

A nighttime photograph of a city skyline, likely Pittsburgh, with numerous skyscrapers illuminated. In the foreground, a fountain sprays water into the air, and its reflection is visible in the water below. The sky is a deep blue, and the city lights create a vibrant, colorful reflection on the water's surface.

# CT2015: Topics in Higgs Physics

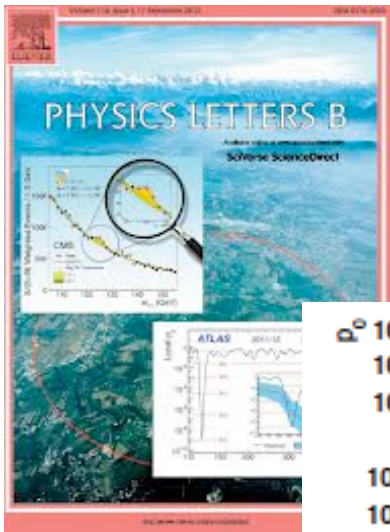
**S. Dawson**

**July, 2015**

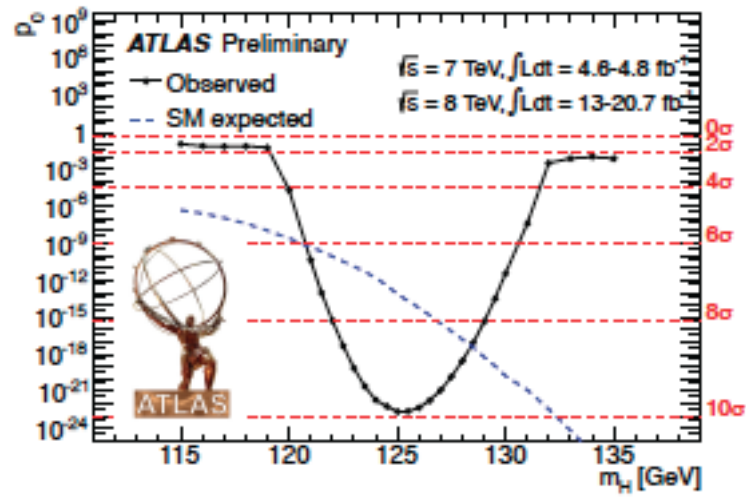
- 1.) Measuring the Higgs Width and Unitarity
- 2.) Fitting Higgs Couplings beyond the  $\kappa$  approach

# We discovered a Higgs boson!

- The Standard Model is very predictive (*testable!*)
- Only free parameter is  $M_H$



Both ATLAS and CMS have close to  $10\sigma$  significance

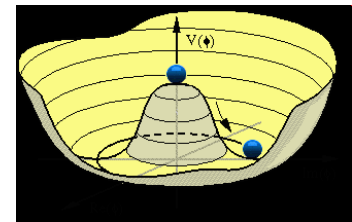


Probability of  $10\sigma$  event being random is  $10^{-23}$

# SM is Very Simple

- Standard Model includes complex Higgs SU(2) doublet

$$\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_1 + i\phi_2 \\ \phi_3 + i\phi_4 \end{pmatrix} = \begin{pmatrix} \varphi^+ \\ \varphi^0 \end{pmatrix}$$



- With SU(2) x U(1) invariant scalar potential

$$V = \mu^2 \Phi^\dagger \Phi + \lambda (\Phi^\dagger \Phi)^2 \quad \text{Invariant under } \Phi \rightarrow -\Phi$$

- If  $\mu^2 < 0$ , then spontaneous symmetry breaking
- Minimum of potential at:

$$\langle \Phi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix} \quad \Phi = e^{\frac{i\omega \cdot \sigma}{v}} \begin{pmatrix} 0 \\ \frac{H+v}{\sqrt{2}} \end{pmatrix}$$

– Choice of minimum breaks gauge symmetry

## More on SM Higgs Mechanism

- Couple  $\Phi$  to **SU(2) x U(1)** gauge bosons ( $W_i^\mu$ ,  $i=1,2,3$ ;  $B^\mu$ )

$$L_S = (D_\mu \Phi)^\dagger (D^\mu \Phi) - V(\Phi)$$

$$D_\mu = \partial_\mu - i \frac{g}{2} \sigma^i W_\mu^i - i \frac{g'}{2} B_\mu$$

Couplings fixed by  
gauge invariance

- Gauge boson mass terms from:

$$\begin{aligned} (D_\mu \Phi)^\dagger D^\mu \Phi &\rightarrow \dots + \frac{1}{8} (0, v) (g W_\mu^a \sigma^a + g' B_\mu) (g W^{b\mu} \sigma^b + g' B^\mu) \begin{pmatrix} 0 \\ v \end{pmatrix} + \dots \\ &\rightarrow \dots + \frac{v^2}{8} \left( g^2 (W_\mu^1)^2 + g^2 (W_\mu^2)^2 + (-g W_\mu^3 + g' B_\mu)^2 \right) + \dots \end{aligned}$$

*Generated masses (ie longitudinal component) for W and Z*

# Recap of SM Higgs Mechanism

- Generate mass for W,Z using Higgs mechanism
  - Higgs VEV breaks  $SU(2) \times U(1)$
  - Single Higgs doublet is minimal case (singlet doesn't work)
- Before spontaneous symmetry breaking:
  - Massless  $W_i, B, \text{Complex } \Phi$
  - *(Massless gauge bosons have only transverse polarizations)*
- After spontaneous symmetry breaking:
  - Massive  $W^\pm, Z$ ; massless  $\gamma$ ; physical Higgs boson H

*Spontaneous symmetry breaking generates longitudinal components of gauge bosons*

\* Count degrees of freedom

# Higgs Parameters

- $G_F$  measured precisely

$$\frac{G_F}{\sqrt{2}} = \frac{g^2}{8M_W^2} = \frac{1}{2v^2} \quad v^2 = (\sqrt{2}G_F)^{-1} = (246\text{GeV})^2$$

- Higgs potential has 2 free parameters,  $\mu^2, \lambda$

$$V = \mu^2 \Phi^\dagger \Phi + \lambda (\Phi^\dagger \Phi)^2$$

- Trade  $\mu^2, \lambda$  for  $v^2, M_H^2$

$$V = \frac{M_H^2}{2} H^2 + \frac{M_H^2}{2v} H^3 + \frac{M_H^2}{8v^2} H^4$$

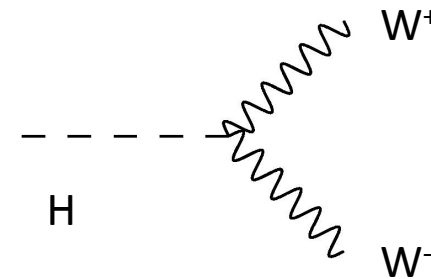
$$v^2 = -\frac{\mu^2}{2\lambda}$$
$$M_H^2 = 2v^2 \lambda$$

- Large  $M_H \rightarrow$  strong Higgs self-coupling
- A priori, Higgs mass can be anything

## Example: $H \rightarrow W^+W^-$

- Rest frame of H:
  - $\epsilon_{\pm}(W^+) = (0, 1, \pm i, 0)/\sqrt{2}$
  - $\epsilon_{\pm}(W^-) = (0, 1, i, 0)/\sqrt{2}$
  - $\epsilon_L(W^+) = (M_H/2M_W)(\beta, 0, 0, 1)$
  - $\epsilon_L(W^-) = (M_H/2M_W)(\beta, 0, 0, -1)$

The action is in the longitudinal sector!



$$A(H \rightarrow W^+W^-) = -gM_W \epsilon(W^+) \cdot \epsilon(W^-)$$

$$A(H \rightarrow W_L^+W_L^-) = g \frac{M_H^2}{4M_W}$$

$$A(H \rightarrow W_T^+W_T^-) = gM_W$$

Longitudinal interactions of gauge bosons with Higgs are enhanced at large  $p^2 = M_H^2$

$$\beta^2 = 1 - 4M_W^2/M_H^2$$

## What about fermion masses?

- Fermion mass term:

$$L = m\bar{\Psi}\Psi = m(\bar{\Psi}_L\Psi_R + \bar{\Psi}_R\Psi_L)$$



Forbidden by  
SU(2)xU(1) gauge  
invariance

- Left-handed fermions are SU(2) doublets  $Q_L = \begin{pmatrix} u \\ d \end{pmatrix}_L$
- Scalar couplings to fermions:  $L_d = -\lambda_d\bar{Q}_L\Phi d_R + h.c.$
- Effective Higgs-fermion coupling

$$L_d = -\frac{\lambda_d}{\sqrt{2}}(\bar{u}_L, \bar{d}_L) \begin{pmatrix} 0 \\ v + H \end{pmatrix} d_R + h.c.$$



## Fermion Masses, 2

- $M_u$  from  $\Phi_c = i\sigma_2 \Phi^*$  (not allowed in SUSY)

$$\Phi_c = \begin{pmatrix} \bar{\phi}^0 \\ -\phi^- \end{pmatrix} \quad L = -\lambda_u \bar{Q}_L \Phi_c u_R + hc$$

$$\lambda_u = \frac{M_u \sqrt{2}}{v}$$

- Higgs-fermion couplings proportional to mass
- No flavor violating Higgs fermion couplings

*SUSY models always have at least 2 Higgs doublets*

\*tch,  $\mu eH$  couplings etc smoking guns for new physics

# Review of Higgs Couplings

- Very precise predictions

- Couplings to fermions proportional to mass  $\frac{M_f}{v} H \bar{f} f$
- Couplings to massive gauge bosons proportional to (mass)<sup>2</sup>

$$2M_W^2 \frac{H}{v} W_\mu^+ W^{-\mu} + M_Z^2 \frac{H}{v} Z_\mu Z^\mu$$

- Couplings to massless gauge bosons at 1-loop

$$\kappa_g \frac{\alpha_s}{12\pi} \frac{H}{v} G_{\mu\nu}^A G^{A,\mu\nu} + \kappa_\gamma \frac{\alpha}{8\pi} \frac{H}{v} F_{\mu\nu} F^{\mu\nu} + \kappa_{Z\gamma} \frac{\alpha}{8\pi s_W} \frac{H}{v} F_{\mu\nu} Z^{\mu\nu}$$

- Higgs self-couplings proportional to  $M_H^2$

$$\frac{M_H^2}{2} H^2 + \frac{M_H^2}{2v} H^3 + \frac{M_H^2}{8v^2} H^4$$

*Only unpredicted parameter is  $M_H$*

## Model Makes Predictions

- Four free parameters in gauge-Higgs sector ( $g, g', \mu, \lambda$ )
  - Conventionally chosen to be
    - $\alpha=1/137.0359895(61)$
    - $G_F = 1.16637(1) \times 10^{-5} \text{ GeV}^{-2}$
    - $M_Z=91.1875 \pm 0.0021 \text{ GeV}$
    - $M_H=125.09 \pm .21 \pm .11 \text{ GeV}$
  - Express everything else in terms of these parameters

$$\frac{G_F}{\sqrt{2}} = \frac{g^2}{8M_W^2} = \frac{\pi\alpha}{2\left(1 - \frac{M_W^2}{M_Z^2}\right)M_W^2} \quad \Rightarrow \text{Predicts } M_W$$

## The Higgs and EW Fits

$$G_F = \frac{\pi\alpha}{\sqrt{2}M_W^2 \sin^2 \theta_W} \frac{1}{(1 - \Delta r)}$$

$$\frac{M_W}{M_Z} \equiv \cos \theta_W$$

- $\Delta r$  is a physical quantity which incorporates 1-loop corrections
- Contributions to  $\Delta r$  from top quark and Higgs loops

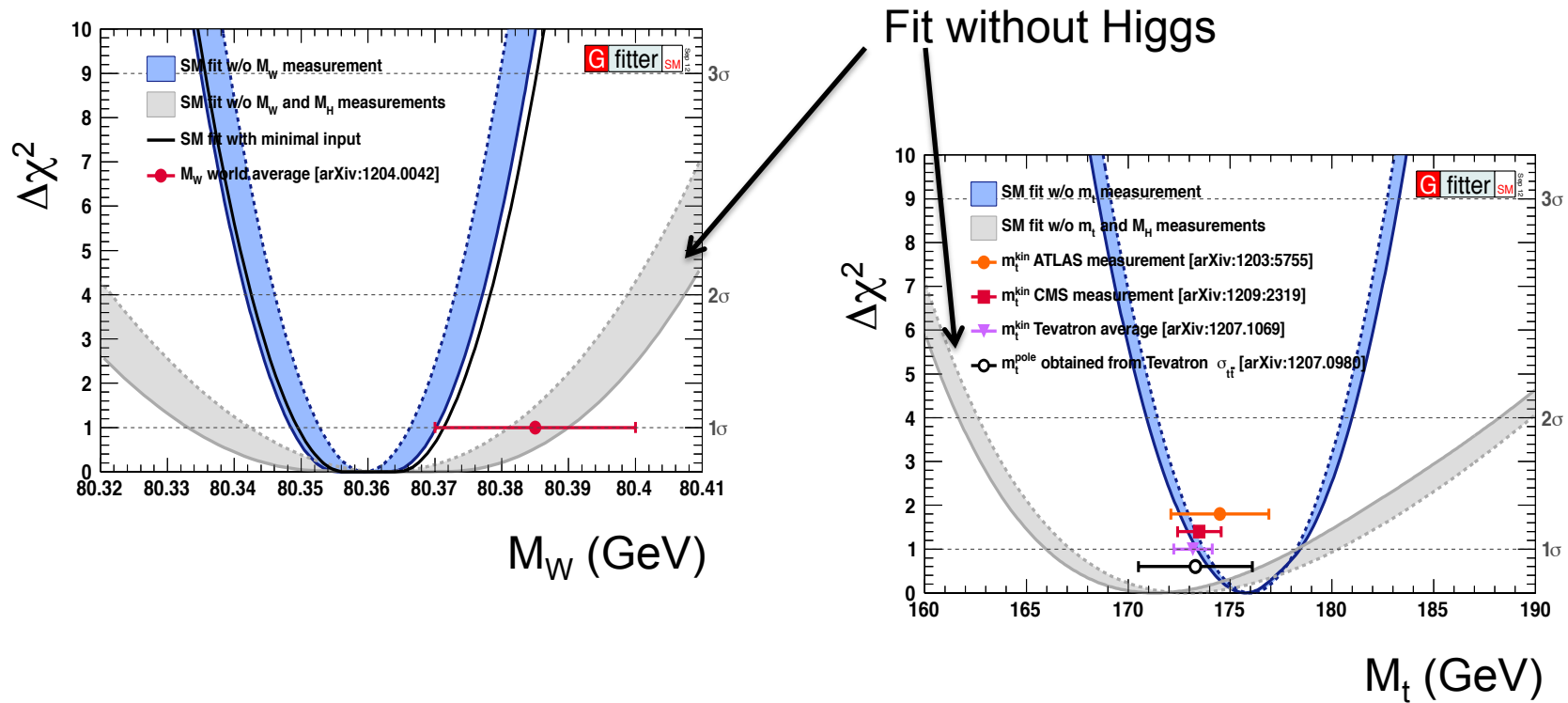
$$\Delta r^t = -\frac{3G_F M_t^2}{8\sqrt{2}\pi^2} \left( \frac{\cos^2 \theta_W}{\sin^2 \theta_W} \right)$$

Extreme sensitivity of precision measurements to  $M_t$

$$\Delta r^H = \frac{11G_F M_W^2}{24\sqrt{2}\pi^2} \left( \ln \frac{M_H^2}{M_W^2} \right)$$

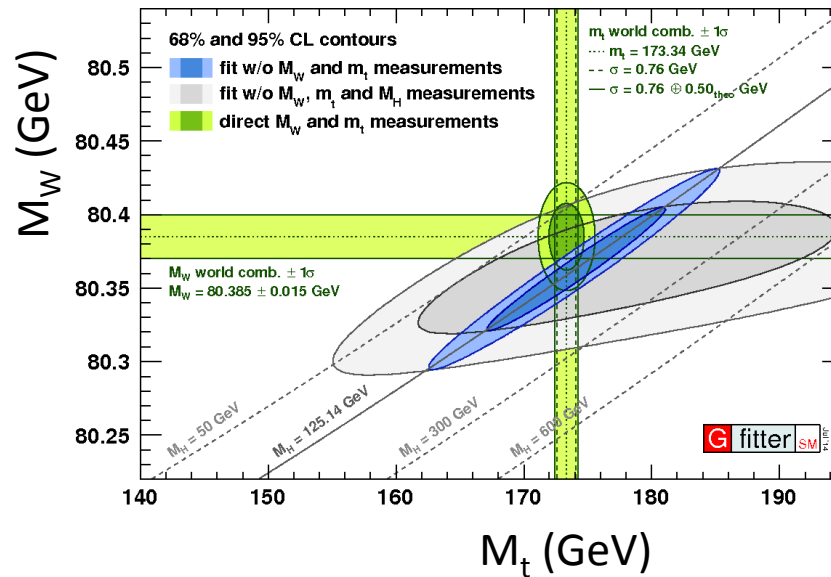
If we removed the Higgs, this formula would be infinite

