button then information about the fit to the data is displayed. The muon lifetime is returned, assuming muon decay times are exponentially distributed, along with the chi-squared per degree of freedom ratio, a standard measure of the quality of the fit. (See Bevington for more details.)

A *Screen capture* allows you to produce a plot of the display. **More detail needed here.**

## Our Lifetime Fitter

Our muon lifetime fitter for the decay time histogram assumes that the distribution of times is the sum of an exponential distribution and a flat distribution. The exponential distribution is attributed to real muon decays while the flat distribution is attributed to background events. The philosophy of the fitter is to first estimate the flat background from the data at large nominal decays times and to then subtract this estimated background from the original distribution to produce a new distribution that can then be fit to a pure exponential.

The background estimation is a multi-step process. Starting with the raw distribution of decay times, we fit the distribution with an exponential to produce a tentative lifetime  $\tau'$ . We then fit that part of the raw distribution that have times greater than  $5\tau'$  with a

straight line of slope zero. The resulting number is our first estimate of the background. We next subtract this constant number from all bins of the original histogram to produce a new distribution of decay times. Again, we fit to produce a tentative lifetime  $\tau''$  and fit again that part of this new distribution that have times greater than  $5\tau''$ . The tentative background level is subtracted from the previous distribution to produce a new distribution and the whole process is repeated again for a total of 3 background subtraction steps.

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### General

- <http://www.pdg.lbl.gov>

- [http://people.hofstra.edu/faculty/Stefan\\_Waner/RealWorld/integral/integral.html](http://people.hofstra.edu/faculty/Stefan_Waner/RealWorld/integral/integral.html)
- <http://aero.stanford.edu/StdAtm.html>
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## Getting Started

You cannot break anything unless you drop the detector on the floor or do something equally dramatic. Every cable you need is provided, along with a  $50\Omega$  terminator.

The black aluminum cylinder (“detector”) can be placed in the wooden pedestal for convenience. (The detector will work in any orientation.) Cable types are unique. Connect the power cable and signal cable between the electronics box and the detector. Connect the communication cable between the back of the electronics box and your PC (or laptop). Use **either** the USB connection or the serial port, but not both.

Turn on power to the electronics box. (Switch is at rear.) The red LED power light should now be steadily shining. The green LED may or may not be flashing.

Set the HV between  $-1150$  and  $-1200$  Volts using the knob at the top of the detector tube. The exact setting is not critical and the voltage can be monitored by using the multimeter probe connectors at the top of the detector tube.

If you are curious, you can look directly at the output of the PMT using the *PMT Output* on the detector tube and an oscilloscope. (A digital scope works best.) **Be certain to terminate the scope input at  $50\Omega$  or you signal will be distorted.** You should see a signal that looks like figure 8. The figure shows details like scope settings and trigger levels.

Connect the BNC cable between *PMT Output* on the detector and *PMT Input* on the box. Adjust the discriminator setting on the electronics box so that it is at  $200 - 300$  mV. The green LED on the box front panel should now be flashing.

You can look at the amplifier output by using the *Amplifier Output* on the box front panel and an oscilloscope. **The scope input impedance must be  $50\Omega$ .** Similarly, you can examine the output of the discriminator using the *Discriminator Output* connector. Again, the scope needs to be terminated at  $50\Omega$ . Figure 9 shows typical signals for both the amplifier and discriminator outputs on the same plot. Details about scope time settings and trigger thresholds are on the plot.

Insert the software CD into your PC and copy all the files in the folder (directory) ??? into a convenient folder/directory.

Launch the program *muonmain* if you are running a Microsoft operating system or *muonlinux* if you are running the Linux operating system. You will see the user interface as shown in figure 4 (user\_face fig)

Configure the port on your PC. See the material under *Control* in the section labeled *Software and Front Panel Display* for details.

Click on *Start*. You should see the rate meter at the lower left-hand side of your computer screen immediately start to display the raw trigger rate for events that trigger the readout electronics. The mean rate should be about 6 Hz or so.

