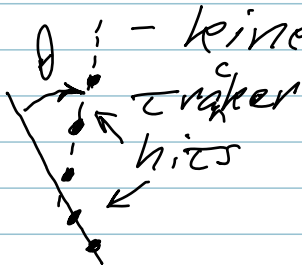


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Calorimetry

Some experimental challenges:

- not all particles are observed in a tracker
- neutrals: γ, n, π^0, ν
- new? WIMPs



- kinematic measurement

- angular deflection of track in B-field
 $\propto \frac{1}{p_T}$

- as p_T increases $\rightarrow \theta$ decreases

- position errors \rightarrow hard to measure high momenta

How address these limitations?

\rightarrow Calorimetry

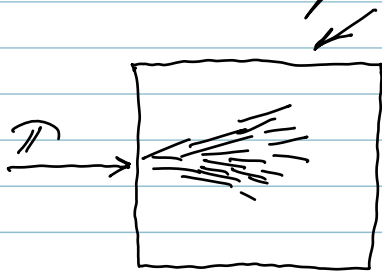
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Use Energy Loss

Sometimes need to stop particles → i.e. absorb all their energy

A calorimeter puts enough material

- in path of particle
- stops them



- many χ for e^\pm, γ
- many π for hadrons

- But need also an observable indicating energy lost

Enormous dynamic range in E in natural phenomena

- $m eV$ (dark matter)
- $> TeV$ (colliders, cosmic rays)

- may need special or specific technology for appropriate regime

Types of Calorimetry

Two most common cases for moderate to high energy:

Electromagnetic calorimeter:

- particles interacting purely electromagnetically (e^\pm, γ)

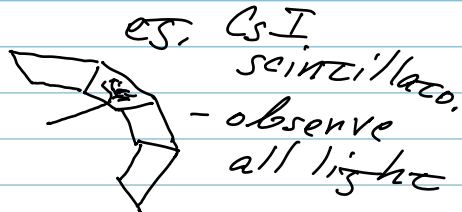
Hadronic calorimeter:

- particles interacting hadronically + electromagnetically
 p, n, π^\pm, \dots

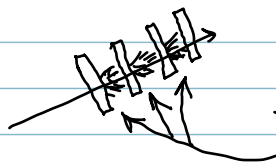
May need enough coverage to infer weakly interacting particles