# Precision Physics After Higgs Discovery



EW fits improved by addition of Higgs

# The SM Works!

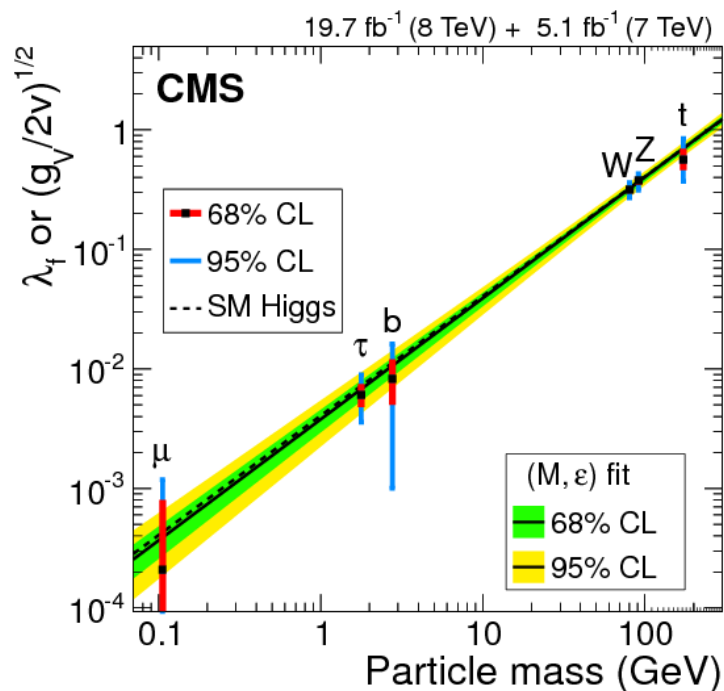


Measurements sensitive to  $\ln(M_H)$  terms

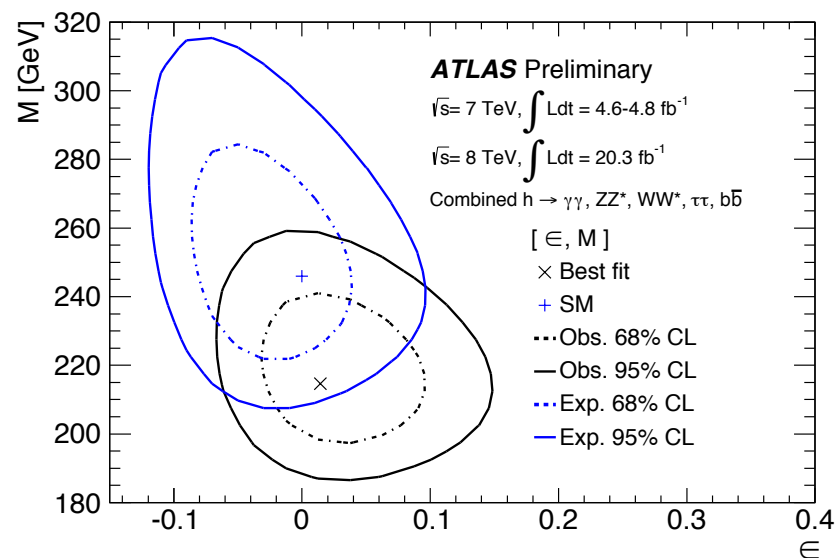
Corollary: New Physics highly restricted by data

*\*So why are we still talking about BSM physics in the Higgs sector?*

# No Unknown Parameters in SM



$$L \sim \left( \frac{m_f}{M} \right)^{1+\epsilon} H \bar{f} f + \left( \frac{M_V^{2+2\epsilon}}{M^{1+2\epsilon}} \right) H V_\mu V^\mu$$



Everything looks reasonably consistent with SM

## At the 10-30% level:

- Fermion couplings to b, t,  $\tau$  ✓
- Gauge boson couplings to W/Z/g/ $\gamma$  ✓
- Higgs  $H^2$  coupling ✓
- No information on  $HZ\gamma$ , 2<sup>nd</sup> generation fermions,  $H^3$ ,  $H^4$  couplings....
- Generically, Higgs coupling deviations in BSM:

$$\mathcal{O}\left(\frac{v^2}{M^2}\right) \sim 5\% \left(\frac{1 \text{ TeV}}{M}\right)^2$$

**Much work to do!**



## Things we need to know

- How close are Higgs couplings to SM predictions?
- Does the Higgs come from a scalar potential?
- Does the Higgs couple to things we don't see?
- What is the Higgs width? Spin? Parity? Mass?
- Are there more Higgs particles?

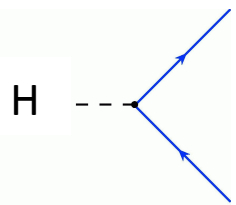
*These questions will be at the center of  
the 13 TeV Higgs physics program*

# Higgs Decays

- At tree level Higgs mostly decays to heaviest particle allowed
  - Coupling proportional to mass
  - Largest uncertainty on Higgs branching ratios comes from  $M_b$
  - BSM models often have enhanced Hbb couplings (e.g. SUSY at large  $\tan \beta$ )
- At loop level:  $H \rightarrow \gamma\gamma$  important
  - Precision discovery channel
  - Sensitive to new physics

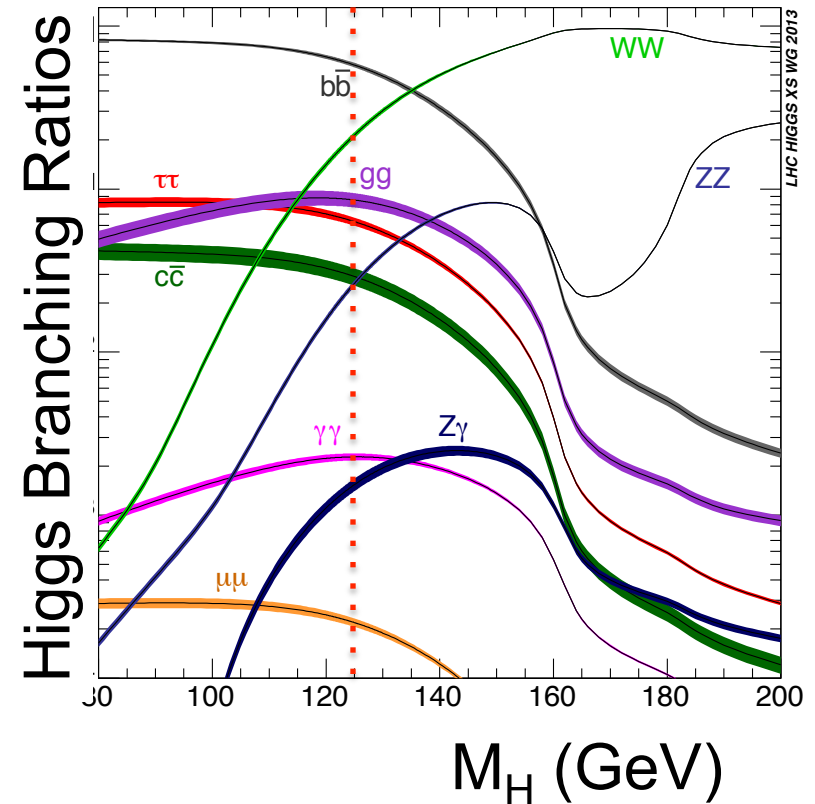
# Higgs Decays

- $H \rightarrow f\bar{f}$  proportional to  $M_f^2$



$$\frac{BR(H \rightarrow b\bar{b})}{BR(H \rightarrow \tau^+\tau^-)} \sim N_c \left( \frac{M_b^2}{M_\tau^2} \right)$$

$$\Gamma_{ff} = N_c \frac{G_F}{4\sqrt{2}\pi} M_H M_f^2 \left( 1 - \frac{4M_f^2}{M_H^2} \right)^{3/2}$$



For  $M_H < 2M_W$ , decays to  $b\bar{b}$  dominate

# Higgs Decays to Photons

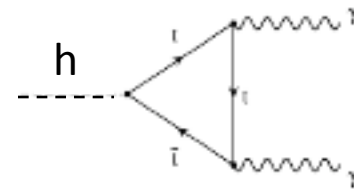
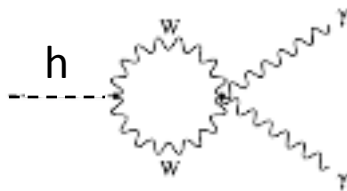
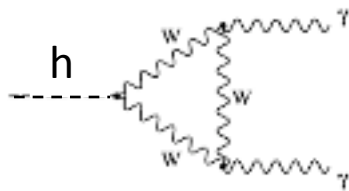
- Dominant contribution is W loops
- Contribution from top is small

*Note opposite signs of t/W loops*

$$\Gamma(H \rightarrow \gamma\gamma) \sim \frac{\alpha^3}{256\pi^2 s_W^2} \frac{M_H^3}{M_W^2} \left| 7 - \frac{16}{9} + \dots \right|^2$$

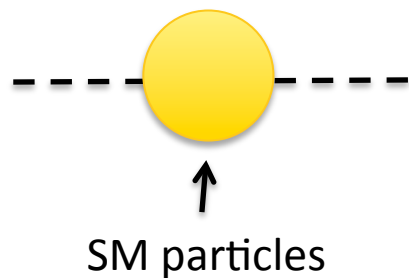
W

top



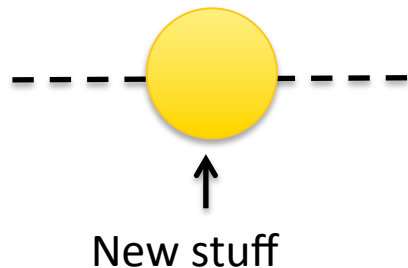
# Why do we expect BSM in Loops?

- Generically, solutions to naturalness involve new particles



$$\delta M_H^2 \sim -(125 \text{ GeV})^2 \left( \frac{\Lambda}{600 \text{ GeV}} \right)^2$$

$\Lambda$  is scale of new physics

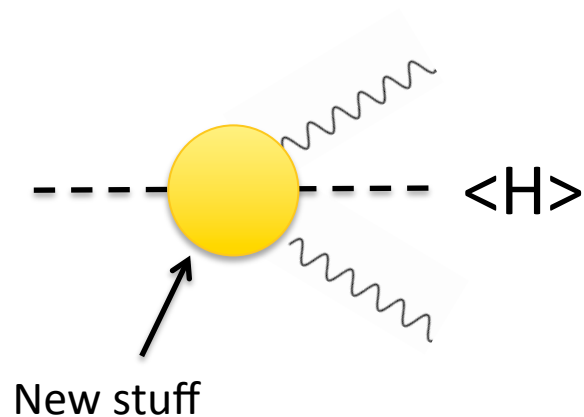


$$\delta M_H^2 \sim +(125 \text{ GeV})^2 \left( \frac{\Lambda}{M_{new}} \right)^2$$

*For this cancellation to work, new stuff can't be too much above TeV scale*

## Why care about $H \rightarrow \gamma\gamma$ ?

- New particles lead to deviations in Higgs couplings



MSSM light stops generically contribute (no mixing):

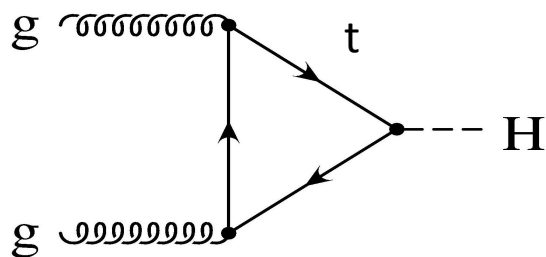
$$\kappa_g^2 = \frac{\sigma(gg \rightarrow H)}{\sigma(gg \rightarrow H)|_{SM}} \sim 1 + \left( \frac{700 \text{ GeV}}{\tilde{m}_t} \right)^2 3\%$$

Target precision < 3%

*As LHC limits on new particles increase, target precision decreases*

## How do we make a Higgs boson?

- Largest production rate is from gluon fusion
- Largest contribution in SM is from top quarks
- (Hff coupling  $\sim M_f/v$ )
- Not a direct measurement of ttH coupling since there could be new particles in loop



*For large  $M_t$*

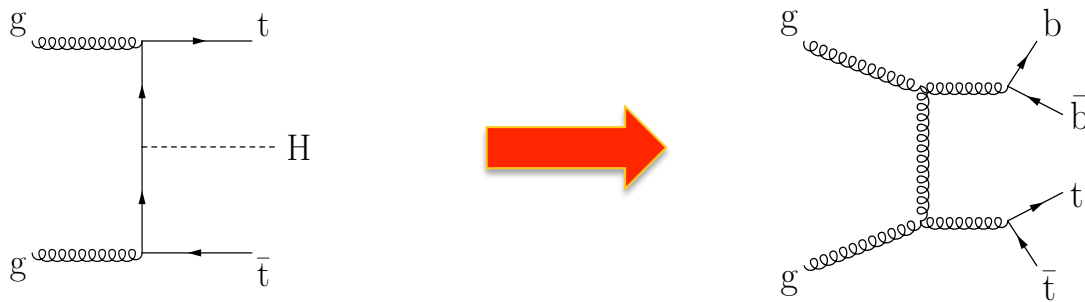
$$L \rightarrow -\frac{\alpha_s}{12\pi v} H G_{\mu\nu}^A G^{A,\mu\nu}$$

*Gluon fusion sensitive to new strongly interacting particles: Ex: squarks or heavy colored fermions*

\*Heavy chiral fermions don't decouple since coupling is proportional to mass

# ttH Production

- Can unambiguously measure ttH Yukawa coupling
- Small rates, large backgrounds



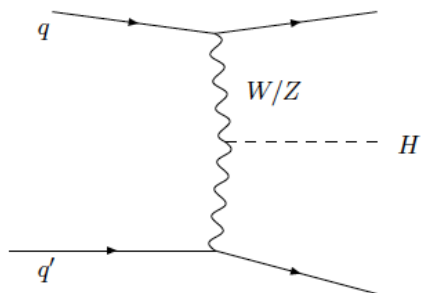
- Most of ttH cross section at LHC is from gluon initial states

\*CMS significance for observation of ttH final state in Run 1 is  $\sigma=3.5$



# Vector Boson Scattering

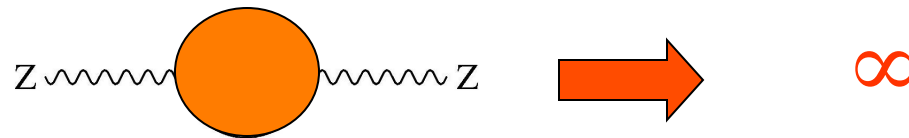
- Outgoing jets peaked in forward direction
- Large jet-jet invariant mass, large angular separation
- Cuts are effective in separating from gluon fusion background



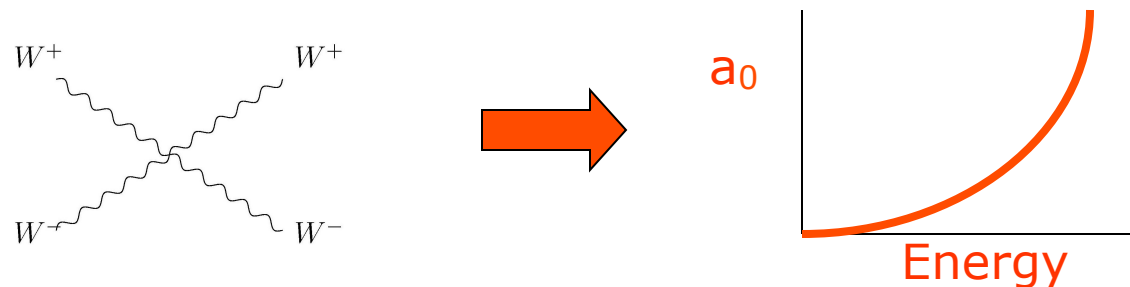
- $W^+W^- \rightarrow W^+W^-$  is a physical process!
- Without a Higgs, this process would grow with energy (**unitarity violation**)

# Higgs has special job in SM

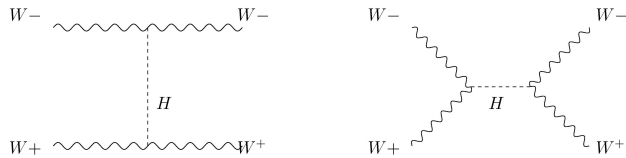
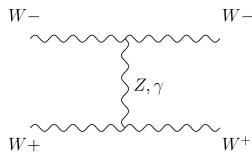
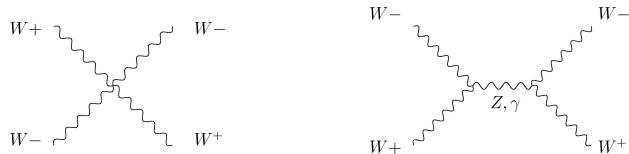
- Massive  $W$  and  $Z$ 's have longitudinal polarizations
- Longitudinal interactions spoil nice properties of gauge theories:
  - Loops are not finite without Higgs



