Deep Inelastic Scattering Part 1

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Outline

Day 1:

- 1. Introduction to DIS and the Quark Parton Model
- 2. Formalism

→Unpolarized DIS→Polarized DIS

3. Results and examples

Day 2:

- 1. Nuclear Effects in DIS
- 2. Beyond inclusive scattering
 - \rightarrow Semi-inclusive reactions (SIDIS)



Disclaimer

- I am an experimentalist, very interested in nuclear effects
 → Much of what I will say comes from this perspective
- Most of my work has been at Jefferson Lab
 → You will be seeing a lot of examples from JLab



What is Deep Inelastic Scattering?

Some context:

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DIS: Using lepton (electron, muon, neutrino) scattering to explore the partonic structure of hadronic matter

Advantages of leptonic (vs. hadronic) probes

- → It's QED: at least one vertex is well understand
- → No complicated structure of the probe to deal with
- → Small value of α_{QED} = 1/137 means higher order corrections are small*



To access partonic structure (i.e. quarks and gluons) we need "high" energies and large inelasticities \rightarrow want to avoid the complications from exciting resonances

*Well, usually. Not always true.

What is Deep Inelastic Scattering?

Lepton scattering cross sections have rich, complex structure

- \rightarrow Elastic scattering
- → Production of excited quark bound states – resonances!

We are primarily interested in the regime in which quarks act like quasi-free, weakly interacting particles

The boundary between these regimes not always so clear cut



Figure from R.G. Roberts, <u>The Structure of the Proton</u>



DIS Experiments

- Plethora of data available from a variety of fixed target experiments
 - − SLAC \rightarrow Electrons at 10's of GeV
 - CERN (EMC/BCDMS/NMC/COMPASS) → Muons at 100's of GeV
 - HERMES \rightarrow 27 GeV positrons and electrons
 - E665 → Muons at 490 GeV
 - − JLab \rightarrow 6 GeV electrons \rightarrow 12 GeV
- Only one source of collider DIS data (so far)
 - HERA (Zeus and H1) : 27 GeV positrons (electrons) on 920 GeV protons
- Neutrinos \rightarrow CCFR, CHORUS, NuTeV, MINER*v*A
- Important information can also be gleaned from hadron colliders (RHIC, LHC, etc.)



Deep Inelastic Scattering

Kinematics:

Beam: *k*= (*E*, 0,0,*p*) \rightarrow Typically ignore electron mass so *E=p*

Scattered electron: k' = E', θ Target: $P = (E_p, 0, 0, P)$

Useful quantities:



Electron momentum transfer

$$Q^2 = -q^2 = -(k - k')^2$$

Total energy in $\gamma^* p$ center of mass

 $= \frac{q \cdot P}{k \cdot p}$

Inelasticity

$$W^2 = (q+P)^2$$

Bjorken scaling variable





Kinematics: Lab frame

Often DIS kinematics expressed in LAB frame (target at rest) \rightarrow Experiments at HERA (or a future EIC) take place in collider

I tend to think in a fixed-target framework – some useful expressions for working in the lab:

$$x = \frac{Q^2}{2p \cdot q} \rightarrow \frac{Q^2}{2m_p\nu} \qquad \nu = E - E'$$
$$W^2 = (q+P)^2 \rightarrow -Q^2 + m_p^2 + 2m_p\nu$$

$$\begin{split} y &= \frac{q \cdot P}{k \cdot P} \to \frac{\nu}{E} & \text{Fraction of electron energy transferred to nucleon} \\ \epsilon &= \left(1 + \frac{2|\mathbf{q}|^2}{Q^2} \tan \frac{\theta_e}{2}^2\right)^{-1} = \frac{1 - y}{1 - y + \frac{1}{2}y^2} & \text{Ratio of long. to} \\ \text{ferson Lab} & \text{flux} & 8 \end{split}$$



$$\frac{d\sigma}{d\Omega dE'} = \frac{4\alpha^2 (E')^2}{Q^4} \left[W_2(\nu, Q^2) \cos^2 \frac{\theta}{2} + 2W_1(\nu, Q^2) \sin^2 \frac{\theta}{2} \right]$$

 W_1 and W_2 parameterize the (unknown) structure of the proton





In the limit of large Q², structure functions scale

$$MW_1(v,Q^2) \to F_1(x) \qquad x = \frac{Q^2}{2Mv}$$
$$VW_2(v,Q^2) \to F_2(x) \qquad x = \frac{Q^2}{2Mv}$$