Kinds of calorimeter

- Homogeneous



- sampling



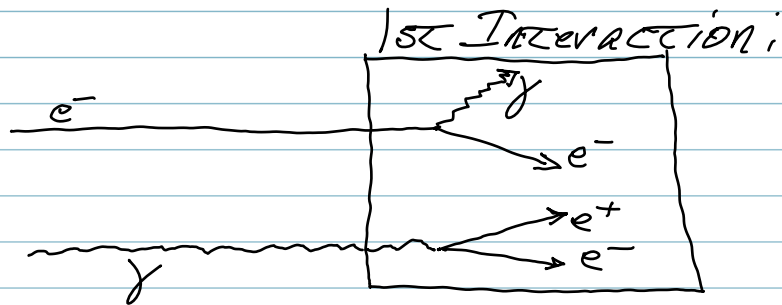
es. LAr ionization

- readout charge in gaps

①37 Electromagnetic Showers

Initial stage

- depends on incident specie

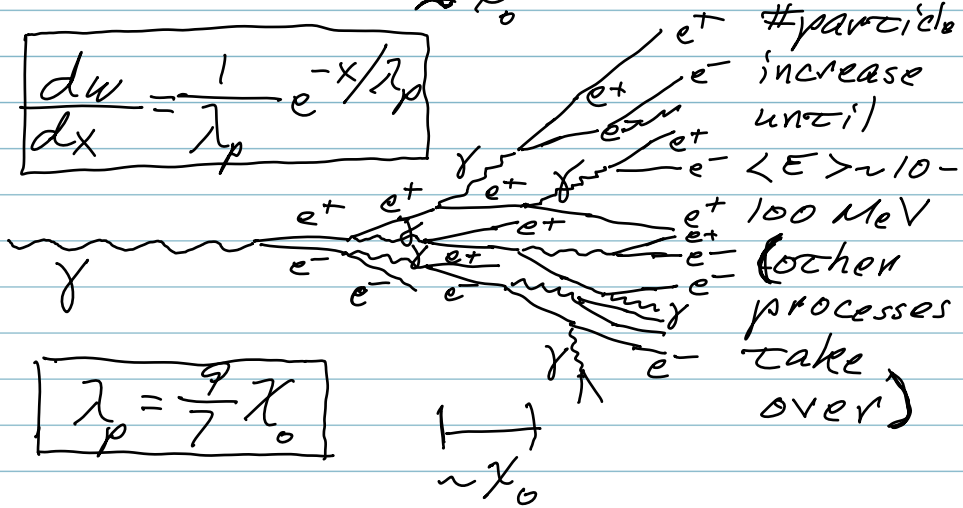
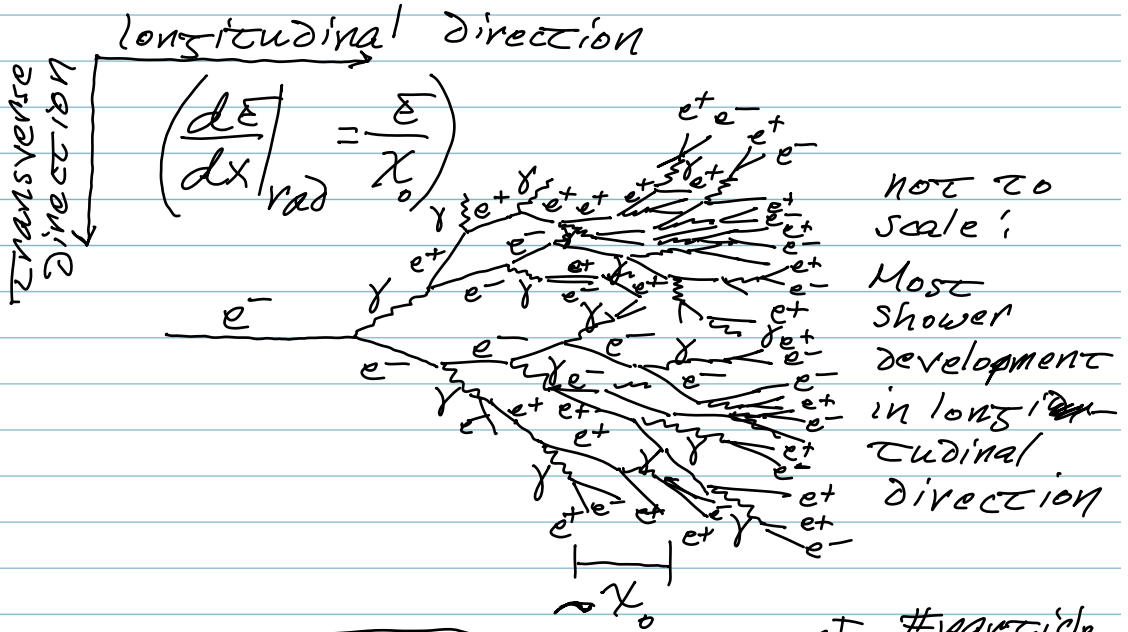


- an e^\pm traversing some material
 - if $E_e > 10-100 \text{ MeV}$
 - Bremsstrahlung

- a γ traversing material
 - if $E_\gamma > 10-100 \text{ MeV}$

Pair Production

Longitudinal Shower Development



(139) A Simple Model

- Heitler model

- when $\epsilon > \epsilon_{crit} \sim 100 \text{ MeV}$

$$\left\{ \begin{array}{l} - e^\pm \text{ travels } 1 \lambda_0 + \text{brems} \\ \rightarrow \epsilon_\gamma = \frac{1}{2} \epsilon_e, \epsilon_{new} = \frac{1}{2} \epsilon_e \\ - \gamma \text{ travels } 1 \lambda_0 + \text{pair} \\ \text{produces} \\ \rightarrow \epsilon_{e^+} = \epsilon_{e^-} = \frac{1}{2} \epsilon_\gamma \end{array} \right.$$