- Scattering amplitudes grow with energy



# VV Scattering



$$A \approx g^2 \frac{E^2}{M_W^2}$$

$$A \approx -g^2 \frac{E^2}{M_W^2}$$

$E^4$  terms cancel  
between TGC and QGC

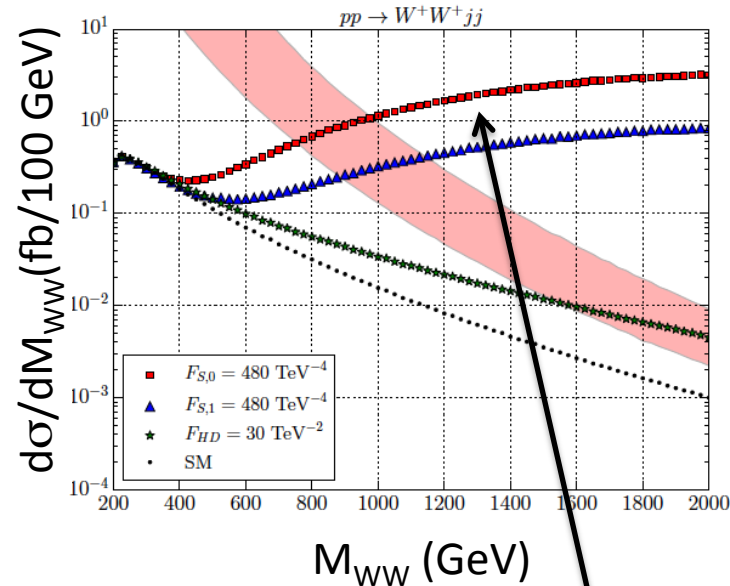
Terms which grow  
with energy cancel for  
 $E \gg M_H$

This cancellation requires  
 $M_H < 800 \text{ GeV}$

***SM particles have just the right couplings so  
amplitudes don't grow with energy***

## VBF Scattering: $W^+W^+jj$

- New physics effects grow like  $s/\Lambda^2$ , spoils cancellations
- Unitarity violation above red band (region of validity) of theory

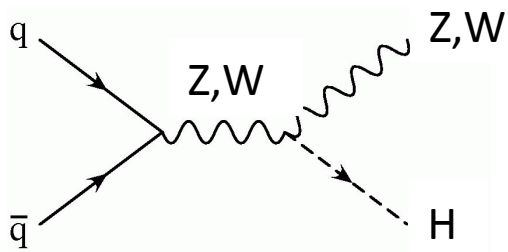


Note growth of new physics effects with  $M_{WW}$

[Kilian,Ohl,Reuter Sekulla]

# Higgstrahlung

- Small rate, clean signal
- High  $p_T$  tails sensitive to new physics



Sensitive to same couplings as VBF

# Separate initial states

Separate quark and gluon initial states



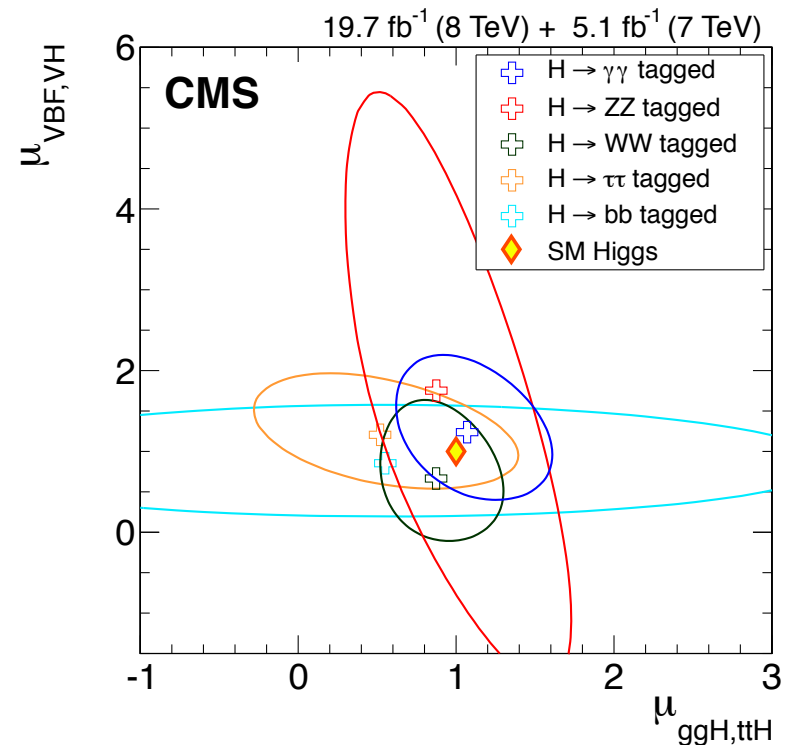
## *Simplistic cheat sheet:*

**Gluon fusion:** Laboratory for higher order QCD; sensitive to new heavy colored states

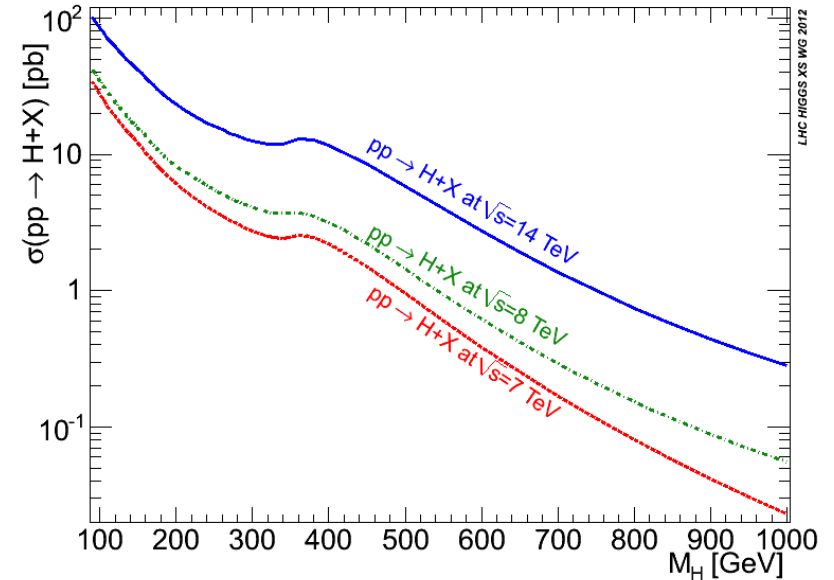
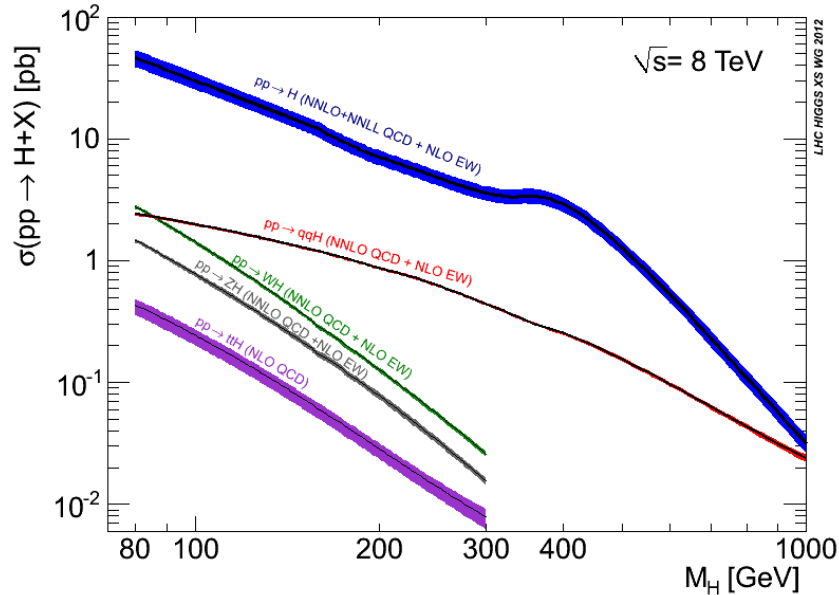
**VBF:** Probes Higgs role in unitarity cancellations (no growth with energy)

**ttH:** Direct measurement of top quark Yukawa coupling

**VH:** Sensitive to new physics in high  $p_T$  tail



# Higgs Production



Reduction of scale uncertainty at N<sup>3</sup>LO:

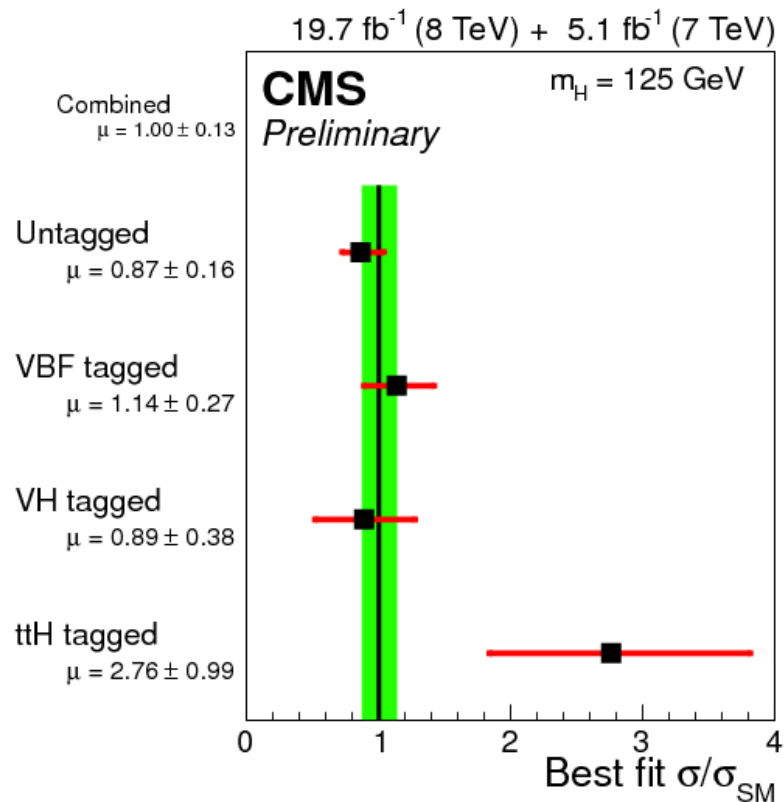
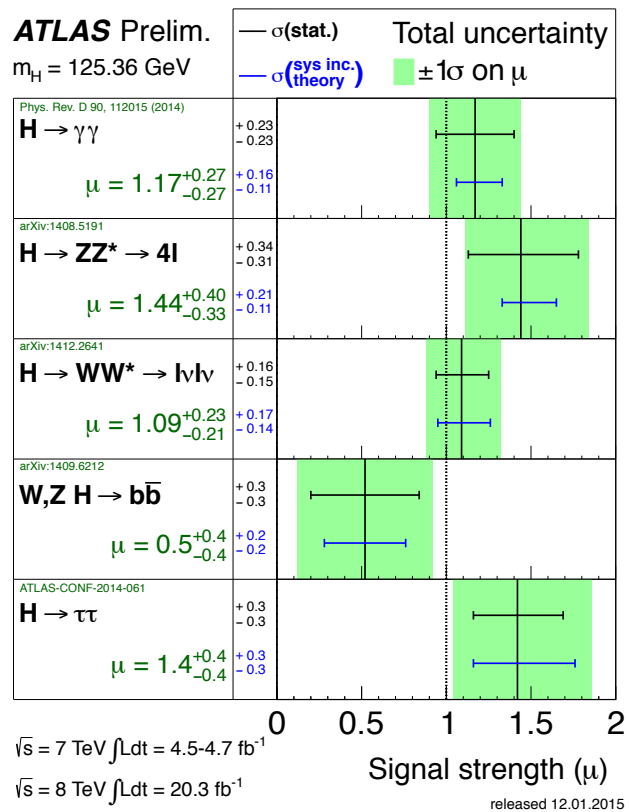
13 TeV  $\sigma(M_H=125 \text{ GeV})=43.14 \text{ pb}^{+2.71\%}_{-4.45\%}$

**3 Loops!**

Increase of +2.2% from NNLO rate

[Anastasiou, Duhr, Dulat, Herzog, Mistlberger, arXiv:1503.06056]

# Production Strengths



Always normalized to SM (*Theory matters!*)



# Higgs Production Increases at 13 TeV

	$\sigma(\text{pb})$ at 13 TeV	$\sigma(\text{pb})$ at 8 TeV
Gluon Fusion	43.9	19.27
Vector Boson Fusion	3.748	1.578
WH	1.38	.70
ZH	.87	.42
ttH	.51	.13
HH	.034	.008

Factors of 2-4 increases in rates

Note large increase  
in ttH rate!

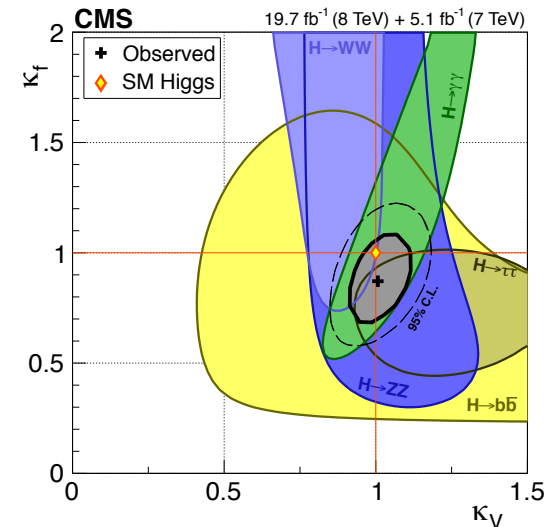
# Testing Higgs Couplings

- Higgs couplings unambiguously predicted
- **Simplest approach:**

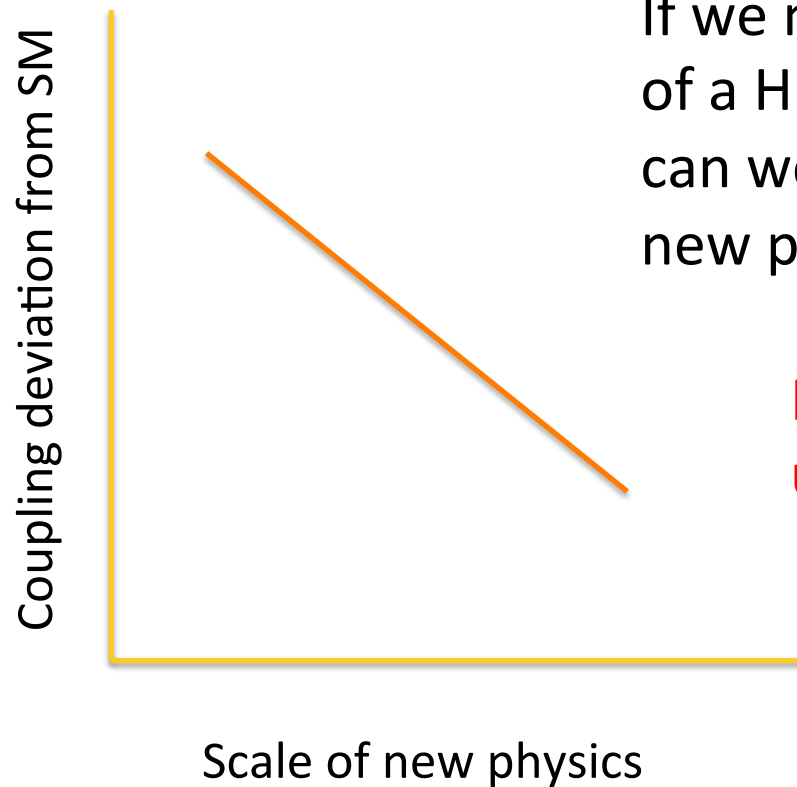
$$L_F \rightarrow (\kappa_F) \frac{M_f}{v} f \bar{f} H$$

$$L_V \rightarrow \frac{M_V^2}{v} (\kappa_V) V^\mu V_\mu$$

- **SM,  $\kappa_i=1$**
- In a particular model, there will be relationships among  $\kappa$ 's



## What we hope for



If we measure a large deviation of a Higgs coupling from the SM, can we associate it with a scale of new physics?

