Charm and Bottom Quark Production

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- Statement of the problem
- Status report:

Comparison of Data & Theory

- How do we make heavy quarks
- B-Hadroproduction: A case study
- Mass-Independent Evolution

Why is it valid?

Conclusions

>Lunch

Standard Disclaimer

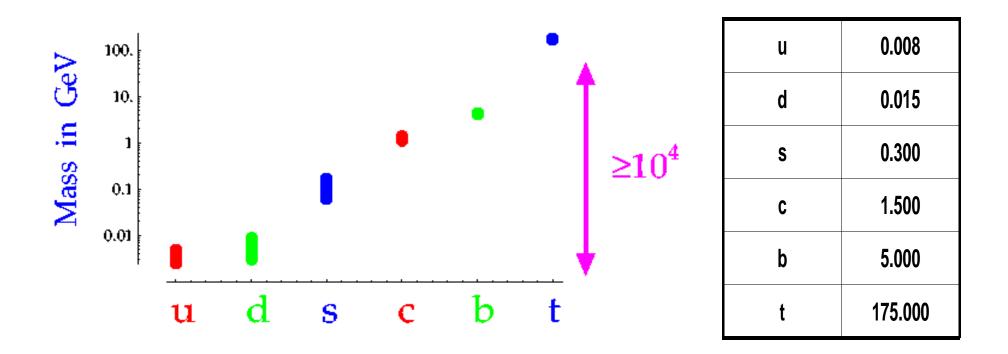
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What is the ideal way to learn about quark masses and their effects on a physical process?

As a theorists, I simply run my calculation over the full range of mass values from 0 to ∞, and study the behavior.

Wouldn't it be great if the experiments could do the same???

Quark Masses Span Wide Dynamical Range ~ 10⁴



We can't vary the quark mass continuously, but these ``notches'' on our control panel give us a lot of flexibility

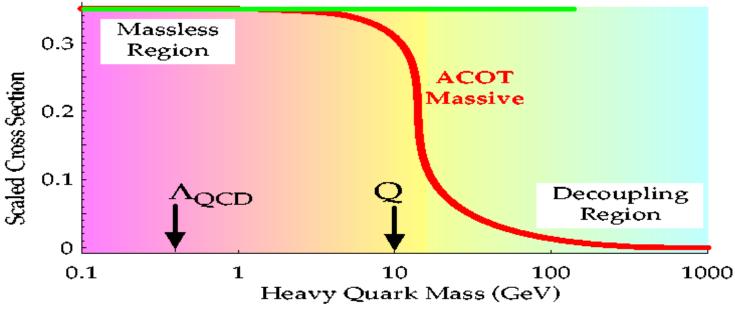
The DOWN Side

Theorists would much prefer that quark masses only come in 2 varieties:

m = 0: Massless case. Mass plays no dynamic role Well understood.

$m = \infty$: Infinite case.

Mass Decouples. We can forget about this object



MS-Bar Massless

Single-Scale Problem in Perturbation Theory:

$$\sigma = \sum_{N=1}^{\infty} (\alpha_s L)^N = \sum_{N=1}^{\infty} \left\{ \alpha_s(\mu) \log\left(\frac{E^2}{\mu^2}\right) \right\}^N$$

... where E is any relevant scale of the problem: Q, P_T , E_T ,...

Use RGE to solve this.
$$\frac{d\sigma}{d\log\mu^2} =$$

Multi-Scale Problem in Perturbation Theory:

What do we do if we have 2 scales???

$$\log\left(\frac{E^2}{\mu^2}\right) = \log\left(\frac{M_H^2}{\mu^2}\right)$$

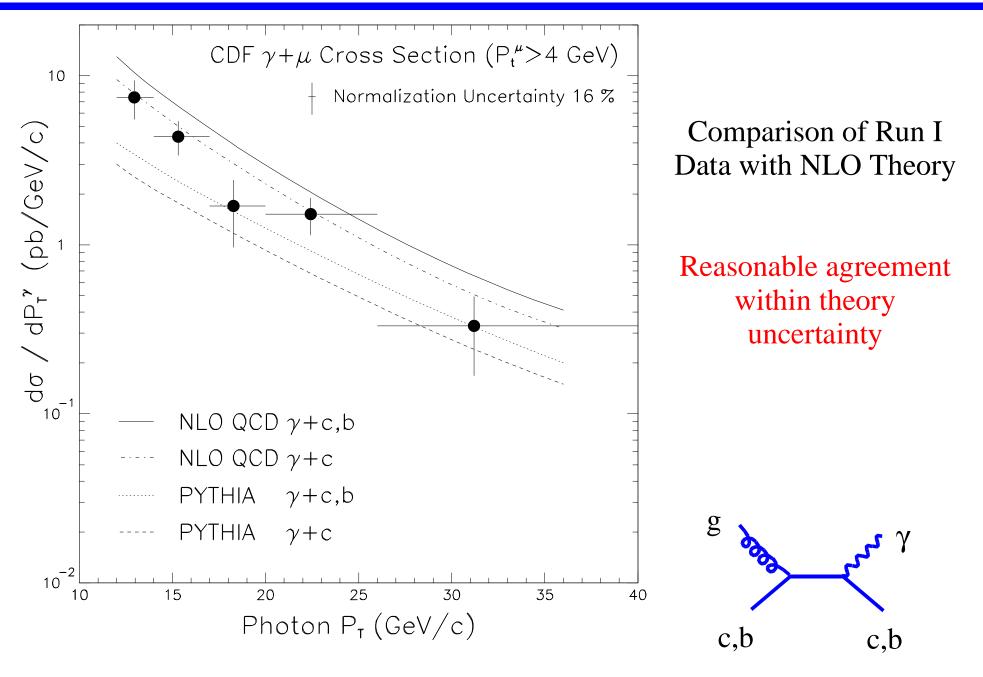
... life gets interesting.

...