- assume high energy e^\pm
have no collisional losses

- when $\epsilon_e < \epsilon_{crit}$
 $\rightarrow e^\pm$ stop radiating
 \rightarrow lose energy
collisionally

Examples:

e^- shower after $1 \lambda_0$:
 $\rightarrow 1 \gamma + 1 e^-$; $\epsilon_\gamma = \epsilon_{new} = \frac{1}{2} \epsilon_0$

@ $2 \lambda_0$:
 $\rightarrow 2 e^-, 1 e^-, 1 \gamma$
 \rightarrow all have $\frac{1}{4} \epsilon_0$

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Implications:

particles after ' τ ' radiation length

$$N(\tau) = 2^\tau = e^{\tau \ln 2}$$

Average particle energy @ depth ' τ '

$$\langle E(\tau) \rangle = E_0 / 2^\tau$$

Rearranging, we get

- depth where shower $E(\tau) = E'$

$$\ln(2^\tau) = \ln(E_0/E')$$

$$\tau(\ln 2) = \ln E_0/E'$$

$$\tau(E') = \ln(E_0/E') / \ln 2$$

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Shower Maximum

Shower grows but $\langle E_i \rangle$ decreases

- at some point
→ $\langle E_i \rangle$ for e^{\pm} goes below

E_{crit}
- ionization dominates

- for e^{\pm}

- for γ 's

- photoelectric + Compton
dominate

- production of new
particles slows + stops

When $E(\tau) = E_{crit}$

⇒ "shower maximum" = highest
particles in shower

$$\tau_{max} = \frac{\ln(E_0/E_{crit})}{\ln 2} \propto \ln(E_0)$$

in GeV

depth of shower max.
(in units of λ_0)

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Particle Multiplicity

Number of particles at maximum:

$$\underline{N_{max.}} = e^{\tau_{max} \ln 2} = e^{\ln(E_0/E_{crit})}$$

$$= \boxed{E_0/E_{crit}}$$

$$\propto E_0$$

∴ # of particles a linear function of energy

→ very important for calibration purposes

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Example:

A CsI crystal calorimeter has 1 GeV incident γ . The critical energy is 18 MeV.

What is depth of shower max?

$$\begin{aligned} \tau_{\max} &= \ln(1000/10) / \ln 2 \\ &= 4.6 / 0.7 \\ &= \underline{\underline{6.6 X_0}} \end{aligned}$$

How many particles at shower max?

$$\underline{N} = E_0 / E_{\text{crit}} = \underline{\underline{100}}$$

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Example (cont.)

If we want to know the number of particles with $E > E'$, where $E' \ll E_0$

$$\begin{aligned} \underline{\underline{N(E > E')}} &= \int_0^{\tau(E')} N(\tau) d\tau \\ &= \int_0^{\tau(E')} e^{\tau \ln 2} d\tau \\ &= \int_0^{\tau(E')} e^{\ln(E_0/E')} d\tau \end{aligned}$$

$$= \frac{1}{\ln 2} \frac{E_0}{E'}$$

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Photons and Shower Containment

For γ 's around (just below)
critical energy, 1-10 MeV

- low cross section
- interaction length
~3x longer than
@ higher energy

Absorbing low E γ 's

- requires a lot of extra
material

95% absorption \Rightarrow $\oplus 70\% \chi_0$
(add this to # χ_0 's
need to get shower
max)

$$\underline{\tau_{\text{total}} \sim 15 \chi_0}$$

Important: must know of calorimeter

- is shower fully contained?
- to what extent is
shower not contained

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Energy Loss of Shower Particles

When particle i (e^\pm) goes below E_{crit}

- primary energy loss by collisions
- yields ionization

Interestingly,

$$\frac{dE}{dx} \Big|_{\text{ioniz.}} \text{ nearly constant w.r.t. } E_i \text{ - for relativistic } e^\pm$$

Also,

$$\underline{N \propto E_0}$$

which means the total ionization observed

$$\sum_i \frac{dE}{dx} \propto N \propto E_0$$

\therefore total losses observed - linearly depend on E_0

Note: a scintillation detector complicates this

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A Couple Caveats

Position of shower max.