For this to work, we have to understand the SM first

# Small Corrections Expected in BSM

If new physics is at 1 TeV:

	$\delta\kappa_V$	$\delta\kappa_b$	$\delta\kappa_\gamma$
Singlet	~6%	~6%	~6%
2HDM	~1%	~10%	~1%
MSSM	~.001%	~1.6%	~-0.4%
Composite	~-3%	~-(3-9)%	~-9%
Top Partner	~-2%	~-2%	~1%

Patterns of deviations can pinpoint specific BSM physics

# Higgs Couplings (STILL!) Interesting

- Precision measurements of Higgs couplings rigorous tests of SM
  - NNLO QCD, NLO EW, resummation all needed!
  - Flavor structure of Higgs sector untested so far
- Models with TeV scale new physics give small corrections to  $\kappa$  parameters

- We would expect deviations from SM to be  $O(v^2/\text{TeV}^2)$
- *Just starting to probe interesting region*

# Testing Higgs Couplings

- Assume 1 resonance/zero width approx/no new tensor structures

$$\sigma \cdot BR(ii \rightarrow H \rightarrow jj) = \frac{\sigma_{ii}\Gamma_{jj}}{\Gamma_H}$$

- Define scaling factors  $\kappa$

$$\mu(gg \rightarrow H \rightarrow \tau^+\tau^-) = \frac{\sigma(gg \rightarrow H \rightarrow \tau^+\tau^-)}{\sigma(gg \rightarrow H \rightarrow \tau^+\tau^-)|_{SM}} = \frac{\kappa_g^2 \kappa_\tau^2}{\kappa_h^2}$$

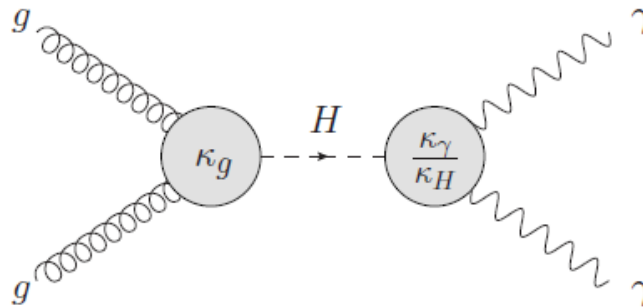
- Approaches to loops:  $\kappa_\gamma$ ,  $\kappa_g$  can be
  - Written as function of SM scaling factors: **eg  $\kappa_g = \kappa_g(\kappa_t, \kappa_b)$**
  - Treated as **free parameters** to look for BSM contributions

[LHC Higgs Cross Section Working group, arXiv1307.1346]

# Higgs Couplings

Example:

$$gg \rightarrow H \rightarrow \gamma\gamma$$



$$(\sigma \cdot BR)(gg \rightarrow H \rightarrow \gamma\gamma) = [\sigma(gg \rightarrow H) \cdot BR(H \rightarrow \gamma\gamma)]_{SM} \times \frac{\kappa_g^2 \cdot \kappa_\gamma^2}{\kappa_H^2}$$

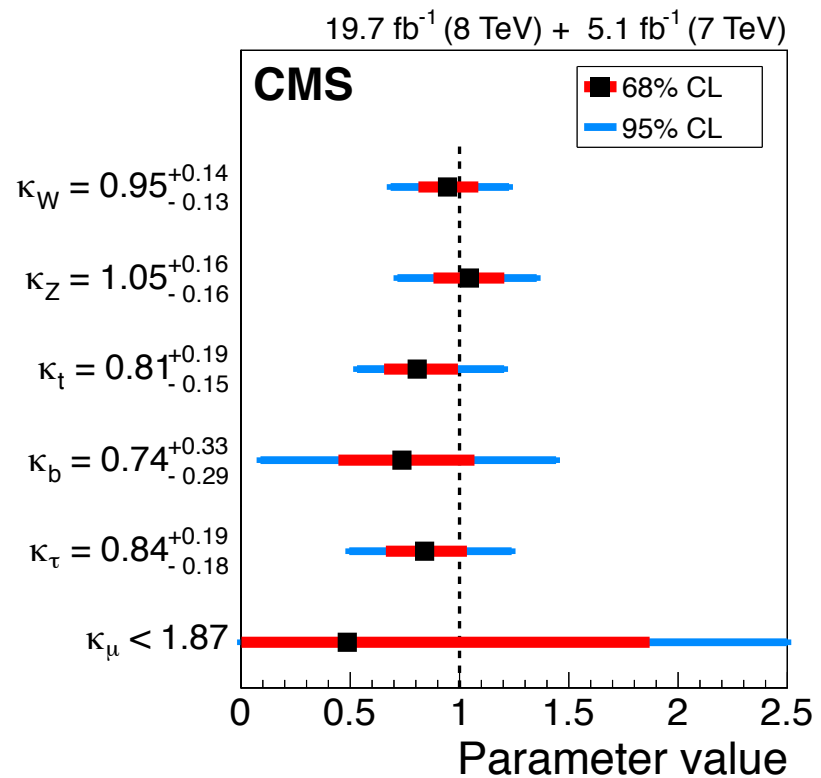
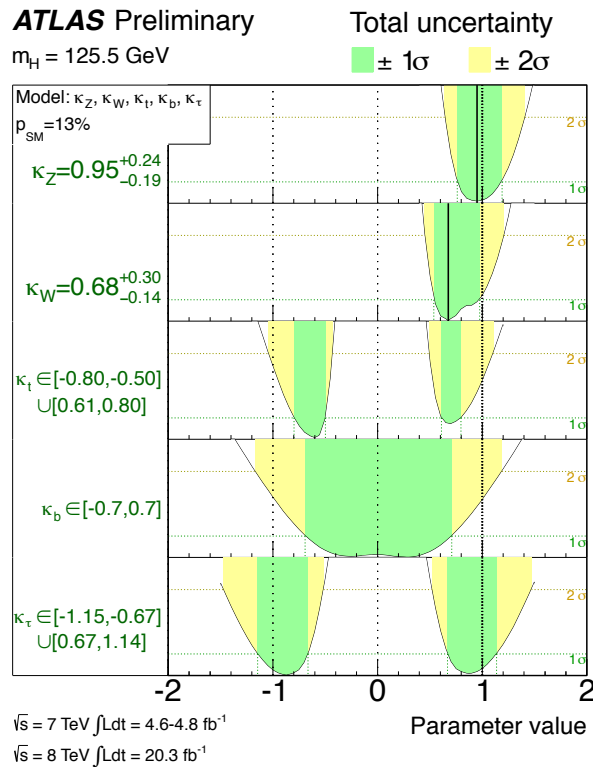
$\kappa_H^2$  is the scale factor to the total Higgs decay width

$$\kappa_H^2 = \sum_x \kappa_x^2 \cdot BR(H \rightarrow xx) \xrightarrow{\text{No BSM decays}} \kappa_H^2 = \sum_x \kappa_x^2 \cdot BR_{SM}(H \rightarrow xx)$$

\*BSM decays really just means unobserved decays

# $\kappa$ Fits (miniature subset)

*Plenty of room for non-SM physics at 10-20% level*



Only SM particles in loops; no invisible decays in these fits

*\* Read the fine print in fits*



# Invisible width

- Invisible is just stuff you don't observe

$$\Gamma_H = \kappa_H^2 \Gamma_H^{SM} = \sum_i \kappa_i^2 \Gamma(H \rightarrow X_i X_i)^{SM} + \Gamma(H \rightarrow invisible)$$

$$\kappa_H^2 = \sum_i \kappa_i^2 \frac{\Gamma(H \rightarrow X_i X_i)}{\Gamma_H^{SM}} + \frac{\Gamma(invisible)}{\Gamma_H^{SM}}$$

$$= \sum_i \kappa_i^2 BR(H \rightarrow X_i X_i) + \kappa_H^2 BR(H \rightarrow invisible)$$

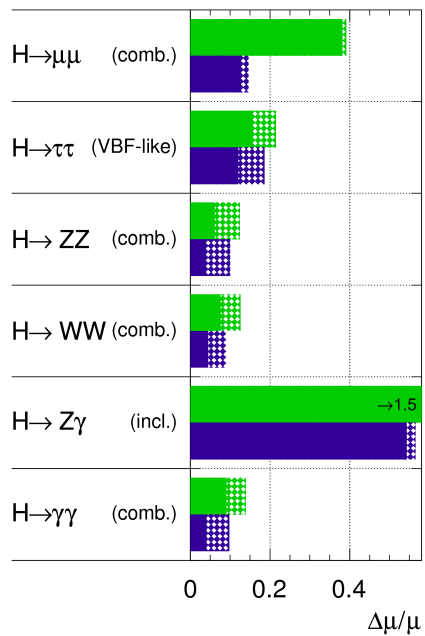
- Can do fits allowing for  $H \rightarrow$  invisible
- CMS:  $BR(H \rightarrow invisible) < .49$  at 95%
- Similar limits from ZH production,  $H \rightarrow$  invisible

Invisible could be new dark matter particles,  
could be unobserved decays to charm....

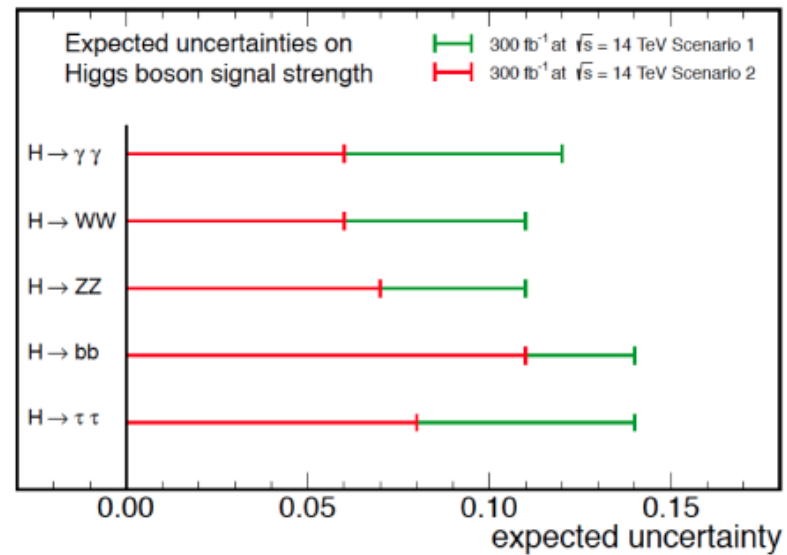
# Projections

Lumi	Exp.	$\kappa_\gamma$	$\kappa_W$	$\kappa_Z$	$\kappa_g$	$\kappa_b$	$\kappa_t$	$\kappa_\tau$	$\kappa_{Zg}$	$\kappa_\mu$
300 fb <sup>-1</sup>	ATLAS	9%	9%	8%	11-14%	22-23%	20-22%	13-14%	24%	21%
	CMS	5-7%	4-6%	4-6%	6-8%	10-13%	14-15%	6-8%	41%	23%
3000 fb <sup>-1</sup>	ATLAS	4-5%	4-5%	4%	5-9%	10-12%	8-11%	9-10%	14%	7-8%
	CMS	2-5%	2-5%	2-4%	3-5%	4-7%	7-10%	2-5%	10-12%	8%

**ATLAS** Simulation Preliminary  
 $\sqrt{s} = 14$  TeV:  $\int L dt = 300 \text{ fb}^{-1}$ ;  $\int L dt = 3000 \text{ fb}^{-1}$

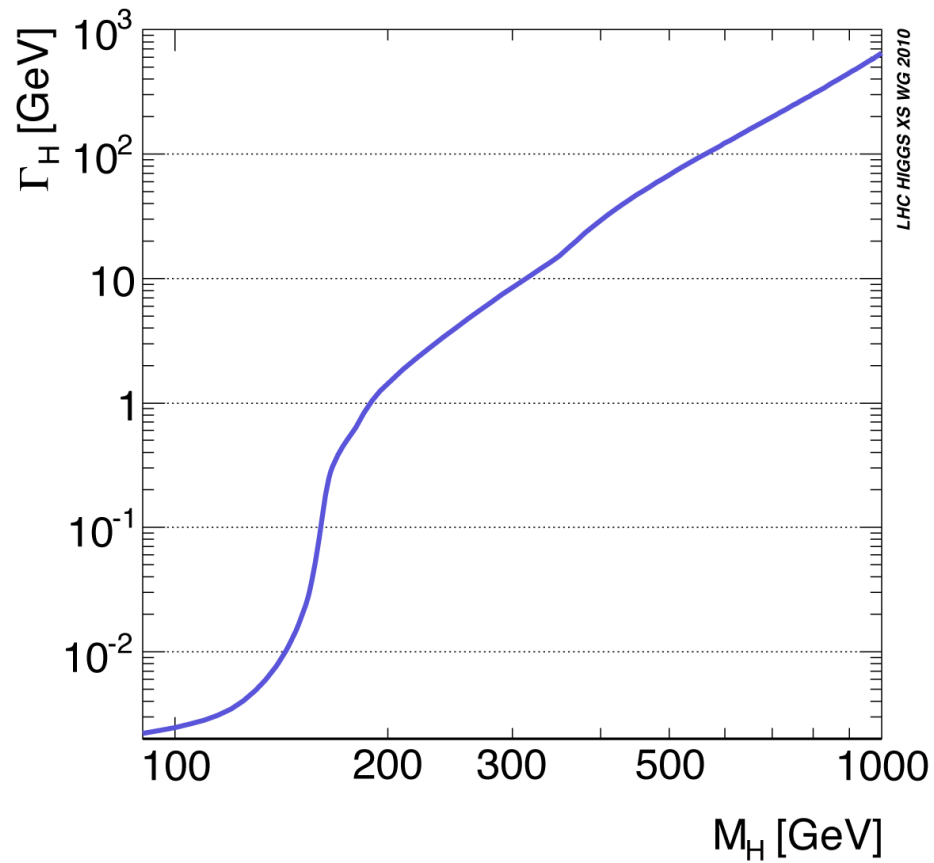


**CMS** Projection



\* Projections allow loop factors,  $\kappa_\gamma$ ,  $\kappa_g$  to vary independently

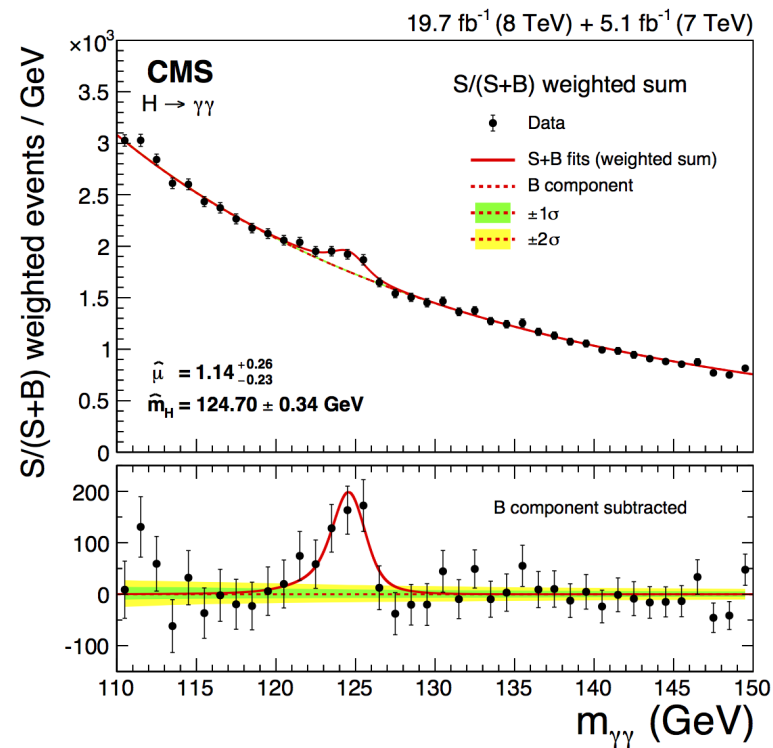
# SM Higgs is Narrow



$$\Gamma_H(M_H = 125 \text{ GeV}) = 4 \text{ MeV} \pm 4\%$$

# Direct Measurement of Higgs width

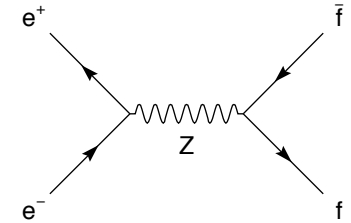
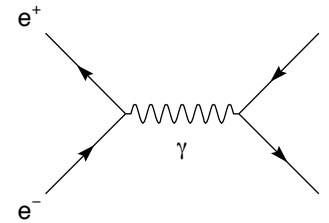
- Detector resolution a few GeV in  $\gamma\gamma$  channel
- Limits are weak:  $\Gamma_H < 6.9 \text{ GeV}$  ( $1600 \Gamma_H^{\text{SM}}$ ) at 95% CL



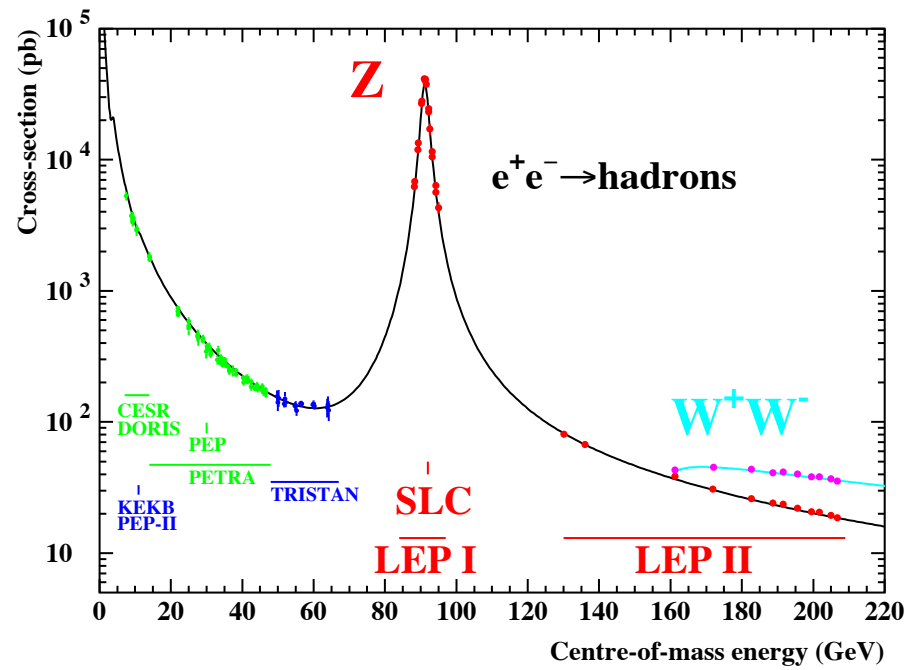
# Z-Resonance

$$e^+e^- \rightarrow f\bar{f}$$

$$A \sim g_{Zff}g_{Zee} \frac{1}{s - M_Z^2 + iM_Z\Gamma_Z}$$



- Narrow resonance:  $\Gamma_Z = 2.495 \pm .0023 \text{ GeV}$



## Narrow width approximation

- Integral near resonance:

$$I = \int \frac{1}{(s - M_Z^2)^2 + (\Gamma_Z M_Z)^2} ds$$

$$\tan \theta = \frac{s - M_Z^2}{\Gamma_Z M_Z} \quad I = \int \frac{d\theta}{\Gamma_Z M_Z} \quad \theta_{min} \sim -\pi, \theta_{max} \sim 0$$