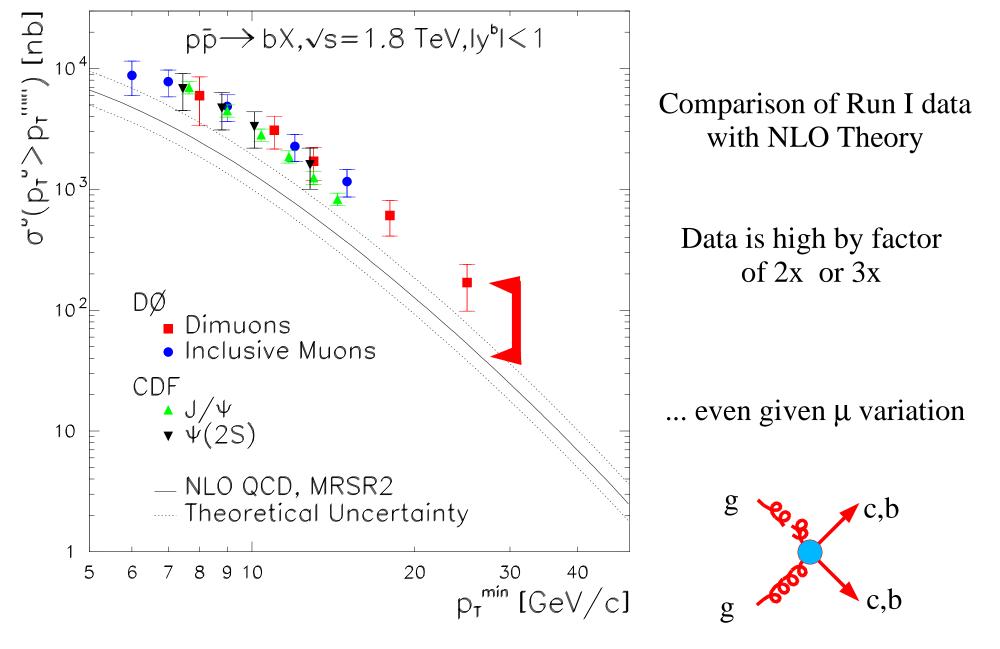
Status Report:

Comparison of Data & Theory

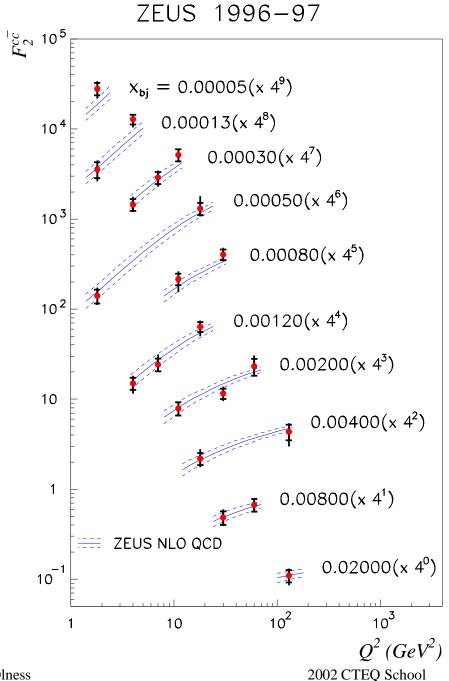
Hadroproduction of Charm (& Beauty) at Tevatron



Hadroproduction of Beauty at Tevatron



Charm Production at HERA



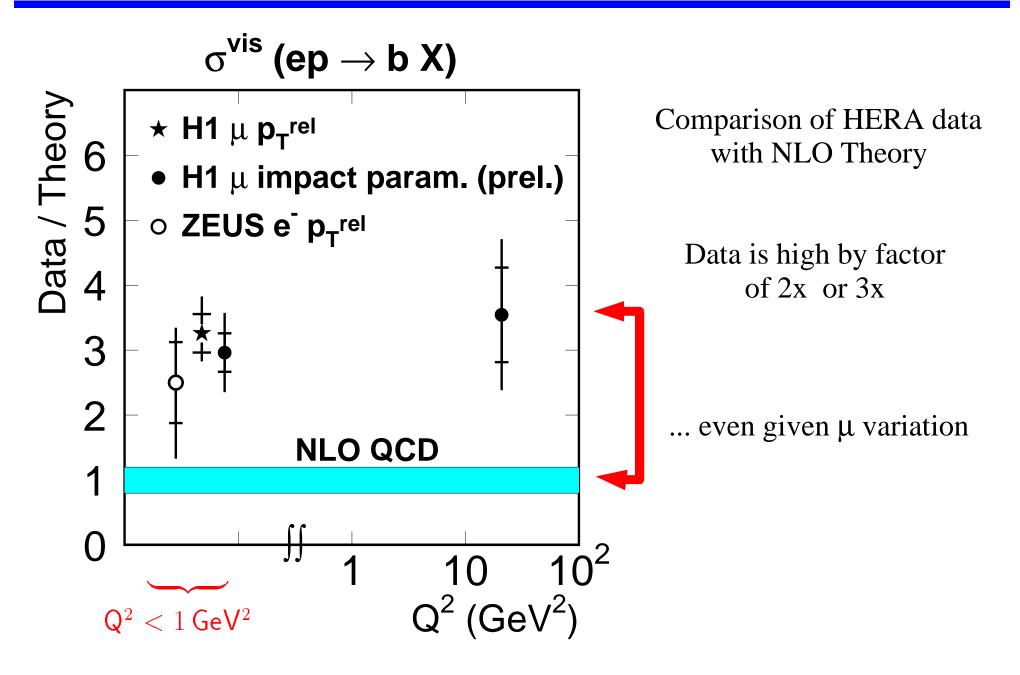
At HERA, Charm production matches well with NLO calculation

What about beauty???