- increases slowly with E_0
- but not linearly

- a more careful simulation

$$\tau_{\max} = \ln\left(\frac{E_0}{E_{\text{crit}}}\right) + C_{\gamma e}$$

where

$C_{\gamma e} = +0.5$ for incident γ

$C_{\gamma e} = -0.5$ " " e^{\pm}

Particle multiplicity

- particles don't reach E_{crit} simultaneously

$$\therefore \underline{N_{\max} < 2^{\tau_{\max}}}$$

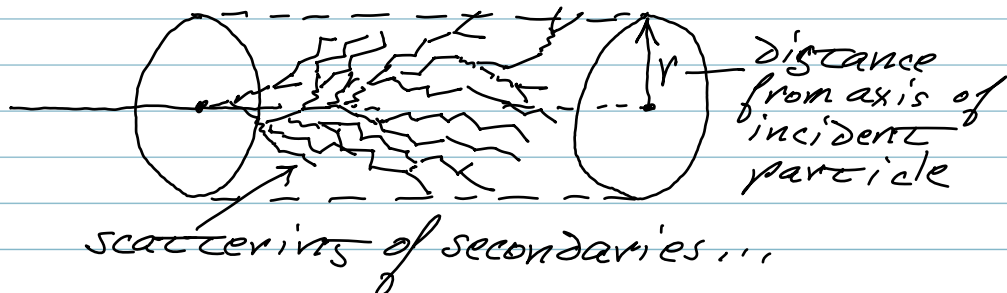
Transverse Profile of EM Showers

Bremsstrahlung γ 's

- confined to very narrow angles
 $\theta (\sim m_e c^2 / E_\gamma)$ around e^-

- do NOT contribute to lateral spreading of the shower

Multiple scattering - main effect



Molière radius:

$$R_M = \frac{21 \text{ MeV } X_0}{E_{\text{crit}}} \left\{ \frac{\text{cm}^2}{\text{g}} \right\}$$

- note: X_0 means $R_M \propto \frac{1}{Z}$

95% of particles when

$$\underline{r = 2 R_M}$$

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Homogeneous Calorimeter

- want to see all of signal

- composed of

- uniform material

- permits function of absorber AND detector

"detector" is "active medium": material where signal is generated + extracted

typical example

crystal calorimeter

- heavy scintillating crystals

- can have very good energy resolution

(150)

TeV calorimeter

(for CP violation @ Fermilab)

- CsI crystals; 50cm deep (27 λ_0)
- designed for
 - γ 's up to 80 GeV
 - (es. $K_L \rightarrow \pi^0 \pi^0 \rightarrow 4\gamma$)

- resolution often quoted as $\frac{\delta E}{E}$

when $E_\gamma > 5 \text{ GeV}$

fractional
energy resolution

$$\frac{\delta E}{E} < 1\%$$

CMS Experiment

- electromagnetic calorimeter
- 80k lead-tungstate (PbWO₄) crystals
- short λ_0 (0.9 cm)
- small R_M (2.2 cm)
- fast scintillation
- radiation - hard

Problem: only 50 γ 's/MeV emitted

So what is $\frac{\delta E}{E}$?