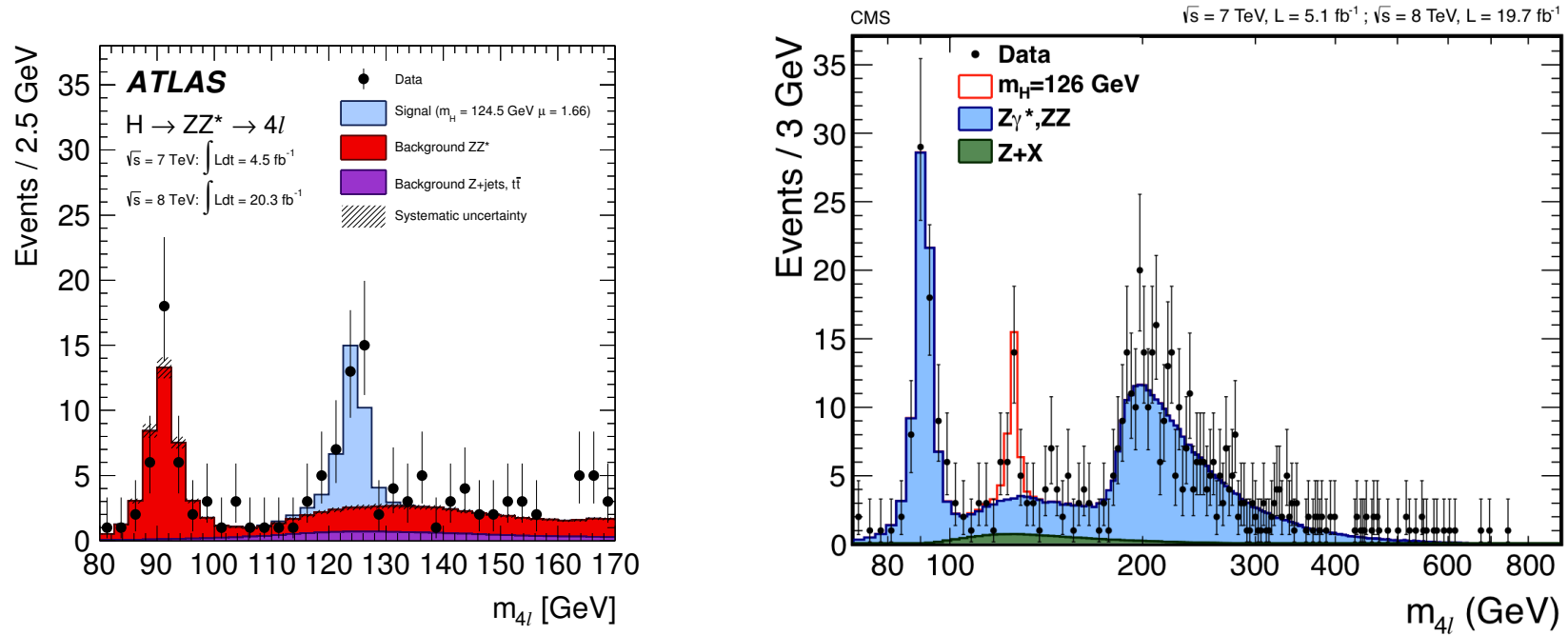
$$\frac{1}{(s - M_Z^2)^2 + (\Gamma_Z M_Z)^2} \rightarrow \frac{\pi}{\Gamma_Z M_Z} \delta(s - M_Z^2)$$

$$\sigma_{res} \sim \frac{(g_Z f_f g_Z e_e)^2}{\Gamma_Z}$$

Sensitive to  
resonance width

$$gg \rightarrow H \rightarrow ZZ$$

- Goal: Measure  $gg \rightarrow H \rightarrow ZZ$  and use insights about resonances



## Aside on HZZ couplings

- $HZ_L Z_L$  couplings vestige of EWSB
  - Massless gauge theory has no longitudinal polarizations
  - $HZ_L Z_L$  coupling  $\sim M_H^2/v$
  - Expect resonance to have high energy tail

$$\epsilon_L(p_Z) \sim \frac{p_Z}{M_Z} \quad \longrightarrow \quad \text{Enhanced at high energy}$$



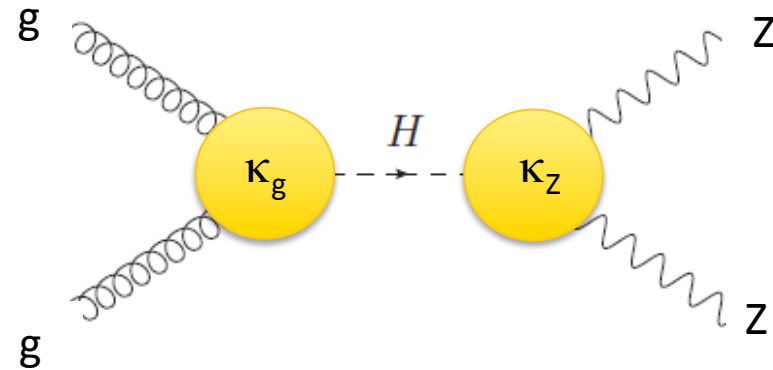
# Higgs Resonance

- Above resonance:

$$\sigma_{above} \sim \frac{\kappa_g^2 \kappa_Z^2}{s} \epsilon_Z^\mu \epsilon_Z^\nu$$

$$\epsilon_L^\mu \sim \frac{p^\mu}{M_Z}$$

$$\sigma_{above} \sim \frac{\kappa_g^2 \kappa_Z^2}{M_Z^2}$$



$$I = \int \frac{1}{(s - M_H^2)^2 + (\Gamma_H M_H)^2} ds \rightarrow \frac{1}{s}$$

No dependence on width

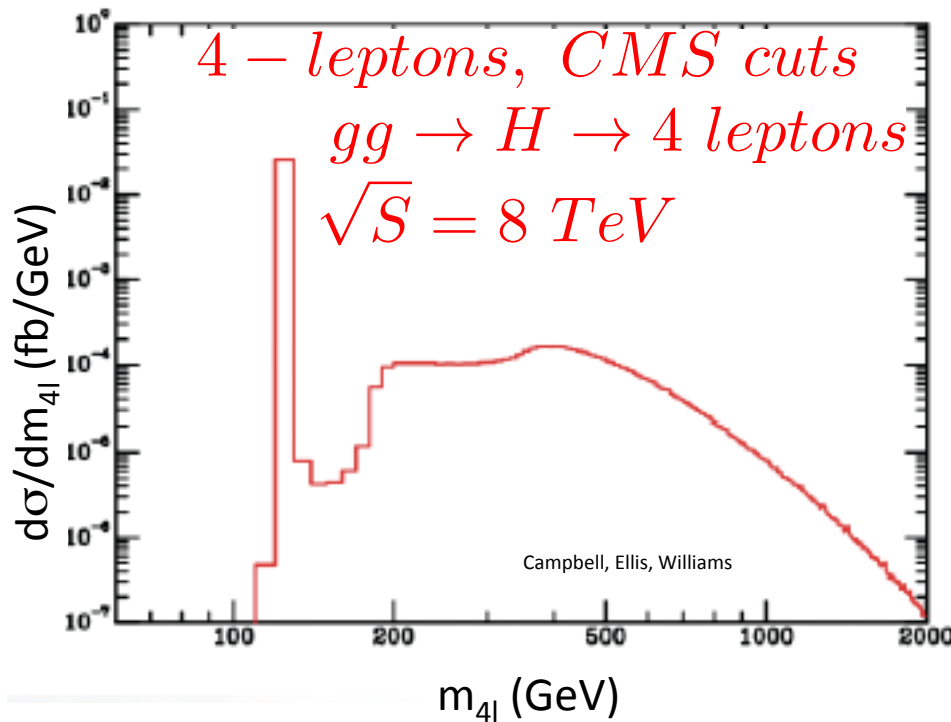
Longitudinal Z polarization grows with energy

# Idea



- Measure above and below the peak:

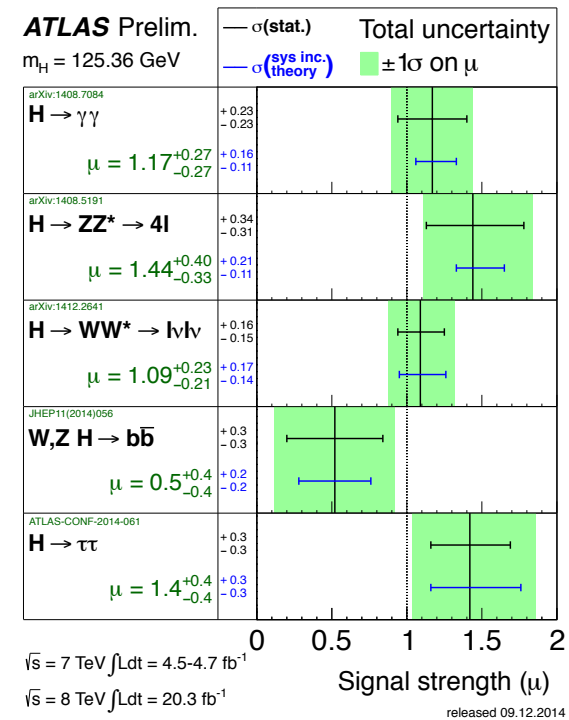
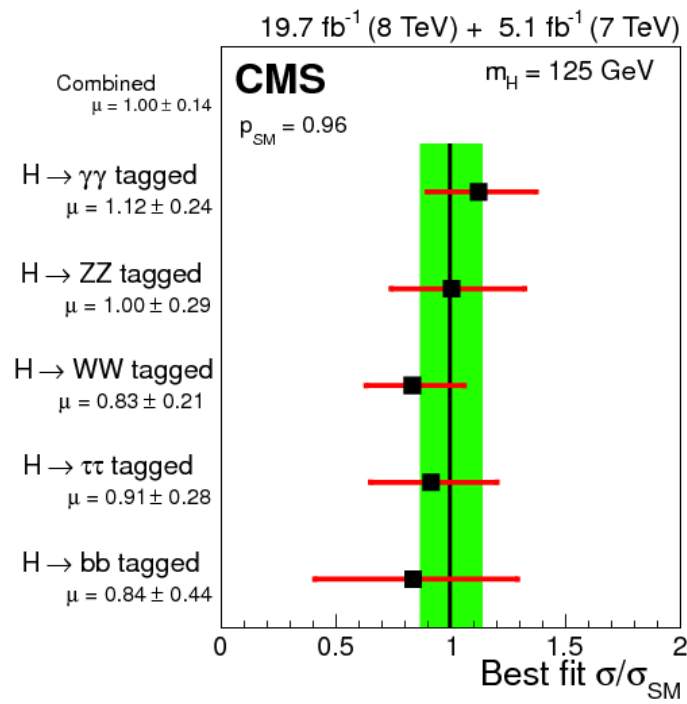
$$\frac{\sigma_{above}}{\sigma_{res}} \sim \Gamma_H$$



About 15% of  
total cross section  
in  $m_{4l} > 140 \text{ GeV}$   
region above peak

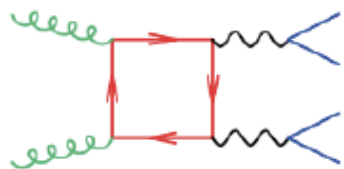
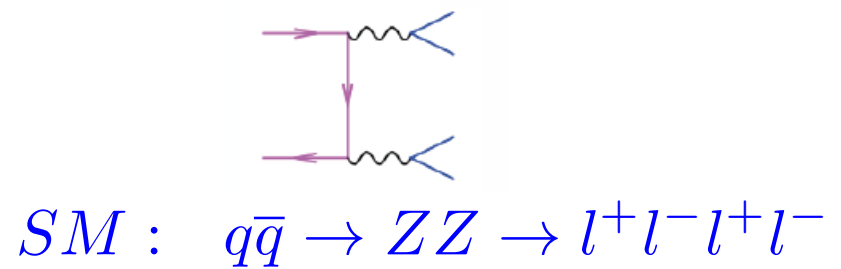
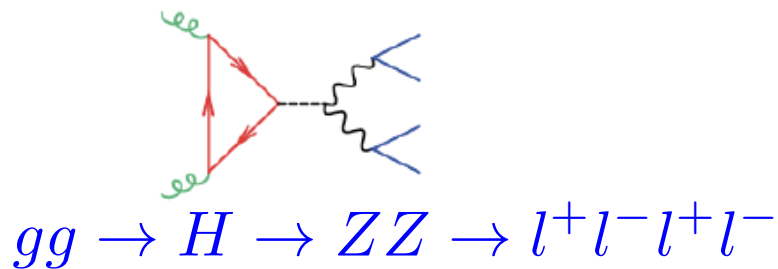
# Technique

- On shell measurement of Higgs cross section consistent with SM expectations
- A larger Higgs width  $\longrightarrow$  more off-shell events:  $\Gamma_H \sim \sigma_{\text{above}} / \sigma_{\text{res}}$



# Other contributions to 4 leptons

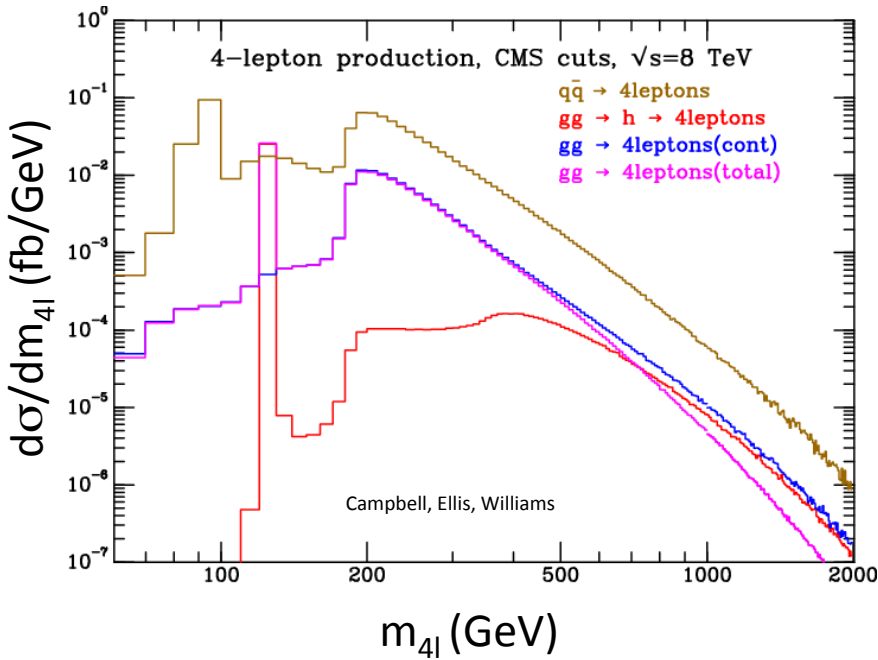
- Not just the Higgs



Box diagram can interfere with Higgs contribution

Separation into “signal” and “background” misses interference

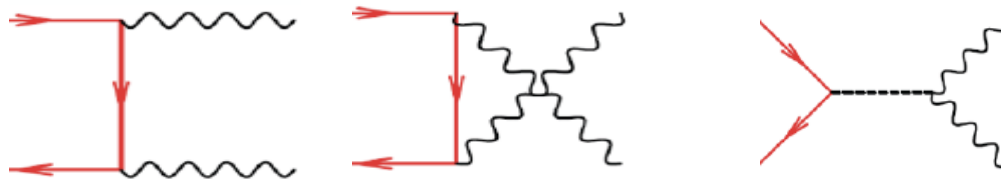
# Observe destructive Interference



- Note destructive interference
- Quark channel  $\gg$  Higgs contribution

# Unitarity and the Higgs Width

$$t\bar{t} \rightarrow Z_L Z_L$$



$O(E^2)$  terms cancel

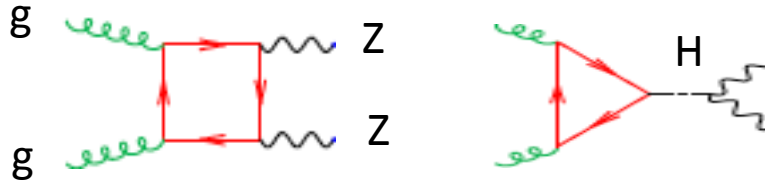


$O(EM_t)$  terms cancel

A naïve separation into signal and background would miss this effect

*Observation of this cancellation shows that Higgs boson is enforcing unitarity cancellations: No effects which grow with energy*

# Unitarity and the Higgs width



- Interference small on peak, but significant above peak

Averaging 7/8 TeV data:

$$\frac{\sigma(m_{4l} > 130 \text{ GeV})}{\sigma_{peak}} \sim 2.8 \frac{\Gamma}{\Gamma_{SM}} - 6 \sqrt{\frac{\Gamma}{\Gamma_{SM}}}$$