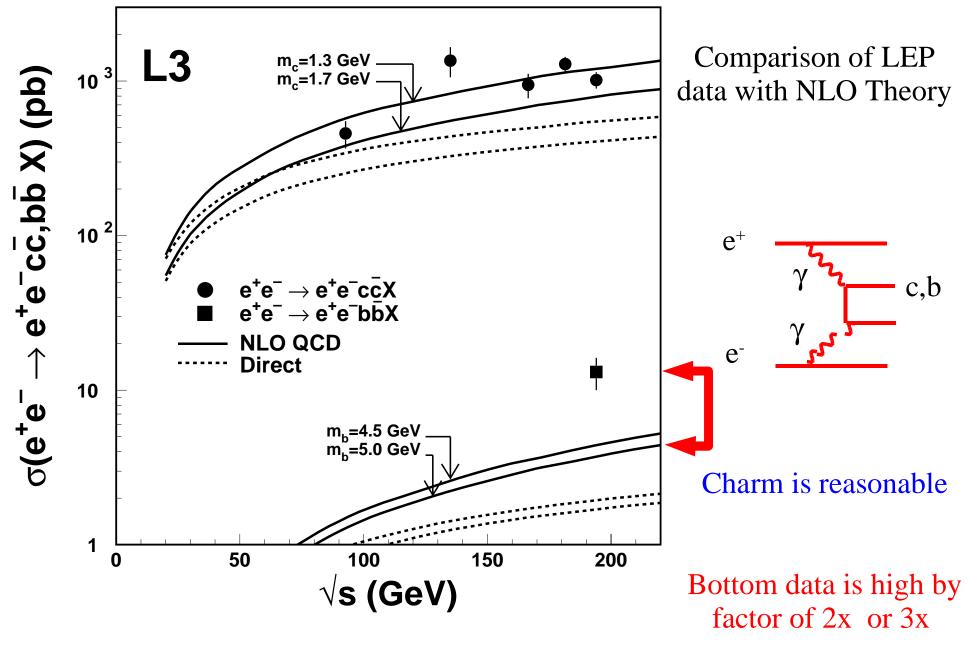


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Beauty Production at HERA



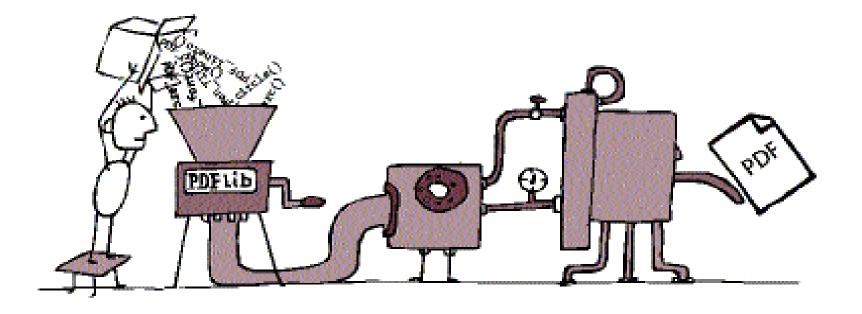
Charm and Bottom Production at LEP



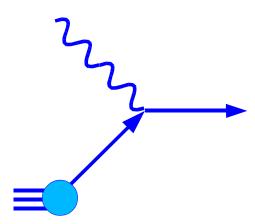
General Trend: Charm: in good shape Bottom: data lies above theory

How can this make sense??? $m_b \approx 4.5 \text{ GeV}$ $m_c \approx 1.5 \text{ GeV}$ $Log[m_b/m_c] \approx Log[3] \approx \text{ Not a big number!!!}$ $\alpha_s(m_b) < \alpha_s(m_c)$

How do we make heavy quarks



Production of Heavy Quarks: The Problem



Which is the correct production mechanism?



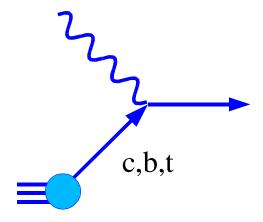
Quark	Channel
S	YES
t	NO
С	???
b	???

Heavy Creation (HC)

Quark	Channel
S	NO
t	YES
С	???
b	???

If you can't beat 'em, join 'em.

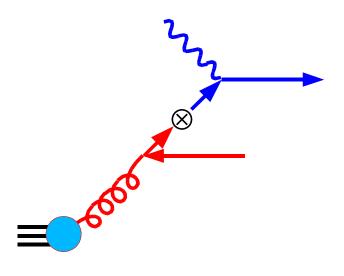
How to Join without ``Double Counting"???



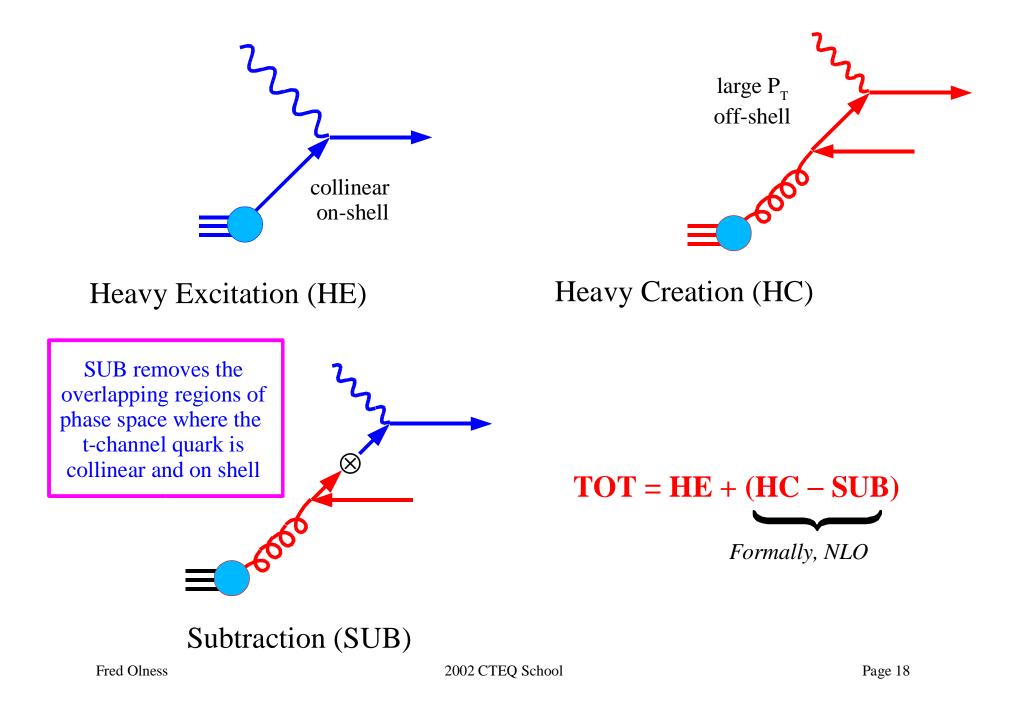
Heavy Excitation (HE)

Wait a minute! Since the heavy quark originally came from a gluon splitting, these diagrams are *Double Counting* Heavy Creation (HC)

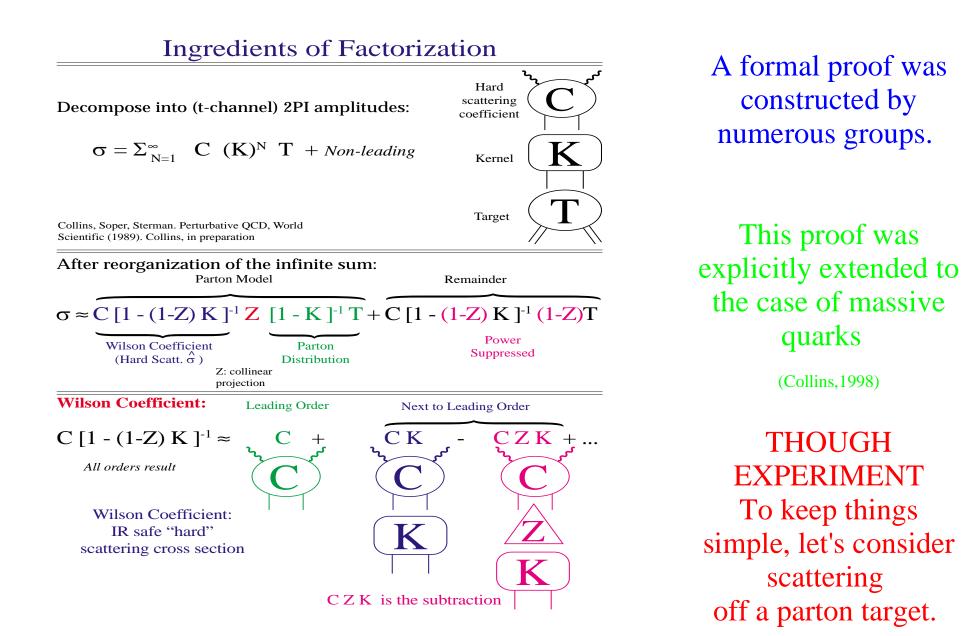
c,b,t



How to Join without ``Double Counting"???