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Energy Resolution

Lect's assume energy calibration correct on average

- several effects alter measured energy on a case-by-case basis

- statistical fluctuations in active media

- energy leakage

- "punchthrough"

- noise in active medium

- e.g. radioactivity

- gain variations

- e.g. scintillation or photomultiplier tube gain

- electronic noise

- events overlapping in time window

- "pileup"

General Description

$$\frac{\sigma_E}{E} = \frac{S}{\sqrt{E}} \oplus \frac{N}{E} \oplus C$$

means sum in quadrature ($a \oplus b = \sqrt{a^2 + b^2}$)

CMS

↓ N ("noise term"):

- fluctuation from electronic noise or pileup
- same size (in GeV) regardless of incident particle E
- ∴ important at low E

$N_{CMS} = 155 \text{ MeV}$

S ("sampling term"):

- statistical fluctuations in shower particle statistics
- scintillation γ 's or ionization e.
- often dominant over whole E range

$S_{CMS} = 2.7\%$

C ("constant term"):

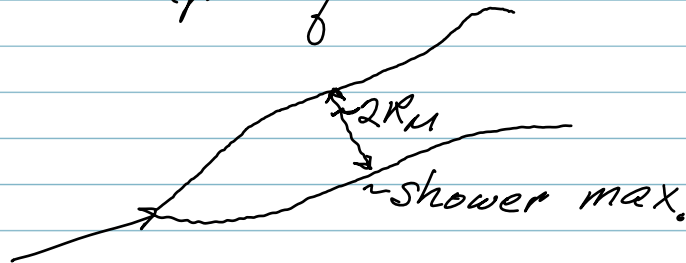
- calibration uncertainty due to detector nonuniformity
- calibration errors
- limiting factor @ highest energies

$C_{CMS} = 0.55\%$

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Position Resolution

Lateral shape of shower



- independent of energy

- Since width of shower
~ Molière radius, R_M

- position resolution a
STATISTICAL MATTER

- ie. error on mean
position of shower

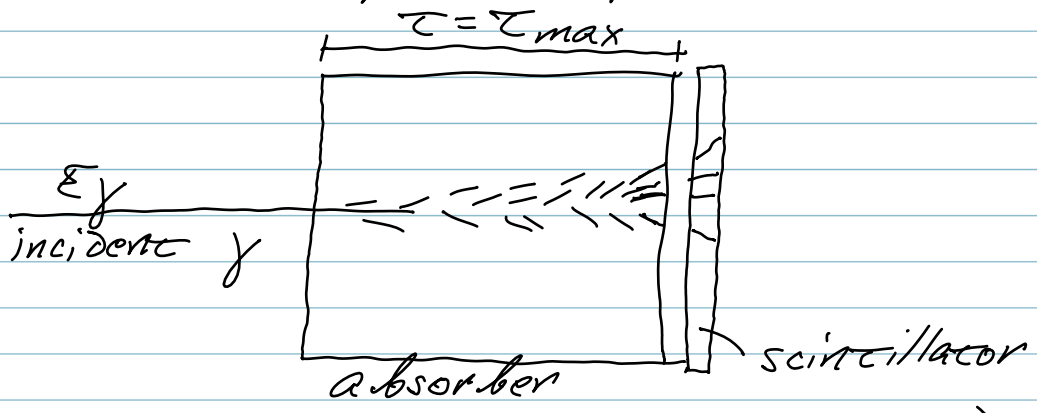
$$\sigma_{\text{pos.}} = \frac{R_M}{\sqrt{N_{\text{shower}}}}$$

consider to be N_{max}

$$\sigma_{\text{pos.}} = \frac{R_M}{\sqrt{E_0/E_c}}$$

Sampling Calorimeter

Consider simple setup:



The # of particles = E_γ / E_{crit}
 $\therefore N_e = \frac{2}{3} N_{max} = \frac{2}{3} \frac{E_\gamma}{E_{crit}}$

Fractional fluctuations on N_e
 $\frac{\delta(N_e)}{N_e} = \frac{1}{\sqrt{N_e}}$

Since $N_e \propto E_\gamma$, we have

$$\frac{\delta E}{E} \approx \frac{1}{\sqrt{N_e}} \approx \frac{1}{\sqrt{2E_\gamma/3E_{crit}}}$$