Interference is destructive and weakens bound

$$CMS : \Gamma_H < 4.2 \Gamma_H^{SM}$$

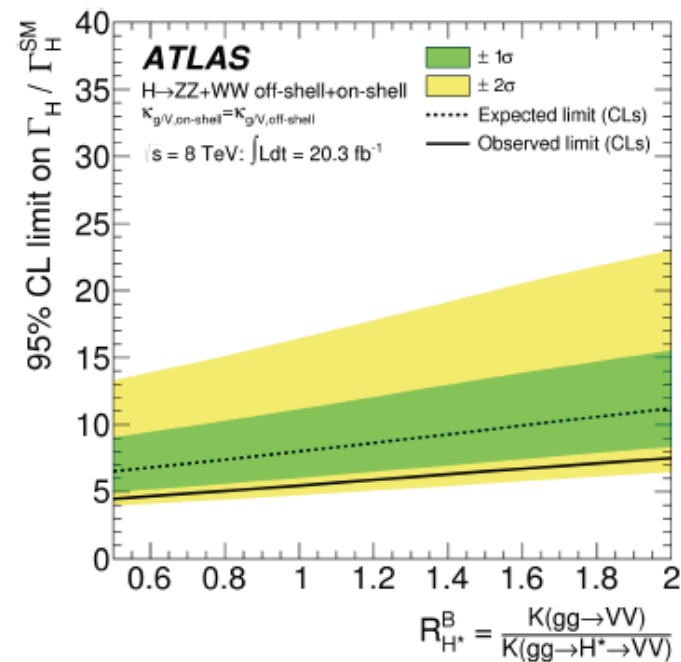
$$ATLAS : \Gamma_H < (4.5 - 7.5) \Gamma_H^{SM}$$

Sign of interference predicted by unitarity conservation

[Campbell, Ellis, Williams, arXiv:1311.3589]

# Counting Orders

- Destructive interference computed at LO (even though it's a loop)
- Need K factor for gg contributions (unknown)
  - Assume similar to that for  $gg \rightarrow$  Higgs ( $\sim 2$ )



Resonance contribution  
known at N<sup>3</sup>LO

Box contribution  
only known at LO



# Are we really measuring $\Gamma_H$ ?

- On-shell measurement:

$$\mu_{peak} = \frac{\sigma_{peak}}{\sigma_{peak}^{SM}} \sim \frac{\kappa_g^2 \kappa_Z^2}{(\Gamma_H / \Gamma_H^{SM})} \sim 1$$

- Since  $\mu_{peak} \sim 1$  a value  $\Gamma_H > \Gamma_H^{SM}$  implies  $\kappa_g^2 \kappa_Z^2 > 1$
- i.e. **BSM physics**
- Measurement above peak is  $\sigma_{above} \sim \kappa_g^2 \kappa_Z^2$ 
  - **Consistency check**
  - Assumes correlation between  $\kappa$  on-shell and above peak

## New Physics Changes $\kappa$ 's

- With BSM physics  $\kappa(m_{ZZ}^2) \neq \kappa(M_H^2)$  in general
- Simple example: Add a colored scalar (as in the MSSM)

$$L \sim -\kappa_s \frac{2m_s^2}{v} H s^* s$$

- For a color triplet scalar

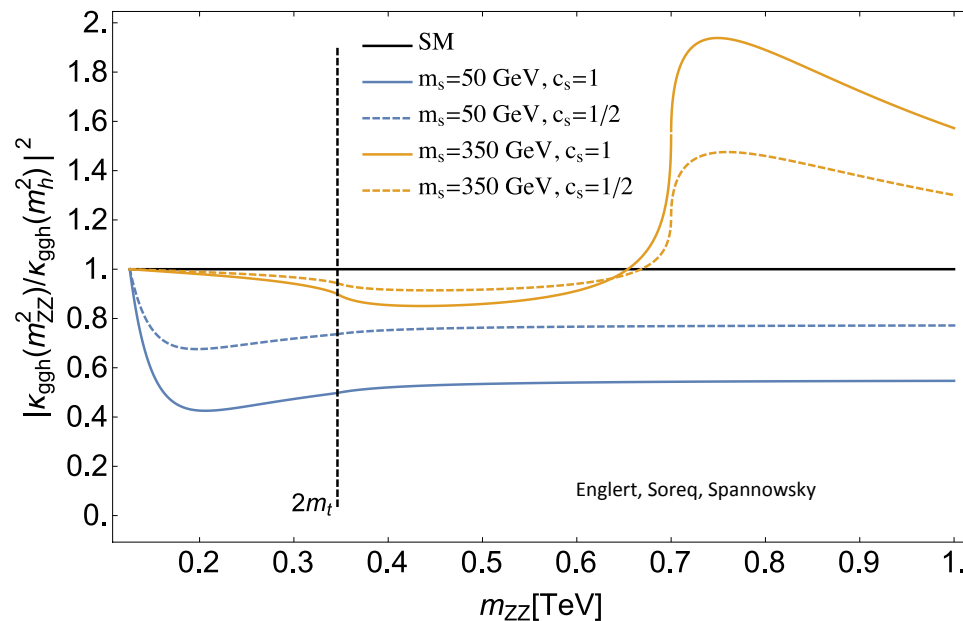
$$\kappa_g(\hat{s}) = 1 + \frac{\kappa_s A_s(\tau_s)}{(A_t^{SM}(\tau_t) + A_b^{SM}(\tau_b))} \quad \tau_i = \frac{\hat{s}}{4m_i^2}$$

- Relation of off-shell couplings to on-shell couplings depends on dynamics of model

Colored scalar changes  $gg \rightarrow H$   
production rate

## Effects can be large

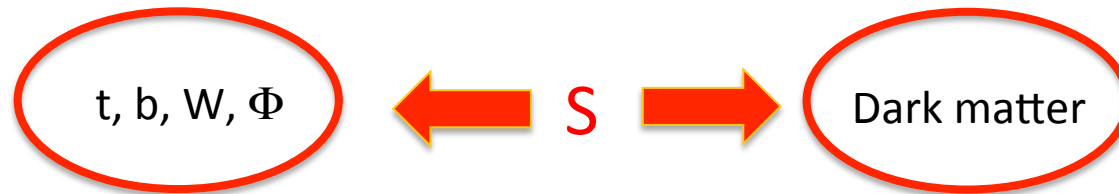
- Look at:  $\frac{\kappa_g(m_{ZZ}^2)}{\kappa_g(M_H^2)}$
- Can have either enhancement or suppression



Interpretation  
requires assumptions  
about model

## Example: Additional Higgs Singlet

- Dark matter models often have Higgs singlet



- Communication with SM particles through mixing
  - SM Higgs mixed with electroweak singlet, S

$$V_4 = \lambda_m |\Phi|^2 S^2 + \frac{\lambda_{SM}}{2} |\Phi|^4 + \frac{\lambda_S}{2} S^4$$

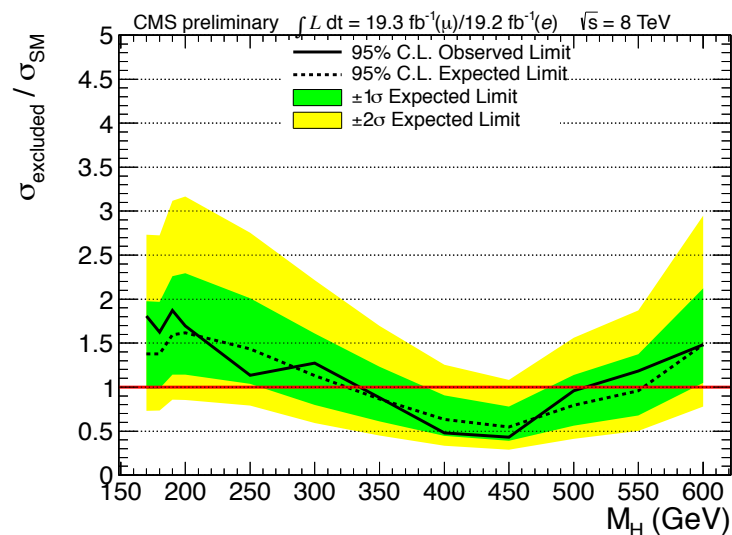
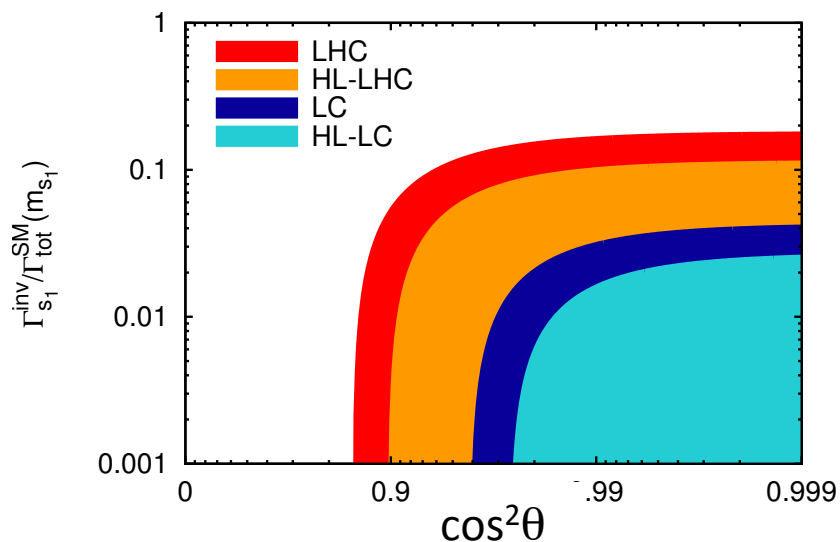
$$h = \cos \theta \phi_0 + \sin \theta S$$

$$H = -\sin \theta \phi_0 + \cos \theta S$$

- Universal rescaling of Higgs couplings,  $\kappa_F = \kappa_V = \cos \theta$

# Complementarity of Approaches

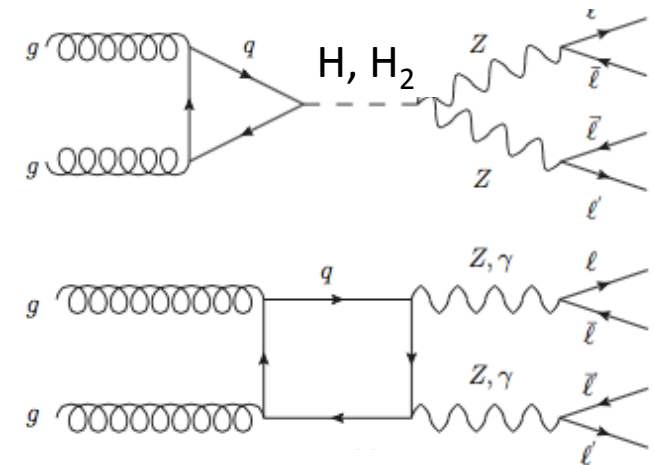
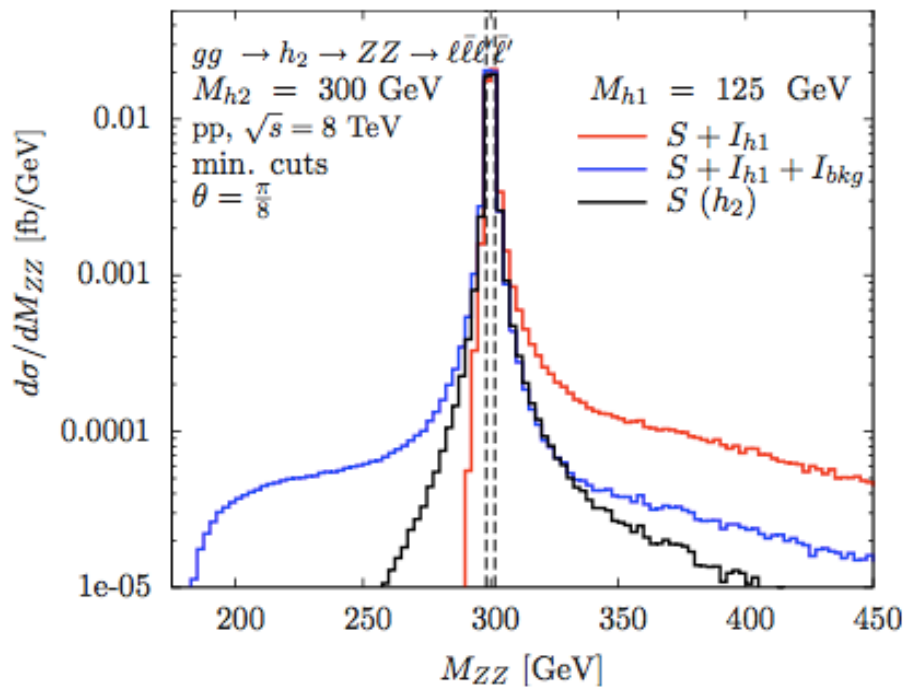
- Find heavier Higgs and measure deviations in couplings
- $\sin^2\theta < .12$  (with no invisible BR) from H couplings
  - Need increased sensitivity in direct searches



These simple studies are very important for limiting EWSB models

# Higgs Width in Singlet Model

- Large interference effects from new scalar,  $H_2$
- Quantitatively different results from SM



[Kauer, O'Brien]

## Example: Two Higgs Doublets

- Many models have extended Higgs sectors
  - Two Higgs doublet models can be used as effective theories for many of these models
  - 5 Higgs bosons:  $h, H, A, H^\pm$
  - 4 types of 2HDM models which avoid tree level FCNCs
  - Classified in terms of  $\tan \beta = v_2/v_1, \alpha, m_h = 125 \text{ GeV}$

$$\sin 2\alpha = -\sin 2\beta \left( \frac{M_H^2 + m_h^2}{M_H^2 - m_h^2} \right)$$

- Predictive models (MSSM is special case)

Rich Phenomenology

# Higgs Couplings: 2 Parameters

- 2 Higgs doublet models with no FCNC
  - Parameters are  $\alpha$  (mixing in neutral h),  $\tan \beta$ ,  $M_H$ ,  $M_A$ ,  $M_{H^\pm}$
  - 4 possibilities for Higgs coupling assignments

$$L = -g_{hii} \frac{m_i}{v} \bar{f}_i f_i h - g_{hVV} \frac{2M_V^2}{v} V_\mu V^\mu h$$

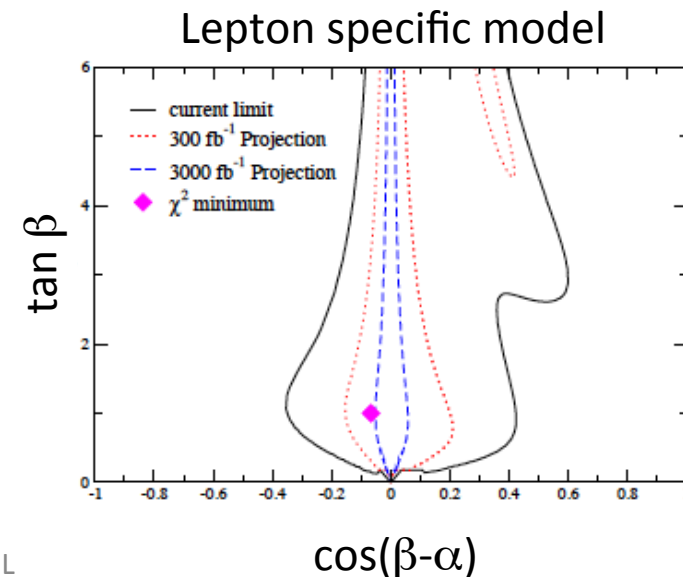
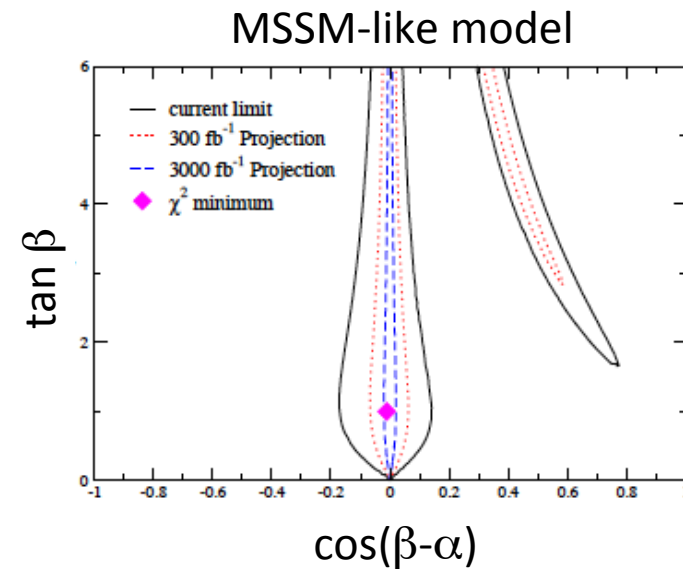
	I	II	Lepton Specific	Flipped
$g_{hVV}$	$\sin(\beta - \alpha)$	$\sin(\beta - \alpha)$	$\sin(\beta - \alpha)$	$\sin(\beta - \alpha)$
$g_{ht\bar{t}}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$
$g_{hb\bar{b}}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$
$g_{h\tau^+\tau^-}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$	$-\frac{\sin \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$