There is a rigorous factorization proof ...



Application of Factorization Formula at Leading Order (LO)

Basic Factorization Formula $\sigma = f \otimes \omega \otimes d + O(\Lambda^2/Q^2)$ At Zeroth Order:

$$\sigma^{0} = f^{0} \otimes \omega^{0} \otimes d^{0} + O(\Lambda^{2}/Q^{2})$$

Use: $f^0 = \delta$ and $d^0 = \delta$ for a <u>parton</u> target.

 f^0 f^1 for parton target

Therefore:

$$\sigma^{0} = f^{0} \otimes \omega^{0} \otimes d^{0} = \delta \otimes \omega^{0} \otimes \delta = \omega^{0}$$

$$\sigma^0 = \omega^0$$

Warning: This trivial result leads to many misconceptions at higher orders

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Application of Factorization Formula at Next to Leading Order NLO)

Basic Factorization Formula

$$\sigma = f \otimes \omega \otimes d + O(\Lambda^2/Q^2)$$

f0

f1

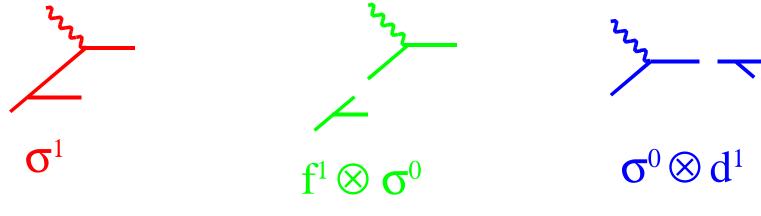
At First Order:

$$\sigma^{1} = f^{1} \otimes \omega^{0} \otimes d^{0} + f^{0} \otimes \omega^{1} \otimes d^{0} + f^{0} \otimes \omega^{0} \otimes d^{1}$$
$$\sigma^{1} = f^{1} \otimes \sigma^{0} + \omega^{1} + \sigma^{0} \otimes d^{1}$$

We used: $f^0 = \delta$ and $d^0 = \delta$ for a <u>parton</u> target.

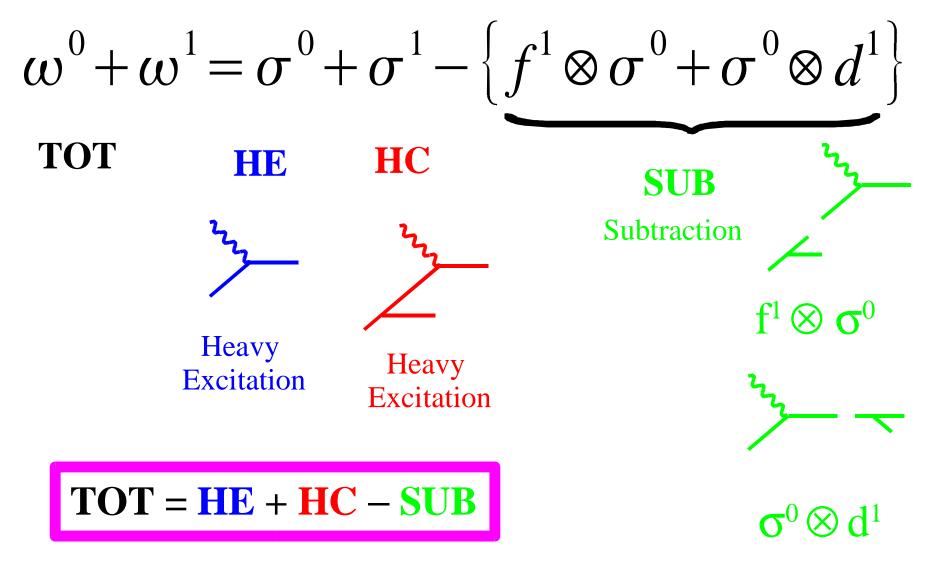
Therefore:

$$\omega^{1} = \sigma^{1} - f^{1} \otimes \sigma^{0} - \sigma^{0} \otimes d^{1}$$

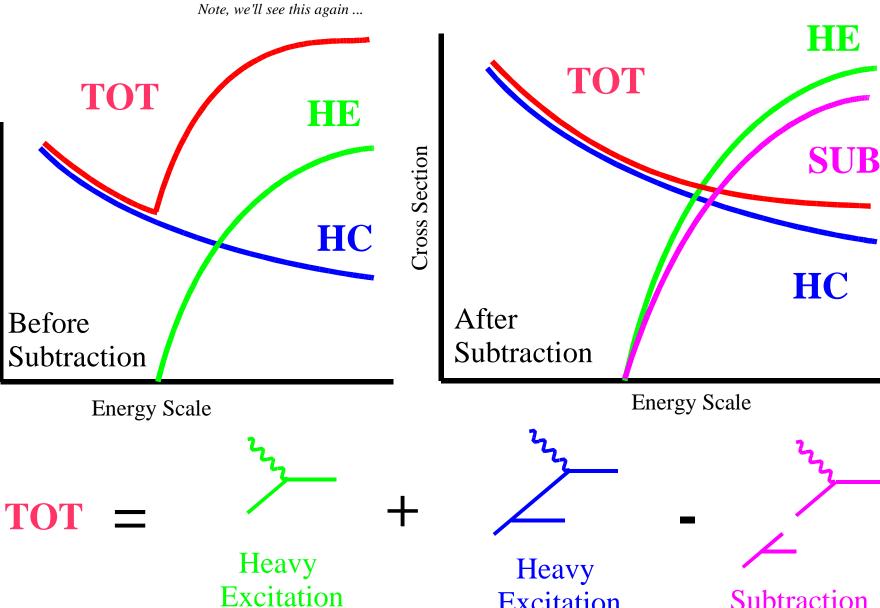


Application of Factorization Formula at Next to Leading Order (NLO)

Combined Result:



Interaction of the separate contributions vs. energy scale

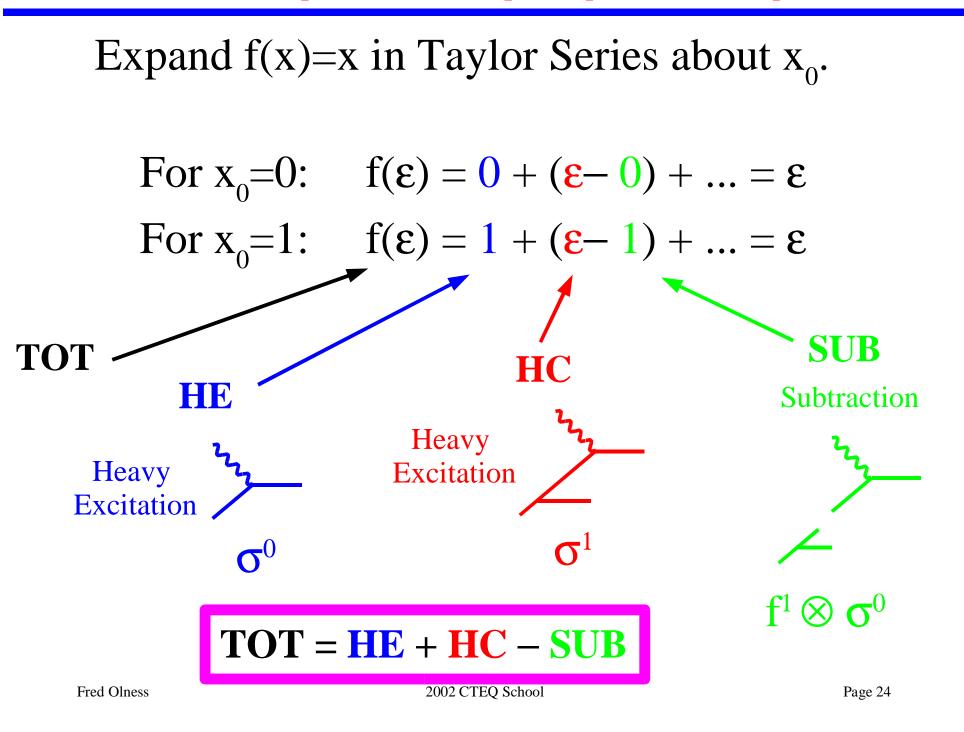


Subtraction

Cross Section

Excitation

An Example: How the separate pieces can conspire



It doesn't matter which expansion point you use; QCD will compensate (if you go to high enough order).

In practice ...

we are often limited to low-order calculations, so it is wise to choose your expansion point carefully.

HOMEWORK PROBLEM: WILSON COEFFICIENTS

Use the Basic Factorization Formula

$$\sigma = f \otimes \omega \otimes d + O(\Lambda^2 / Q^2)$$

At Second Order:

$$\sigma^{2} = f^{2} \otimes \omega^{0} \otimes d^{0} + \dots$$
$$f^{1} \otimes \omega^{1} \otimes d^{0} + \dots$$

Therefore:

$$\omega^2 = ???$$

- Compute ω^2 at second order.
- Make a diagrammatic representation of each term.

Part 1) Show these 3 definitions are equivalent; work out the limits of integration.

$$f \otimes g = \int f(x)g(y)\delta(z - x * y) dx dy$$
$$f \otimes g = \int f(x)g(\frac{z}{x})\frac{dx}{x}$$
$$f \otimes g = \int f(\frac{z}{y})g(y)\frac{dy}{y}$$

Part 2) Show convolutions are the ``natural" way to multiply probabilities.

If f represents the heads/tails probability distribution for a single coin flip, show that the distribution of 2 coins is $f \oplus f$ and 3 coins is $f \oplus f \oplus f$.

$$f \oplus g = \int f(x)g(y)\delta(z - (x + y))dx dy$$
$$f(x) = \frac{1}{2}(\delta(1 - x) + \delta(1 + x))$$

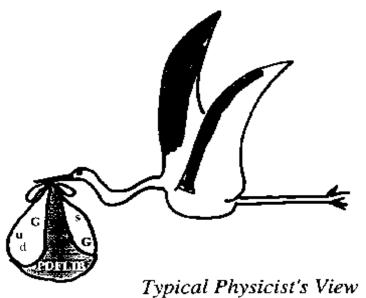
BONUS: How many processes can you think of that don't factorize?

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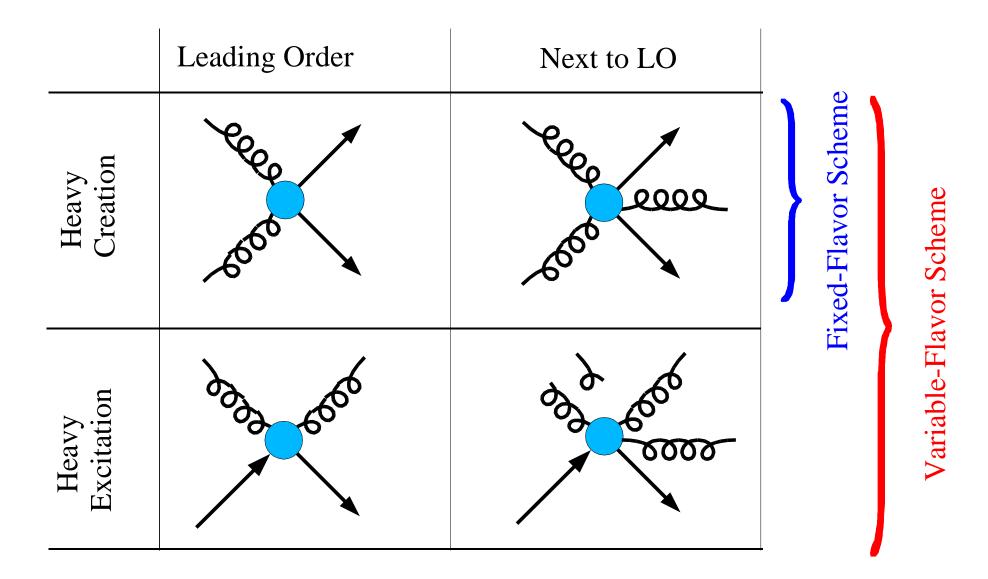
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B-Hadroproduction: A Case Study

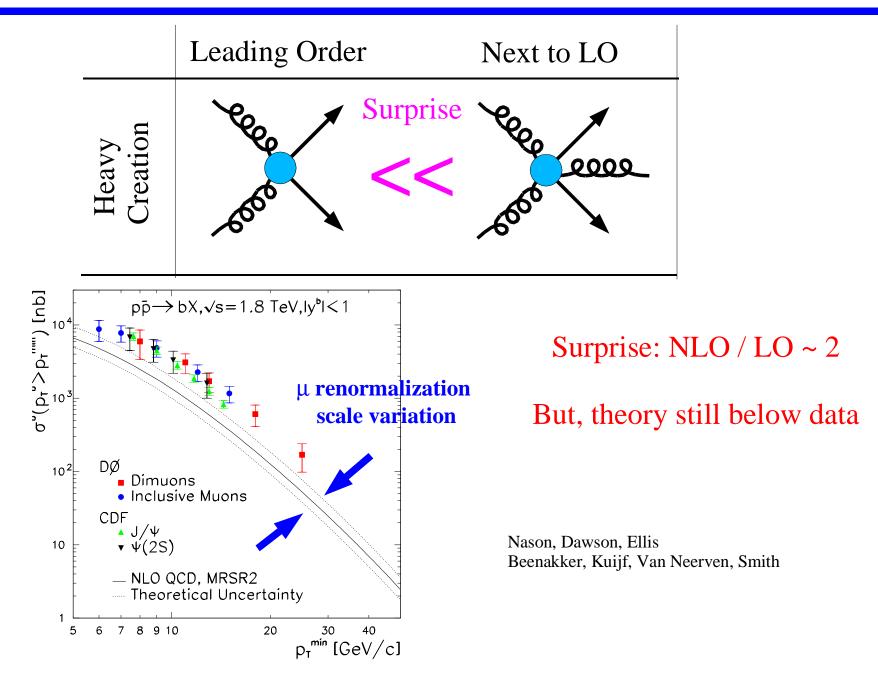
Where do PDF's come from???