"Sampling term" \rightarrow tends to be more dominant than homogeneous calorimeter \rightarrow

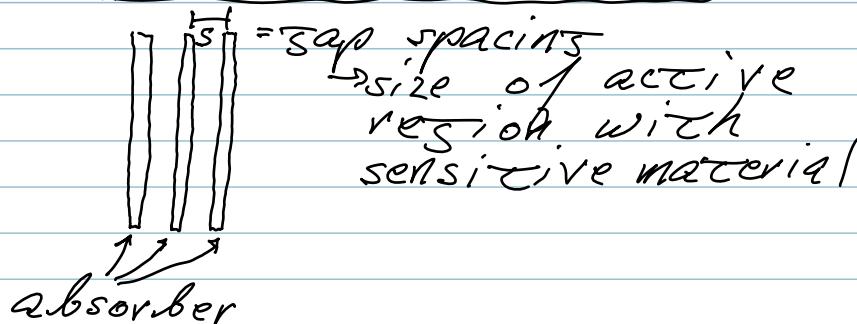
Resolution improves with energy \rightarrow increases linearly \rightarrow tracker

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Sampling Fluctuations

A general form in a sampling calorimeter

$$\frac{\sigma_s}{E} = \frac{2.7\%}{\sqrt{E[\text{GeV}]}} \sqrt{\frac{s[\text{mm}]}{f_{\text{samp}}}}$$



sampling fraction, f_{samp}

- ratio of energy loss

$\left(\frac{dE}{dx}\right)_{\text{MIP}}$ in active medium

- vs. - energy loss (MIP) in absorber + active

Example: $\Delta\phi$ EM calorimeter

$s = 2\text{mm}$ $\langle f_{\text{samp}} \rangle \sim 10\%$

$$\therefore \frac{\sigma_s}{E} = \frac{2.7\%}{\sqrt{E}} (s) \sim \frac{14\%}{\sqrt{E}}$$

→ actual value → $15\%/\sqrt{E}$

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Choice of Materials

Absorber: Generally dense material
- moderate R_M

Active Medium: material providing observable correlated with particle energy
→ ionization
→ scintillation

→ liquid argon (LAr) +
scintillators

- ~~not~~ better resolution than gaseous media

- gases give larger Landau fluctuations

Scintillators

- might use alternating layers of absorber + plastic scintillator
- light sensitive device has large gain

- charged particles in shower produce light in active medium.

- fast signals, large amplitude
if "read out" with PMTs

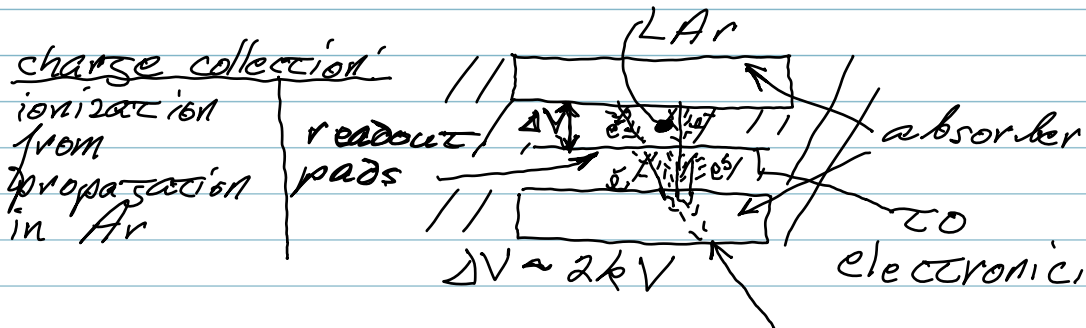
o - problem if a magnetic field
- move them outside

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Examples: ATLAS (Fe/LAr)
 $D \approx 200 \mu\text{m/LAr}$