## Suggested Student Exercises

1) Measure the gain of the 2-stage amplifier using a sine wave.

Apply a 100kHz 100mV peak-to-peak sine wave to the input of the electronics box input. Measure the amplifier output and take the ratio  $V_{out}/V_{in}$ .

Q: Increase the frequency. How good is the frequency response of the amp?

Q: Estimate the maximum decay rate you could observe with the instrument.

2) Measure the saturation output voltage of the amp.

Increase the magnitude of the input sine wave and monitor the amplifier output.

Q: Does a saturated amp output change the timing of the FPGA? What are the implications for the size of the light signals from the scintillator?

3) Examine the behavior of the discriminator by feeding a sine wave to the box input and adjusting discriminator threshold. Monitor the discriminator output.

4) Measure the timing properties of the FPGA:

a) Using the pulser on the detector, measure the time between successive rising edges on an oscilloscope. Compare this number with the number from software display.

b) Measure the linearity of the FPGA:

Alter the time between rising edges and plot scope results v. FPGA results;

Can use time between 1  $\mu$ s and 20  $\mu$ s in steps of 2  $\mu$ s.

c) Determine the timeout interval of the FPGA by gradually increasing the time between successive rising edges of a double-pulse and determine when the FPGA no longer records results;

Q: What does this imply about the maximum time between signal pulses?

d) Decrease the time interval between successive pulses and try to determine/bound the FPGA internal timing bin width.

Q: What does this imply about the binning of the data?

Q: What does this imply about the minimum decay time you can observe?

- 5) Adjust (or misadjust) discriminator threshold.  
Increase the discriminator output rate as measured by the scope or some other means.  
Observe the raw muon count rate and the spectrum of "decay" times. (This exercise needs a digital scope and some patience since the counting rate is "slowish.")
- 6) What HV should you run at? Adjust/misadjust HV and observe amp output. (We know that good signals need to be at about 200 mV or so before discriminator, so set discriminator before hand.) With fixed threshold, alter the HV and watch raw muon count rate and decay spectrum.
- 7) Connect the output of the detector can to the input of the electronics box. Look at the amplifier output using a scope. (A digital scope works best.) **Be sure that the scope input is terminated at 50Ω.** What do you see? Now examine the discriminator output simultaneously. Again, be certain to terminate the scope input at 50Ω. What do you see?
- 8) Set up the instrument for a muon lifetime measurement.  
Start and observe the decay time spectrum.  
Q: The muons whose decays we observe are born outside the detector and therefore spend some (unknown) portion of their lifetime outside the detector. So, we never measure the actual lifetime of any muon. Yet, we claim we are measuring the lifetime of muons. How can this be?
- 9) Fitting the decay time histogram can be done with the included fitter or with your own.
- 10) From your measurement of the muon lifetime and a value of the muon mass from some trusted source, calculate the value of Fermi coupling constant  $G_F$ . Compare your value with that from a trusted source.
- 11) Using the approach outlined in the text, measure the charge ratio  $\rho$  of positive to negative muons at ground level or at some other altitude.
- 12) Following the approach in the manual, measure the muon stopping rate at two different elevations and compare predictions that do and do not assume the time dilation effect of special relativity.

13) Once the muon lifetime is determined, compare the theoretical binomial distribution with an experimental distribution derived from the random lifetime data of individual muon decays. For example, let  $p$  be the (success) probability of decay within 1 lifetime,  $p = 0.73$ . The probability of failure  $q = 1 - p$ . Take a fresh data sample of 2000 good decay events. For each successive group of 50 events, count how many have a decay time of less than 1 lifetime. (On average this is 35 or so). Histogram the number of "successes." This gives you 40 experiments to do. The plot of 40 data points should have a mean at  $50 \cdot 0.73$  with a variance  $\sigma^2 = Npq = 50 \cdot 0.73 \cdot 0.37 = 13.5$ . Are the results consistent with a Poisson probability distribution?