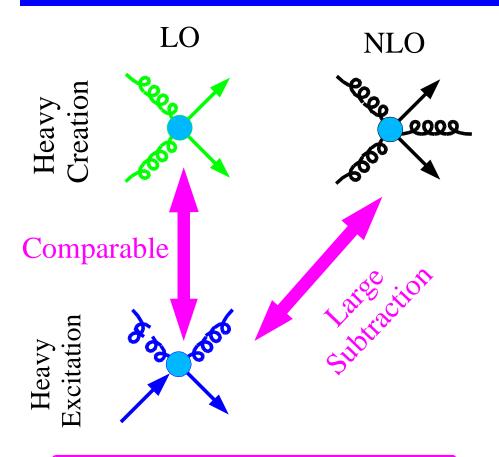
Drawing by Heidi Schellman 2002 CTEQ School



NLO Fixed-Flavor Scheme



NLO Variable Flavor Scheme



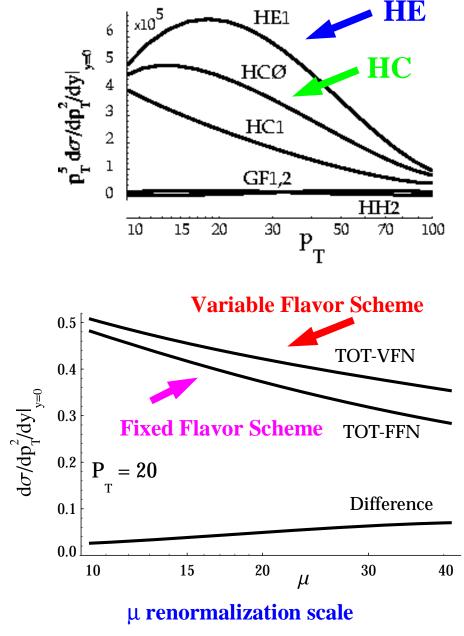
Net result:

- Reduction of µ-dependence
- 30% to 50% increase in σ

Aivazis, Collins, Olness, Tung Olness, Scalise, Tung

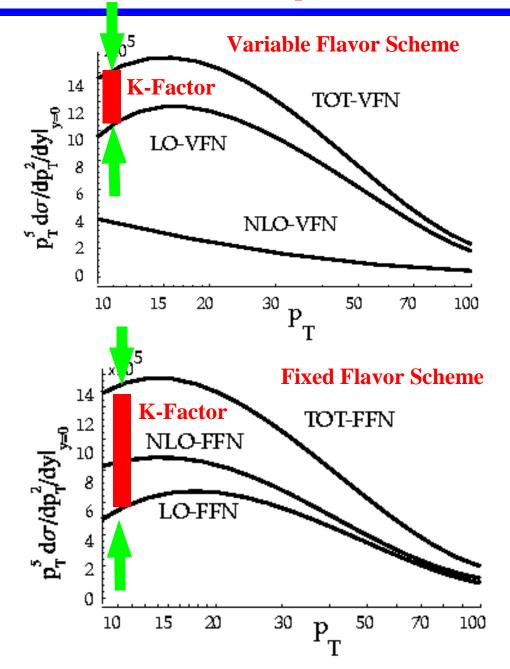
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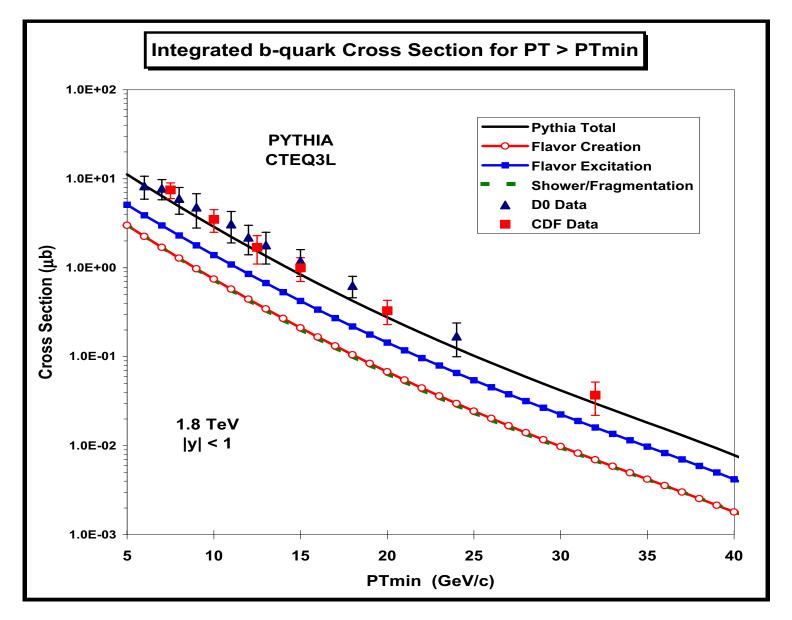
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Compare Fixed & Variable Flavor Scheme

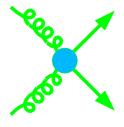


- To NLO, different schemes are comparable.
- K-Factor very different.
- Suggestion: VFS may provide more efficient organization of perturbation series than FFS.
- Recall: Choice of expansion point x₀ in Taylor series.