Liquid Noble Gases

- Ar, Kr, Xe: Ar is common in liquid form
- ionization detector



- readout → metal pads
- absorber → metal plates immersed in LAr

No gain: # e^- directly read out
∴ very linear for e^\pm, γ

- small amount of charge
- cryogenically cool (80 K) for low noise
- need preamplifier and electronics

Purity: important as impurities in Ar allow e^\pm recombination

- loss of signal
- energy dependent

Hadronic Calorimeter

Same basic idea as EM Calorimeter

- STOP particle (absorb all its energy)
- measure parameters correlated with this energy
 - IONIZATION
 - SCINTILLATION
- calorimeter generally sampling
 - same technology as before

Most particles besides e^+ or γ

- do not directly create EM showers
- hadrons
 - more massive than e^+
 - charged ones generally lose little energy to ionization
- interact via nuclear interactions
 - if reach detector
 - initiates a shower

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Hadronic Showers

Initial hadron interactions with matter

- some ionization
- produce secondary hadrons

- charged pions
 - produce ionization
 - tertiary particles

- π^0
 - lifetime, $\tau \sim 10^{-16}$ s
 - decay $\rightarrow \gamma\gamma$
 - EM shower in hadron shower
 - about 1/3 of secondaries

- some K, ρ , n
- nuclear breakup fragments
 - binding energy + excitation
 - ν production
- μ^{\pm} from in-flight decays

- particle multiplicity $\propto \ln(E)$
- typical $p_T \sim 0.35$ GeV/c

Very difficult to model well

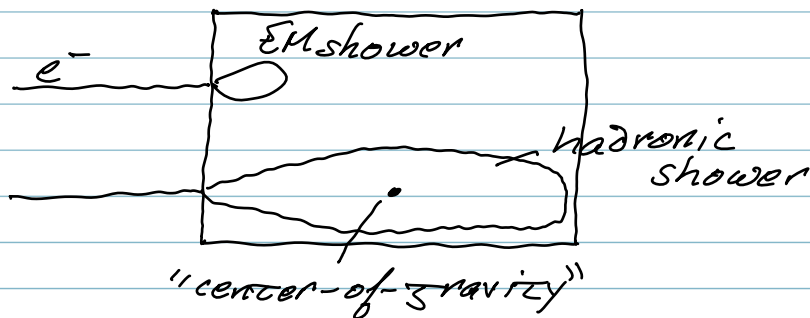
Longitudinal Shower Development (160)

Set by nuclear absorption length

$$\lambda_0 = A / (N_A \sigma_{abs}) \propto A^{1/3}$$

absorption
cross section

As we've seen, this is $\gg \lambda_0$ for high Z materials



Distance with which 95% of energy contained

$$L(95\%) \sim \frac{\lambda_0^x}{\lambda_{Fe}} \left(9.4 \ln\left(\frac{E}{\text{GeV}}\right) + 3.9 \right) \{ \text{cm} \}$$

- where "x" is some material (eg. Pb) and "Fe" is iron

Require a larger detector (than EM) for full containment

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Lateral Shower Development

- EM shower width: due mainly to multiple scattering

Nuclear processes

- large momentum transfer in collisions

$\therefore p_{\perp}$ can be large: large angle of secondary relative to primary



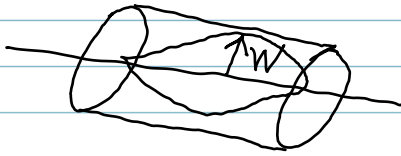
- nuclear or particle decay
- produce very wide showers

~~Width of a shower~~

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Width of a Shower

Diameter of a cylinder (in cm)
contains 99% of energy



$$W(\epsilon) = -17.3 + 14.3 \ln(\epsilon)$$

↓ in GeV

Very strong fluctuations
in hadronic showers

- produces wide variations
in hadronic showers
structure

- much more than
EM showers

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Electromagnetic Content of Hadronic Showers