Type II is MSSM  
– like 2 Higgs doublet model



# Decoupling Limit

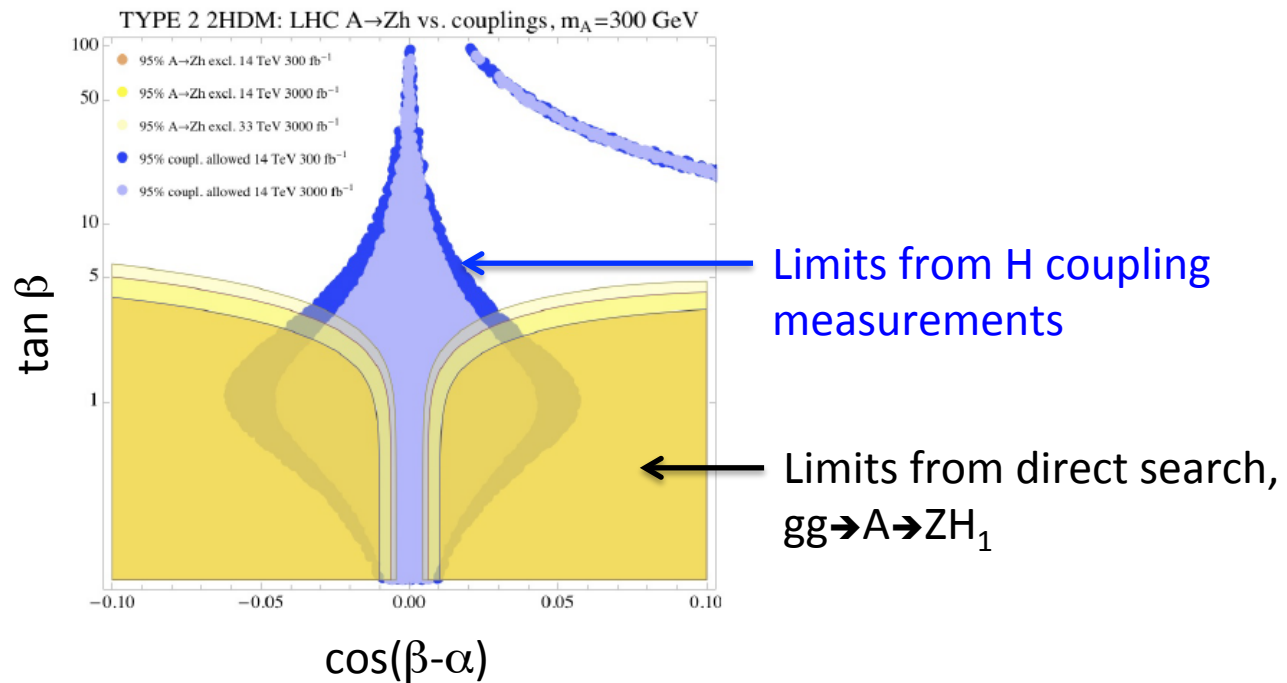
- 2HDMs approach SM when  $\cos(\beta-\alpha) \rightarrow 0$
- Current limits allow non-SM like couplings
- $\tan \beta < .4$  excluded by  $\Delta M_{Bd}$  for  $M_{H^\pm} < 2 \text{ TeV}$ 
  - Higgs coupling measurements sensitive probes of theory even if new Higgs particles too heavy to be produced
  - Prefer small  $\tan \beta$



# New Higgs Bosons → New Signatures

- 2HDM example:  $gg \rightarrow A \rightarrow ZH_1$ 
  - Complementary limits from direct search/coupling measurements

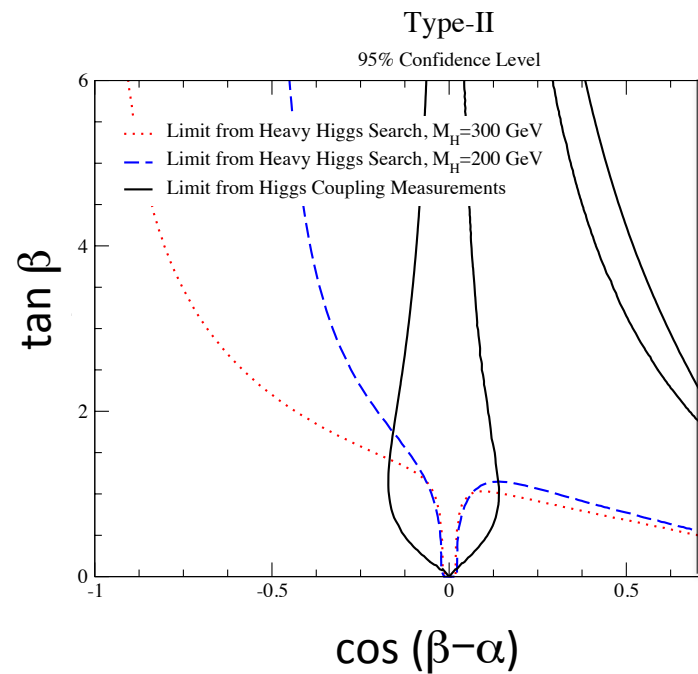
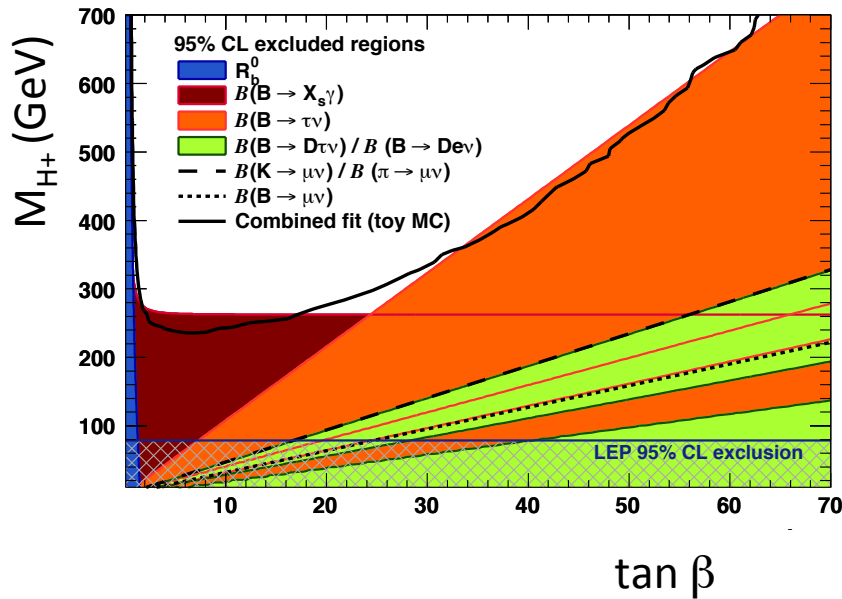
14 TeV  
projections:



[Brownson, 1308.6334]

# Again.... Complementarity

- Many limits on 2HDM besides Higgs parameters
- Precision EW, B physics.....



## The Problem with the $\kappa$ Approach

- SM Higgs couplings fixed—cannot be varied separately
  - Can test consistency of SM hypothesis
- Run 1 approach:
  - Rescale fundamental Higgs couplings:  $\kappa_W, \kappa_Z, \kappa_f$  and loop induced couplings,  $\kappa_\gamma, \kappa_g, \kappa_{\gamma Z}$
  - Simple and easy to implement
  - Electroweak corrections not included exactly
  - No information from angular distributions
  - How to interpret deviations?
    - *Rescaling breaks gauge invariance, renormalizability*

# Need to Use Effective Field Theory

- Many possible parameterizations:
  - HISZ (no fermions), Buchmuller/Wyler (59 operators before flavor), SILH,.....
  - Operators related by equations of motion
  - Need to simplify and make assumptions!
  - Assume: Higgs comes from doublet ***BIG ASSUMPTION***
    - Always have combination  $(H+v)^n$
    - Assume CP conservation, no flavor violation in Higgs sector

# Higgs Couplings & Effective Field Theory

- Operators obey symmetry of SM

$$L \sim L_{SM} + \sum_i \frac{C_i}{\Lambda^{n-4}} O_n \quad \text{Consistent expansion}$$

- New physics decouples at high scales
  - ***No new light particles***
  - n=6 operators expected to give dominant contribution
  - $\Lambda$  is scale of new physics  $\gg v$
  - EFT valid at  $E \ll \Lambda$
  - Consider all n=6 operators that can be constructed from SM fields

Looking for new physics in tails of distributions, but have to make sure EFT is valid

# New Physics in Higgs Sector

Use effective field theory

Can we determine source of new physics?

No resonance or light resonance

Find resonance!

Current limits will be strengthened at LHC-13

# Construct EFT for Higgs

- Take SM operators and add  $\Phi^\dagger\Phi$

$g_s$	$(\Phi^\dagger\Phi)G_{\mu\nu}^A G^{A,\mu\nu}$	$gg \rightarrow H$
$g$	$(\Phi^\dagger\Phi)B_{\mu\nu}B^{\mu\nu}$	$H \rightarrow \gamma\gamma$
$g'$	$(\Phi^\dagger\Phi)W_{\mu\nu}^a W^{a,\mu\nu}$	$H \rightarrow Z\gamma$ UNKNOWN
$M_W$	$(\Phi^\dagger\Phi)  D_\mu\Phi ^2$	$H \rightarrow VV^*$
$M_H$	$(\Phi^\dagger\Phi)^3$	$\lambda_3$ UNKNOWN
$M_f$	$(\Phi^\dagger\Phi)\bar{f}_L\Phi f_R + h.c.$	$H\tau\tau, Hbb, Htt$

Here, I am only concerned with effective operators that affect Higgs production



# Effective Theory Example

- Very simple EFT:

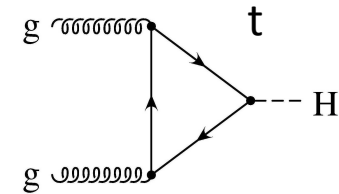
$$L \sim L_{SM} + \frac{\alpha_s}{12\pi v} c_g G^{\mu\nu, A} G_{\mu\nu}^A H - \delta Y_t \frac{M_t}{v} \bar{t} t H$$

–  $gg \rightarrow H$  sensitive to  $|c_g + \delta Y_t|^2$

$$A(gg \rightarrow H) = A^{SM} \left( \frac{M_H^2}{M_t^2} \right) \left[ 1 + \delta Y_t \right] + A^{SM}(0) c_g$$

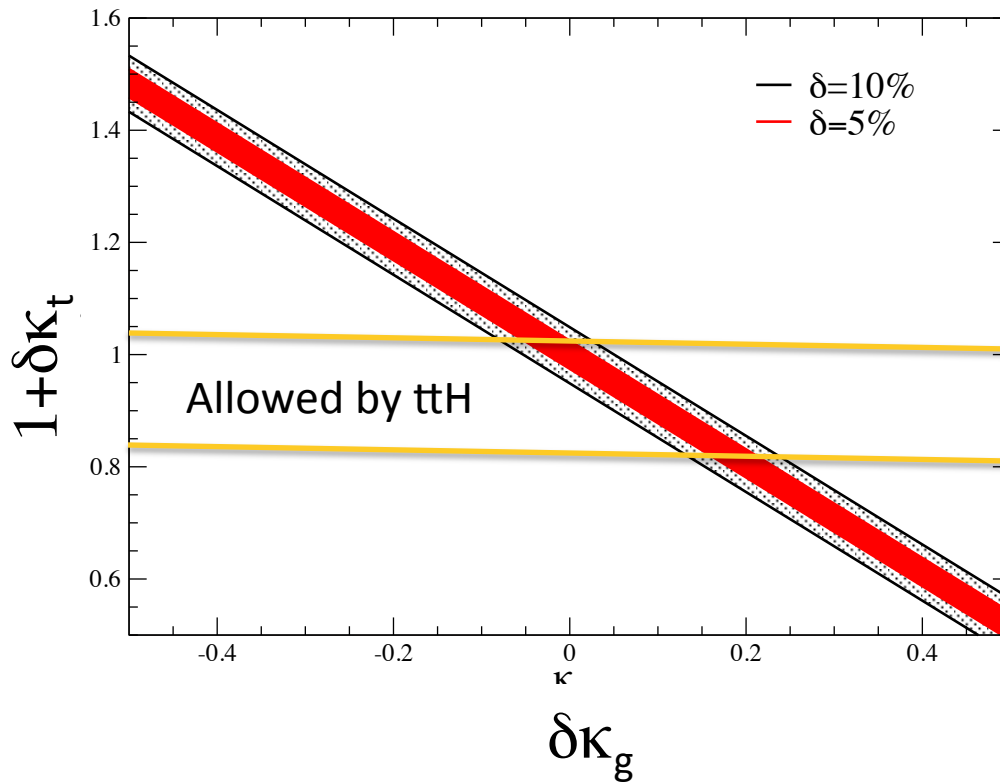
Almost equal in SM

Can't distinguish *long distance* physics ( $\delta Y_t$ ) from *short distance* physics (new particles in loops,  $c_g$  nonzero)



# How to break $\kappa_t$ - $\kappa_g$ degeneracy?

gg  $\rightarrow$  H rate within  $\delta$  of SM prediction



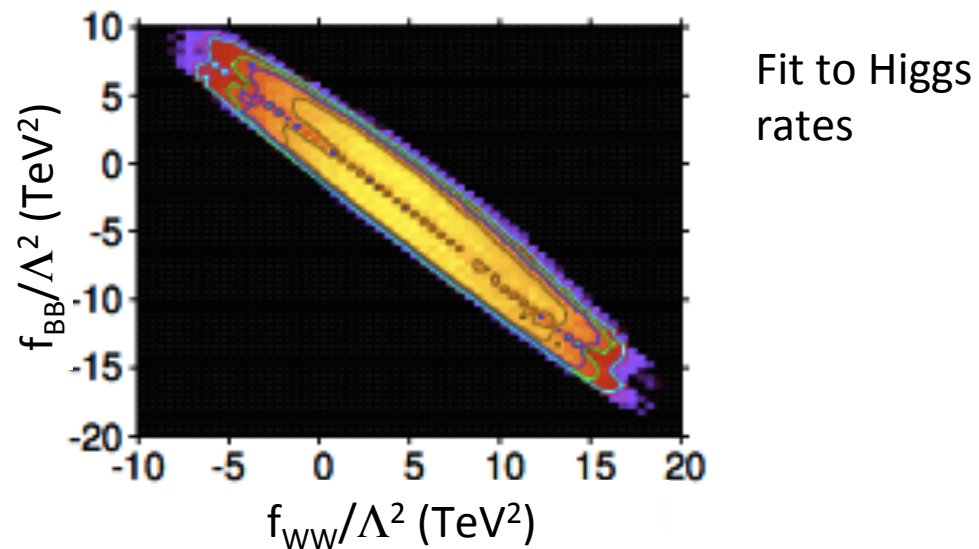
*Need global fits*

- ttH production proportional to  $(1 + \delta\kappa_t)^2$
- (very small dependence on  $\kappa_g$  neglected in ttH)
- Assume

$$\frac{\delta\sigma_{ttH}}{\sigma_{ttH}} \sim .2$$

# Many Global Fits to EFT Parameters

- Limits on EFT coefficients are correlated



95% cl  $f_{WW}/\Lambda^2$ : (-3.7, 13.7)

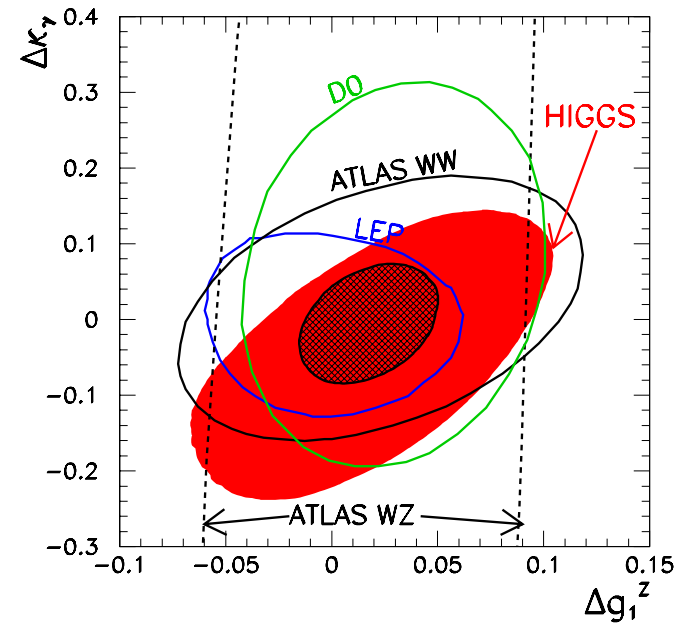
[Corbett et al, arXiv:1505.05516]

