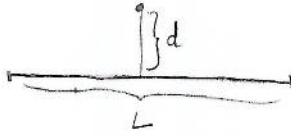


1) A 10 km non-conducting wire of essentially no thickness has 50C placed uniformly on it. What is the strength of the E field 1cm from the wire near the center of its length? [10 pts]



$$\lambda = \frac{Q}{L} = \frac{50\text{C}}{10 \times 10^3\text{m}} = 5 \times 10^{-3} \text{ C/m}$$

$$E = \frac{2k\lambda}{d} = \frac{2 \cdot (9 \cdot 10^9) \cdot (5 \cdot 10^{-3})}{0.01}$$

$$E = 9 \cdot 10^9 \text{ N/C}$$

2) A large (100m by 100m) plate has 10 C uniformly distributed over its surface. What is the difference in electric potential when moving from a distance of 1 cm above the center of the plate to 10 cm? [10 pts]

$$\sigma = \frac{Q}{A} = \frac{10\text{C}}{100\text{m} \times 100\text{m}} = 10^{-3}$$

$$E = \frac{\sigma}{2\epsilon_0} = \frac{10^{-3}}{2 \cdot (8.85 \times 10^{-12})} = 0.0565 \times 10^9 = 5.65 \times 10^7$$

$$\Delta V = -\int \vec{E} \cdot d\vec{s} = -E \cdot \int ds = -E \cdot (d_f - d_i) = -(5.65 \times 10^7) \cdot (0.1 - 0.01)$$

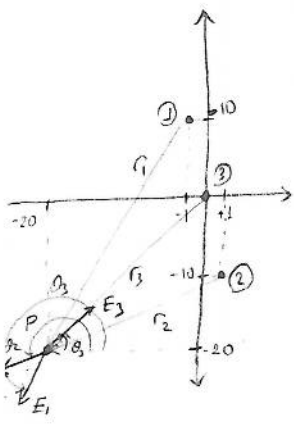
$$\Delta V = -5.08 \times 10^6$$

3) A disk of radius 1m is cut out of the charged plate in Problem 2 above and carried far away. What is the electric potential at a perpendicular distance of 10 cm along the disk axis? [10 pts]

$$\begin{aligned} V &= 2\pi k \sigma [(R^2 + x^2)^{1/2} - x] \\ &= 2\pi (9 \cdot 10^9) (10^{-3}) [(1^2 + 0.1)^{1/2} - 0.1] \\ &= 5.11 \times 10^7 \end{aligned}$$

$$E = \frac{kq}{r^2}, \quad r = \sqrt{\Delta x^2 + \Delta y^2}, \quad \theta = \tan^{-1}\left(\frac{\Delta y}{\Delta x}\right)$$

4) Two 5 mC charges are at (x,y) = (-1cm, +10cm) and (+1cm, -10cm), and one charge is at (0cm, 0cm) with -15 mC. What is the E field at the point (-20cm, -20cm)? [10 pts]



$$r_1 = \sqrt{(-20-(-1))^2 + (-20-10)^2} = \sqrt{(-19)^2 + (-30)^2} = 0,355 \text{ m}, \quad \theta_1 = \tan^{-1}\left(\frac{-30}{-19}\right) = 57,7^\circ \text{ or } 237,7^\circ$$

$$r_2 = \sqrt{(-20-1)^2 + (-20-(-10))^2} = \sqrt{(-21)^2 + (-10)^2} = 0,233 \text{ m}, \quad \theta_2 = \tan^{-1}\left(\frac{-10}{-21}\right) = 25,5^\circ \text{ or } 205,5^\circ$$

$$r_3 = \sqrt{(-20-0)^2 + (-20-0)^2} = \sqrt{(-20)^2 + (-20)^2} = 0,283 \text{ m}, \quad \theta_3 = \tan^{-1}\left(\frac{-20}{-20}\right) = 45^\circ$$

$$E_1 = \frac{(9 \cdot 10^9)(5 \cdot 10^{-3})}{(0,355)^2} = 3,57 \cdot 10^8; \quad E_2 = \frac{(9 \cdot 10^9)(5 \cdot 10^{-3})}{(0,233)^2} = 8,29 \cdot 10^8; \quad E_3 = \frac{(9 \cdot 10^9)(15 \cdot 10^{-3})}{(0,283)^2} = 16,9 \cdot 10^8$$

$$E_x = E_1 \cos \theta_1 + E_2 \cos \theta_2 + E_3 \cos \theta_3 = 2,56 \cdot 10^8; \quad E_y = E_1 \sin \theta_1 + E_2 \sin \theta_2 + E_3 \sin \theta_3 = 5,36 \cdot 10^8$$

$$E = \sqrt{E_x^2 + E_y^2} \Rightarrow E = 5,94 \cdot 10^8 \text{ N/m} \quad \theta = \tan^{-1}\left(\frac{E_y}{E_x}\right) \Rightarrow \theta = 64,5^\circ$$

5) A thin hoop has a total of 1mC distributed evenly over its circumference. Its radius is 0.5m. A tiny charged pellet is placed along the axis of the hoop 5m from the plane of the hoop. What force is felt by the pellet? [10 pts]

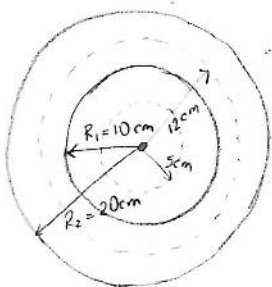
$$F = \frac{k \times Q}{(a^2 + x^2)^{3/2}} = \frac{(9 \cdot 10^9) \cdot (5 \cdot 10^{-3})}{(0,5^2 + 5^2)^{3/2}} = 3,55 \cdot 10^{-5}$$

$$F = q_{\text{pellet}} \cdot E$$

$$F = 3,55 \cdot 10^{-5} q_{\text{pellet}} \text{ N/C}$$

6) A thick shell has 6mC uniformly distributed thru its volume. Its inner radius is 10cm and its outer radius is 20cm. (Note: There is no charge inside the inner radius.) What is the E field for radius = 5cm? Please document the Gaussian surface you used. What is the E field for radius of 12 cm? [10 pts]

$$q_{\text{in}} = \rho \cdot V_{\text{in}} = \frac{Q}{\frac{4\pi}{3}(R_{\text{out}}^3 - R_{\text{in}}^3)} \cdot \frac{4\pi}{3}(r^3 - R_{\text{in}}^3) = Q \cdot \left(\frac{r^3 - R_{\text{in}}^3}{R_{\text{out}}^3 - R_{\text{in}}^3}\right) = 6,24 \cdot 10^{-4}$$



$$\int \vec{E} \cdot d\vec{a} = \frac{q_{\text{in}}}{\epsilon_0}$$

$$r = 5 \text{ cm} \Rightarrow q_{\text{in}} = 0 \Rightarrow E = 0$$

$$r = 12 \text{ cm} \Rightarrow E \cdot 4\pi r^2 = \frac{q_{\text{in}}}{\epsilon_0} \Rightarrow E = \frac{q_{\text{in}}}{4\pi \epsilon_0 r^2}$$

$$E = \frac{(9 \cdot 10^9) \cdot (6,24 \cdot 10^{-4})}{(0,12)^2}$$

$$E = 3,9 \cdot 10^8 \text{ N/C}$$