$\frac{1}{3}$ of secondaries are π^0 for each interaction

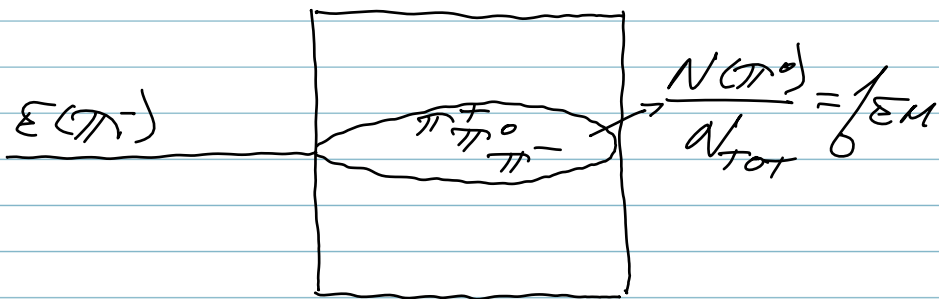
- Since $\pi^0 \rightarrow 2\gamma$: $\frac{1}{3}$ of shower goes to EM sub-shower

- next nuclear interaction
 $\frac{1}{3} \pi^0 \rightarrow$ EM showers

- et cetera, ...

Naively, EM fraction of a shower should rise vs. Energy

$$f_{EM} \sim 1 - \left(\frac{2}{3}\right)^n \quad \text{--- \# of shower generations}$$



Non-Electromagnetic Components

→ some secondaries can be "invisible"

- nuclear fragments
 - short lived
 - absorbed before can be detected
- long-lived neutrals
 - n, K_L, ν
 - escapes detector leaving little or no energy
- muons
 - created in decay of hadrons
 - only small ionization losses
 - can contribute up to 40% of hadronic shower

Result:

- hadron energies usually undermeasured relative to γ

$$\frac{h\nu}{h} > 1 \quad (+ \text{it's Energy dependent})$$

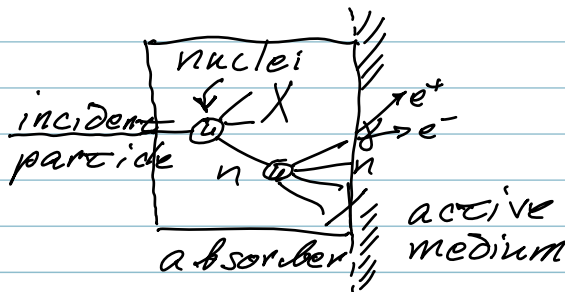
- makes hadronic calibration much more difficult

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Compensation

Possible to recover, or "compensate" for lost signal in hadronic showers

- consider fissile material, U
- neutrons produced in nuclear interactions



1) caught by other nuclei

2) fission + emission of more n 's + γ 's

3) conversion of γ 's $\rightarrow e^+e^-$ yields a signal

Need to be above a few GeV
- for good compensation
improves with energy

Example: $\Delta\phi$ U/LAN calorimeter

$$e/\pi \sim 1.05$$

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Energy Resolution

Use same general expression as for EM calorimetry

$$\boxed{\frac{\delta}{E} = \frac{N}{E^2} \oplus \frac{S}{E} \oplus C}$$

⊕ = addition
in quadrature

Now we have large variations in hadronic shower evolution

- composition of ^{each} shower (ie. # π^0 , f_{EM})
- dominates statistical term, S , of resolution

Best hadron sampling calorimeters

- less performant than EM calorimeter
- two examples, dP (U absorber, compensation)

$$\boxed{\frac{\delta(E)}{E} = \frac{35\%}{\sqrt{E[\text{GeV}]}}$$

- ATLAS (Fe absorber + Scintillator, $\eta \sim 1.37$)

$$\frac{\delta(E)}{E} = \frac{42\%}{\sqrt{E[\text{GeV}]}}$$

Still, for 50 GeV π^-

$$\frac{\delta}{E} \sim \frac{0.35}{\sqrt{E}} = 0.05 \quad \text{so 5\% precision possible}$$