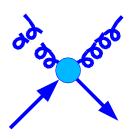
b-Quark Hadroproduction via Monte Carlo



Flavor Creation



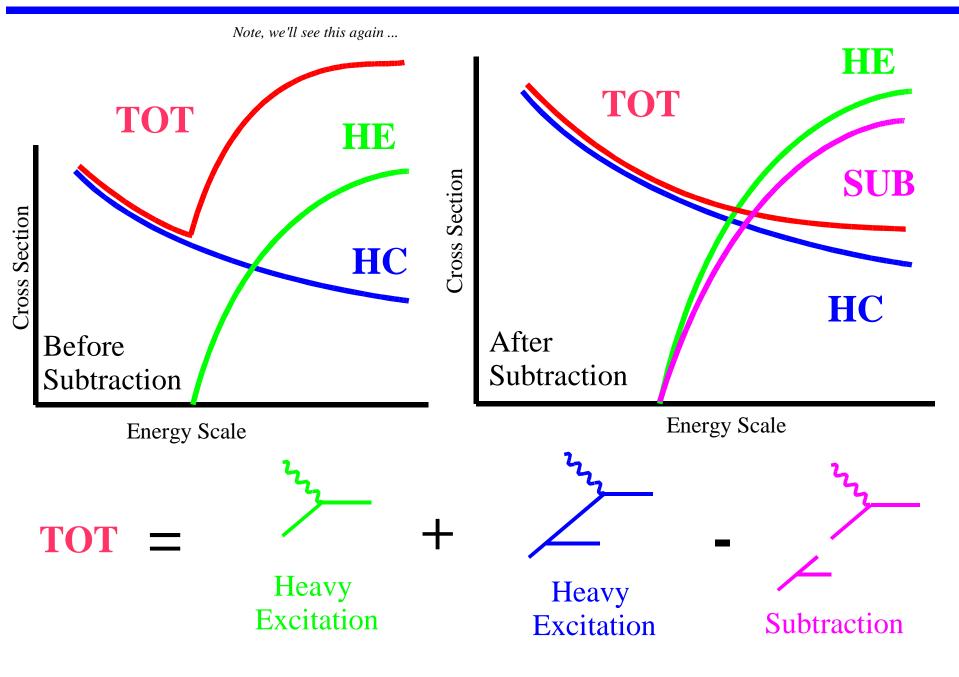
Flavor Excitation



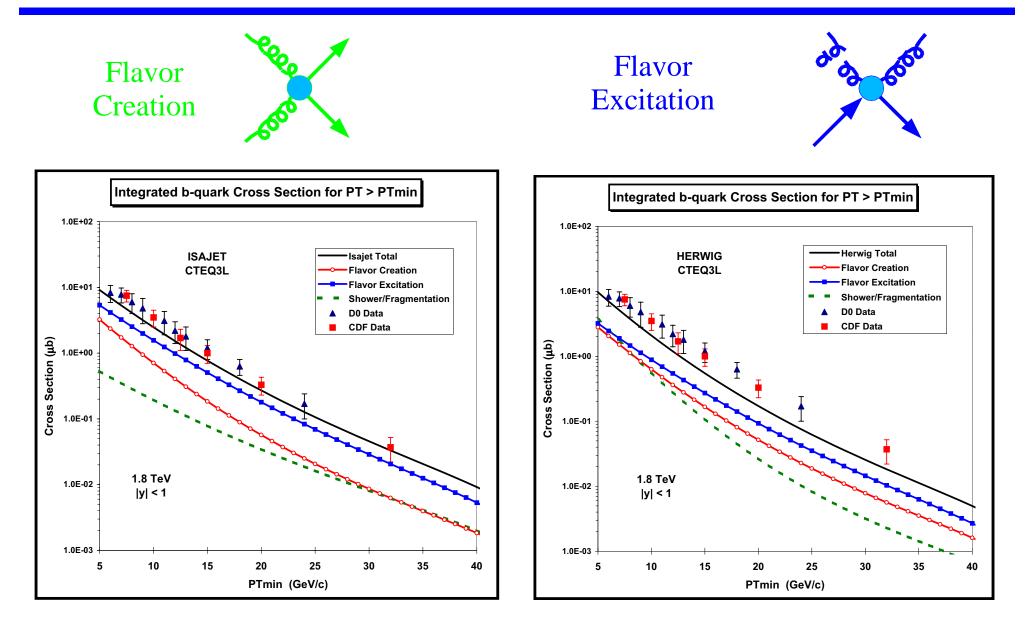
R. Field, hep-ph/0201112

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Recall



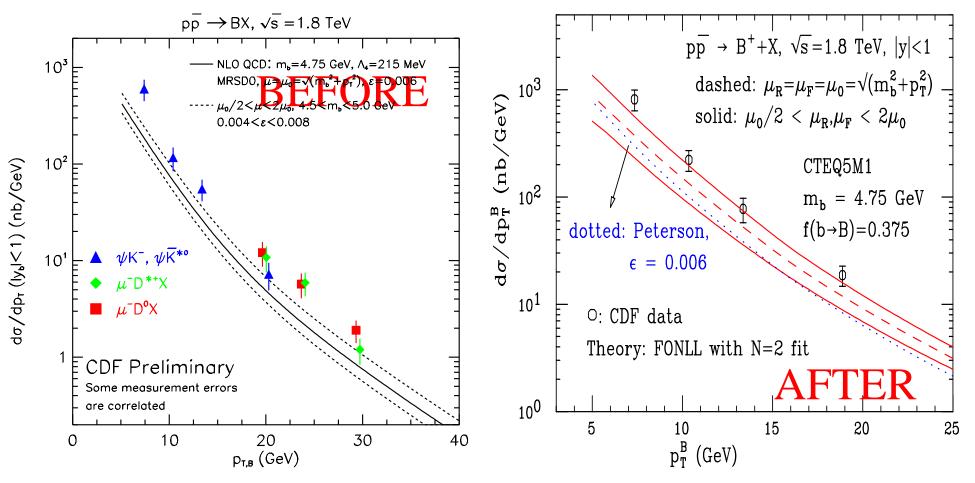
b-Quark Hadroproduction via Monte Carlo



R. Field, hep-ph/0201112

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B production with modified fragmentation function

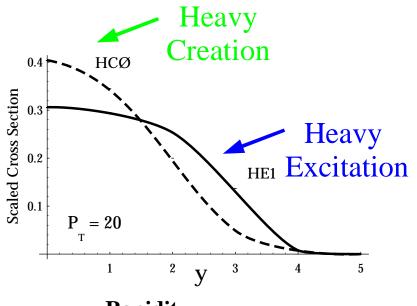


Cacciari & Nason hep/ph-0204025 Cacciari, Greco, Nason, JHEP 9805:007, 1998 Cacciar & Greco, Nuc.Ph.B421:530, 1994

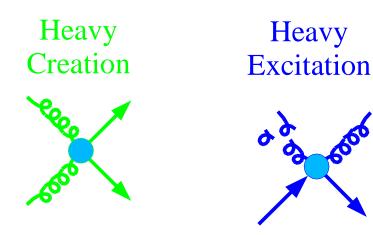
The effect of modifying the bottom fragmentation function raises theory predictions in the range of data

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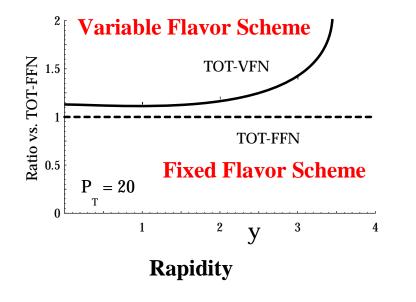
Rapidity Distribution

