

# Modern Physics

## Problem Set 13

### JC-58) Quantum Numbers for Hydrogen

Explain why the following sets of quantum numbers ( $n, l, m_l, m_s$ ) are not permitted for hydrogen.

- (10 points) (2, 2, -1, +1/2)
- (10 points) (3, 1, +2, -1/2)
- (10 points) (4, 1, +1, -3/2)
- (10 points) (2, -1, +1, +1/2)

### JC-59) Stern-Gerlach Revisited

(20 points) Suppose the silver atoms in the Stern-Gerlach experiment traveled horizontally, first 1 m through the magnet and then after exiting the magnet, 1 m in a field-free region at a speed of 250 m/s.

What must have been the gradient of  $B_z$ ,  $dB_z/dz$ , in order that the beams each be deflected a maximum of 0.5 mm from the central position?

### JC-60) SWE for 2 Particles

(10 points) Derive an expression for the energy of a two-particle system using the wave function given in equation 8-17 in your text. Assume particle 1 is in the  $n = 1$  state and particle two is in the  $n = 2$  state and that the potential is equal to zero ( $U = 0$ ).

### JC-61) Electrons and Pions

Five identical noninteracting particles are placed in an infinite square well with  $L = 1.0$  nm. Compare the lowest total energy for the system if the particles are

- (10 points) electrons.
- (10 points) pions. Pions have symmetric wave functions and their mass is  $264 m_e$ .

### JC-62) The 21 cm Line

One of the most important windows to the mysteries of the cosmos is the *21 cm line*. With it, astronomers map hydrogen (important in star formation) throughout the universe. An important trait is that it involves a highly forbidden transition that is quite long-lived. It is an excellent example of the coupling of angular momenta. Hydrogen's ground state has no spin-orbit interaction. For  $l = 0$ , there is no orbit. However, the proton and electron magnetic moments do interact.

Consider the following model.

- (10 points) The proton sees itself surrounded by a spherically symmetric cloud of  $1s$  electron, which has an intrinsic magnetic dipole moment/spin that has a direction. For the purpose of investigating its effect on the proton, treat this dispersed magnetic moment as behaving effectively like a single loop of current whose radius is  $a_0$ . Then find the magnetic field at the middle of the loop in terms of  $e, \hbar, m_e, \mu_0$ , and  $a_0$ .
- (10 points) The proton sits right in the middle of the electron's magnetic moment. Like the electron, the proton is a spin-1/2 particle, with only two possible orientations in a magnetic field. Noting, however, that its spin and magnetic moment are parallel, rather than opposite, would the interaction energy be lower with the proton's spin aligned or anti-aligned with that of the electron?
- (10 points) For the proton,  $g_p$ , is 5.6. Obtain a rough value for the energy difference between the two orientations.
- (10 points) What would be the wavelength of a photon that carries away this energy difference?

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Talk) **FINAL DRAFT DUE MONDAY NOVEMBER 20 AT 3 PM.**

**(0 points)** Email your pdf to [cooley@physics.smu.edu](mailto:cooley@physics.smu.edu) before due date. If your talk is late less than one hour, your maximum grade will drop one increment (i.e. A  $\rightarrow$  A- ). If your talk is late 1 - 2 hours, your maximum grade drops two increments (A  $\rightarrow$  B+) and so on.