# Complementarity

- Effective operators contribute to precision electroweak interactions
- Some operator coefficients known to be small from  $M_W$ ,  $\rho$ ...
- $W^+W^-$  production probes complementary coupling space to Higgs coupling limits

$$\Delta\kappa_\gamma = \frac{M_W^2}{2\Lambda^2} (f_W + f_B)$$

$$\Delta g_1^Z = \frac{M_Z^2}{2\Lambda^2} f_W$$

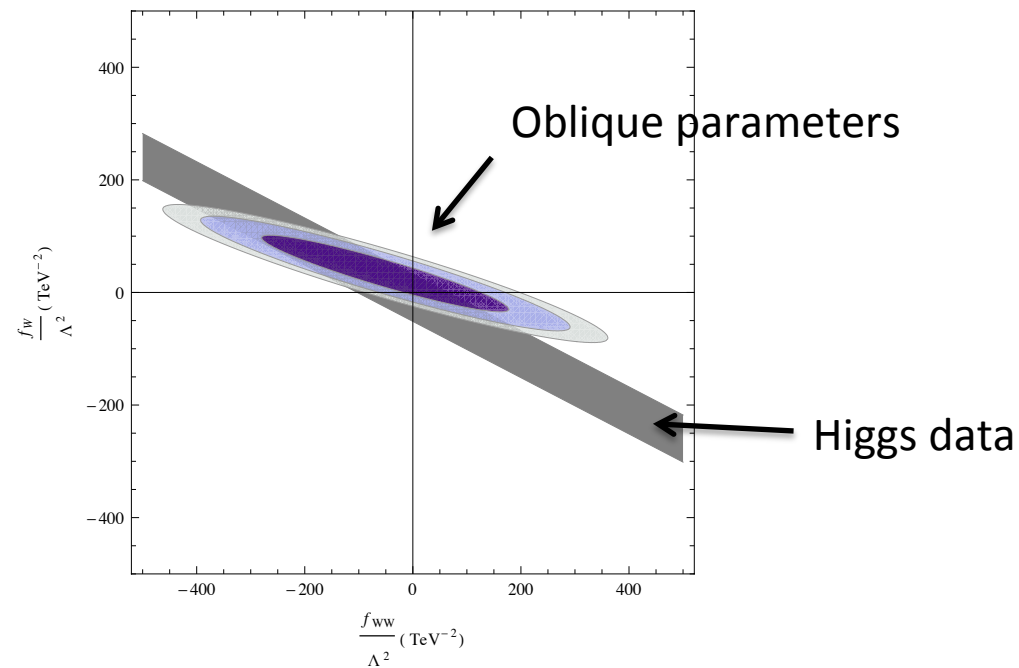


[Corbett et al, arXiv:1304.1151]

Limits highly correlated

# EFT: Need Global Fits

$$\frac{\Gamma(H \rightarrow W^+W^-)}{\Gamma(H \rightarrow W^+W^-)_{SM}} \sim 1 + \left[ .0086 f_{WW} + .017 f_W \right] \left( \frac{1 \text{ TeV}}{\Lambda} \right)^2$$

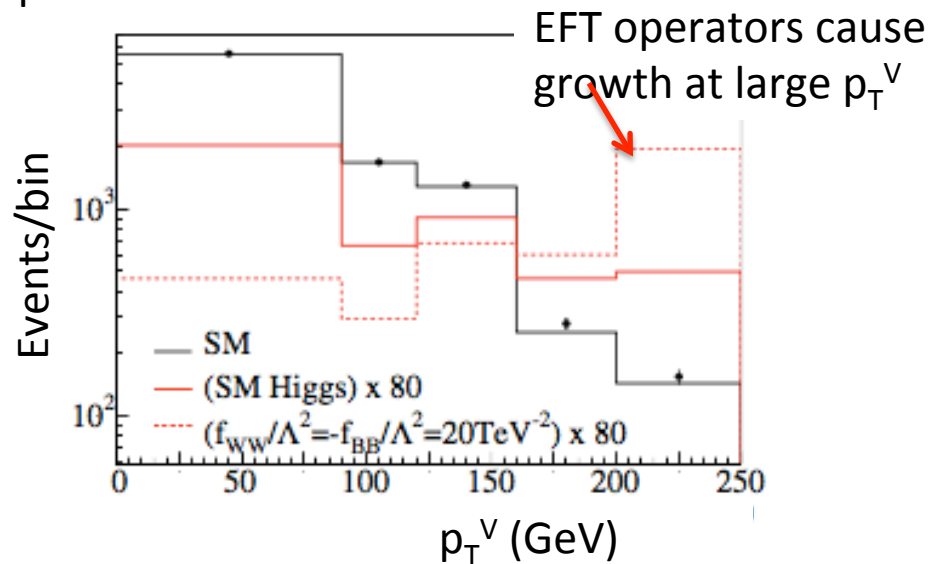


Complementary data from oblique parameters and Higgs data

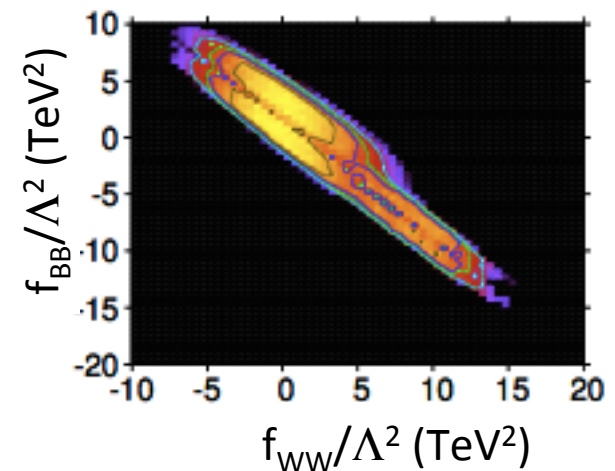
# EFTs change kinematic distributions

- Dimension-6 operators contribute terms  $\sim E^2/\Lambda^2$

VH (single lepton)  
production at 8 TeV



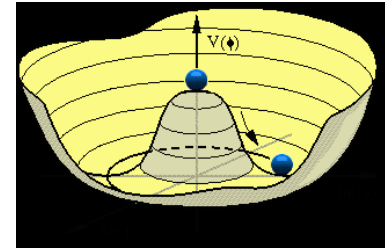
- Can improve fits by including kinematic distributions



95% cl.  $f_{WW}/\Lambda^2$ : (-4.3, 4.4)

# Does the Higgs come from the SM Potential?

$$V = \frac{M_H^2}{2} H^2 + \frac{M_H^2}{2v} H^3 + \frac{M_H^2}{8v^2} H^4$$



We know the the Higgs self interactions are weak:  $\frac{M_H^2}{2v^2} \sim .13$

- Need to measure HHH and HHHH couplings
- HHH coupling can be measured with HH production

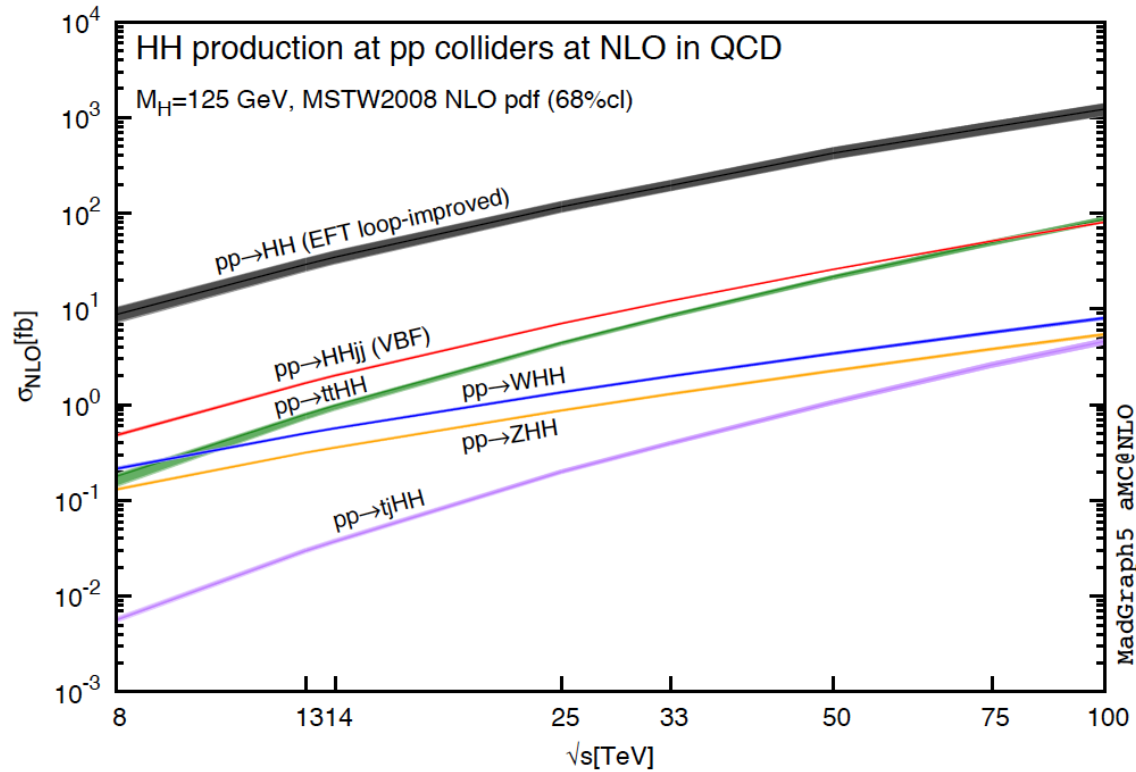
$$14 \text{ TeV} : \sigma(gg \rightarrow HH) \sim 34 \text{ fb}$$

$$\sigma(gg \rightarrow HHH) \sim .04 \text{ fb}$$

**BSM models can change the HHH and HHHH couplings**

$M_H$  is a free parameter of the theory

# Small Rates for HH Production



*This is  $3000 \text{ fb}^{-1}$  physics and  
motivation for 100 TeV Collider!*

[Frederix et al, arXiv:1401.7440, Baglio et al, arXiv:1215.5581]



# Two Higgs Production at LHC

- Cross section has spin-0 and spin-2 contributions

$$\frac{d\sigma(gg \rightarrow HH)}{dt} = \frac{\alpha_s^2}{32768\pi^3 v^4} \left( |F_0|^2 + |F_2|^2 \right)$$

- $M_t^2 \gg s, p_T^2$

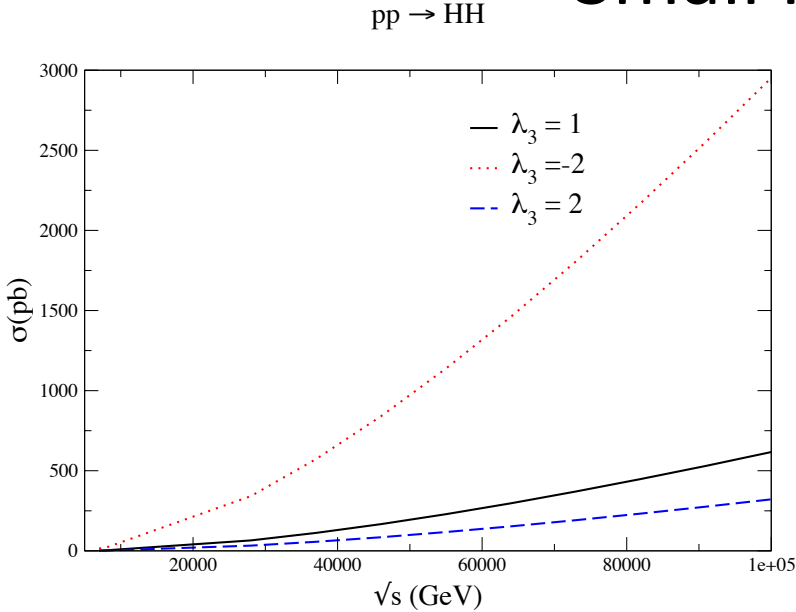
$$F_0 \rightarrow -\frac{4}{3} + \frac{4M_H^2}{s - M_H^2} (\lambda_3)$$

$$F_2 \rightarrow 0$$

HHH coupling (1 for SM)

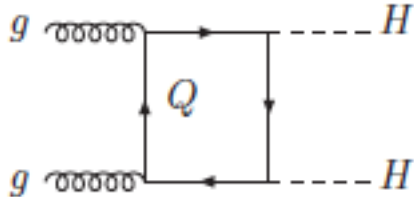
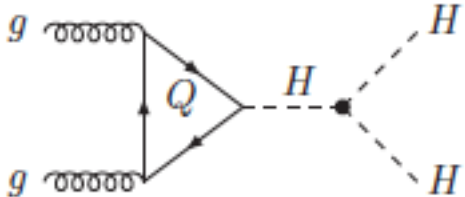
- For large  $s$ , dependence on  $\lambda_3$  suppressed
- More sensitivity to negative  $\lambda_3$
- Exact cancellation at threshold

# Small Rates



For  $\sqrt{s} = 14 \text{ TeV}$ ,  
 $K \sim 2$  in  $m_t \rightarrow \infty$  limit  
 (not in plot)

Sensitivity to HHH coupling; also to  $\text{sign}(\lambda_3)$

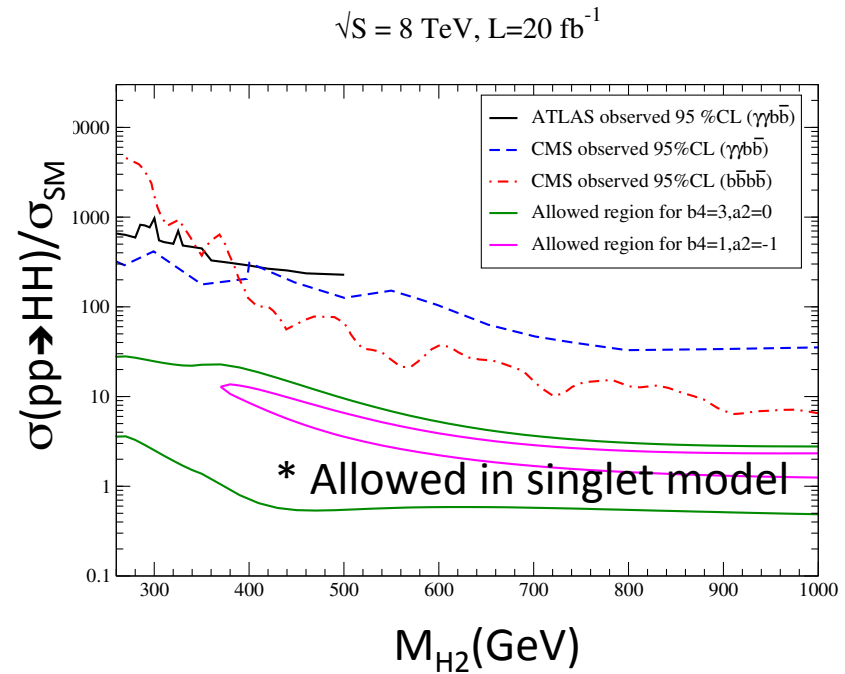
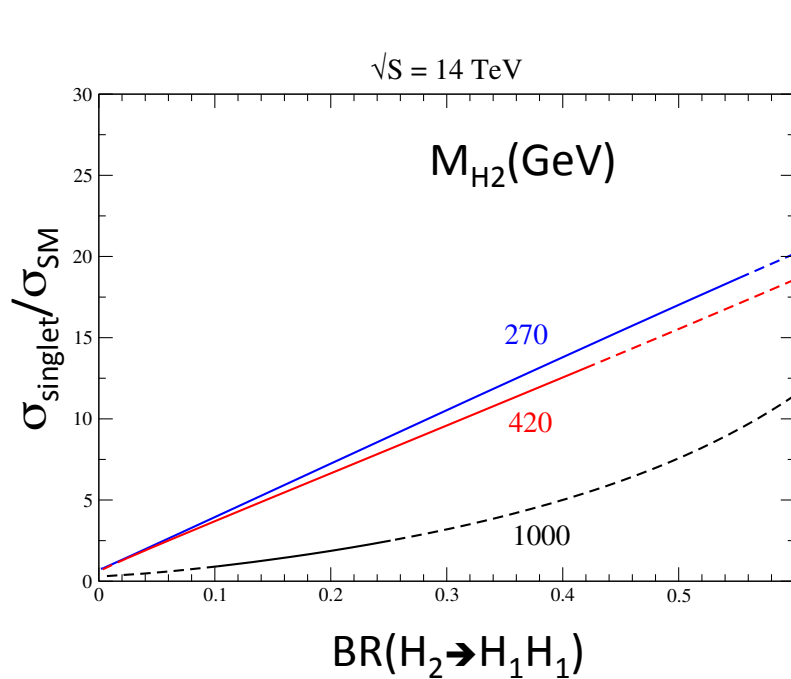


# Double Higgs Production

- Can we measure it?
  - Small rate!
- Can we construct models where it is enhanced?
  - Non-SM couplings ( $\lambda_3$  or  $ttHH$  vertex, eg)
  - New particles in loops
  - Resonances:  $gg \rightarrow X \rightarrow HH$  (MSSM, eg)

Creativity restricted by requiring single H production to have experimentally measured value and by precision EW measurements

# Enhanced HH in Singlet Model



- Enhancements of  $H_1 H_1$  rate of factors 10-15 if  $M_{H_2} < 400 \text{ GeV}$
- Easy to arrange in many models.... Major constraint is  $gg \rightarrow h$  needs to have observed rate

[Chen, Dawson, Lewis, arXiv:1410.5488]

# The Story is Just Beginning

We are just starting the exploration of weak scale physics

- We know that deviations from SM predictions cannot be too large
- *But there is lots of room for discovery of new Higgs particles, measurements of Higgs signals in new channels, precision measurements of Higgs properties*

Big questions remain: Flavor, dark matter, hierarchy....

*Lots of Higgs Physics  
to do in Run 2!*