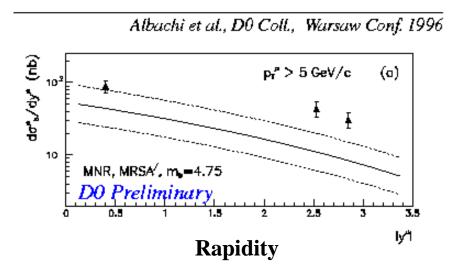


Rapidity



Different processes have different kinematic distributions

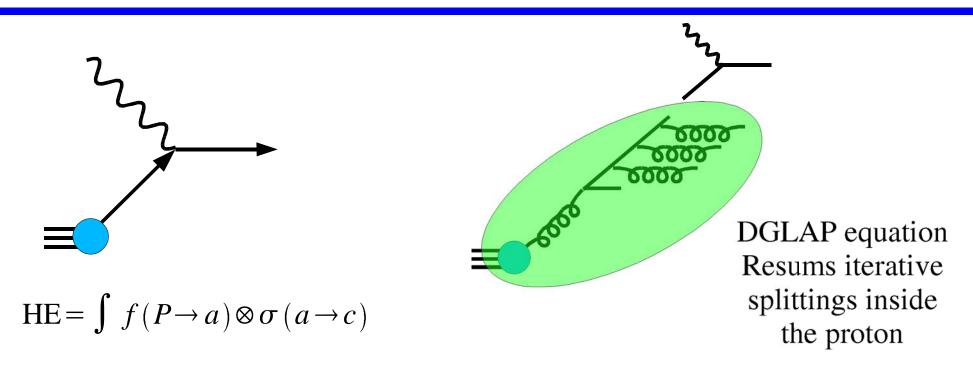




Mass-Independent Evolution.

Why is it valid?

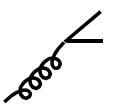
DGLAP Equation and the Heavy Quark PDF



DGLAP Equation
$$\frac{df_i}{d\log\mu^2} = \frac{\alpha_s}{2\pi} P_{j\to i} \otimes f_j + \dots$$

Splitting Function

$${}^{1}P_{g \to q} = \frac{1}{2} \left[x^{2} + (1-x)^{2} \right] + \left(\frac{M_{H}^{2}}{\mu^{2}} \right) \left[x(1-x) \right]$$

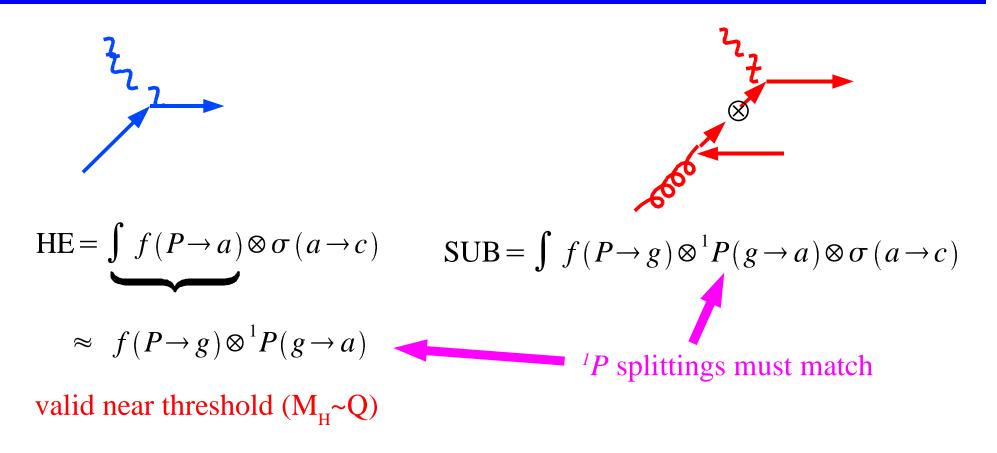


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Effect of Heavy Quark Mass in the Calculation



In Summary:

Near threshold($M_{H} \sim Q$), mass effects cancel between HE and SUB

Above threshold($M_{H} \ll Q$), mass effects can be ignored

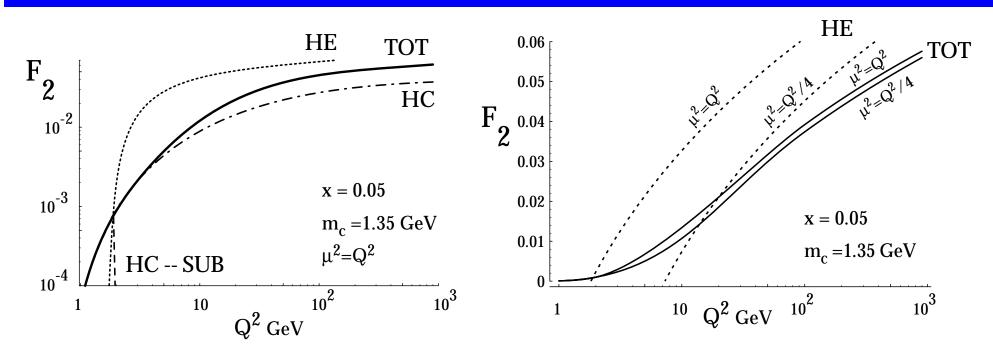
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0.08 0.08 Massive Massive HE 0.07 0.07 **Massless** Massless 0.06 0.06 F₂ 0.05 0.05 TOT Q = 10 GeVSUB 2 0.04 0.04 x = 0.050.03 0.03 Q =10 GeV HE - SUB HE - SUB 0.02 0.02 x = 0.05 0.01 0.01 0 2 10 15 20 3 7 5 2 3 7 10 15 20 1 5 $\mu \, GeV$ μ GeV $HC = \int f(P \to g) \otimes \sigma(g \to c)$ $\text{HE} = \int f(P \rightarrow a) \otimes \sigma(a \rightarrow c)$ $SUB = \int f(P \to g) \otimes {}^{1}P(g \to a) \otimes \sigma(a \to c)$

Effect of Heavy Quark Mass in the Calculation is Trivial

Variation of σ vs. renormalization scale μ



LO = HE result is very sensitive to the choice of scale (i.e., $\mu^2 = Q^2$ or $Q^2/4$) TOT result (higher order) is stable w.r.t. the choice of scale

An accurate calculation must be stable as the renormalization scale varies

Conclusions

... or, lunch is just around the corner

Charm & Bottom Quark Production

- An interesting subject because:
 - Lots of data at present; more in near future
 - Theoretical issues of multi-scale problem
- A fascinating subject because:
 - Theory & data not fully consistent
 - This should be a region we can compute



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