Transverse and longitudinal



$$\frac{d\sigma}{d\Omega dE'} = \frac{4\alpha^2 (E')^2}{Q^4} \left[W_2(v,Q^2)\cos^2\frac{\theta}{2} + 2W_1(v,Q^2)\sin^2\frac{\theta}{2} \right]$$

Replacing W_1 and W_2
 $WW_1(v,Q^2) \rightarrow F_1(x,Q^2)$
 $vW_2(v,Q^2) \rightarrow F_2(x,Q^2)$

And defining:

$$F_L(x,Q^2) = \left(1 + \frac{4M^2x^2}{Q^2}\right)F_2(x,Q^2) - 2xF_1(x,Q^2)$$

$$\frac{d\sigma}{d\Omega dE'} = \Gamma \frac{4\pi^2 \alpha}{x(W^2 - M^2)} \left[2xF_1(x, Q^2) + \epsilon F_L(x, Q^2) \right]$$





At very high energies (HERA) – contributions from Z exchange can no longer be ignored

$$\frac{d\sigma^{e^{\pm}}}{dxdQ^{2}} = \frac{2\pi\alpha^{2}(1+(1-y)^{2})}{Q^{4}x} \left[\tilde{F}_{2} \mp \frac{1-(1-y)^{2}}{1+(1-y)^{2}}x\tilde{F}_{3} - \frac{y^{2}}{1+(1-y)^{2}}\tilde{F}_{L}\right]$$

$$\tilde{F}_{2} = F_{2} - \kappa_{Z}v_{e}F_{2}^{\gamma Z} + \kappa_{Z}^{2}(v_{e}^{2} + a_{e}^{2})F_{2}^{Z}$$

$$\tilde{F}_{L} = F_{L} - \kappa_{Z}v_{e}F_{L}^{\gamma Z} + \kappa_{Z}^{2}(v_{e}^{2} + a_{e}^{2})F_{L}^{Z}$$

$$x\tilde{F}_{3} = -\kappa_{Z}a_{e}xF_{3}^{\gamma Z} + \kappa_{Z}^{2}2v_{e}a_{e}xF_{3}^{Z}$$

$$r_{Z} = \frac{Q^{2}}{Q^{2} + M_{Z}^{2}}\frac{1}{4\sin\theta_{W}^{2}\cos\theta_{W}^{2}}$$
Vector weak

$$=-1/2 + 2\sin^{2}\theta_{W}$$
Axial-vector weak

$$=-1/2 + 2\sin^{2}\theta_{W}$$

$$\tilde{F}_{3} = -\kappa_{Z}a_{e}xF_{3}^{2}$$

=-1/2+2sin² θ_{W}

coupling

Quark Parton Model

DIS can be described as inelastic scattering from noninteracting, point-like constituents in the nucleon

Consequences:

At fixed x, inelastic structure functions scale:

$$MW_1(v,Q^2) \to F_1(x)$$

$$VW_2(v,Q^2) \to F_2(x)$$
Large Q²

$$F_2(x) = \sum_i e_i^2 x q_i(x)$$
 $F_2(x) = 2x F_1(x)$ Spin ½:
Callan-Gross relation
 $R = \frac{\sigma_L}{\sigma_T} = 0$

Quark Parton Model

DIS can be described as inelastic scattering from noninteracting, point-like constituents in the nucleon

$$F_{2}(x) = \sum_{q} e_{q}^{2} x(q(x) + \bar{q}(x))$$

$$g_{V}^{q} = \pm \frac{1}{2} - 2e_{q} \sin \theta_{W}^{2}$$

$$F_{2}^{\gamma Z}(x) = \sum_{q} 2e_{q}g_{V}^{q} x(q(x) + \bar{q}(x))$$

$$F_{2}^{Z}(x) = \sum_{q} [(g_{V}^{q})^{2} + (g_{A}^{q})^{2}]x(q(x) + \bar{q}(x))$$

$$F_{3}^{\gamma Z}(x) = \sum_{q} 2e_{q}g_{A}^{q}(q(x) - \bar{q}(x))$$

$$F_{3}^{Z}(x) = \sum_{q} [(g_{V}^{q})^{2} + (g_{A}^{q})^{2}](q(x) - \bar{q}(x))$$

 \boldsymbol{q}



Scaling – SLAC-MIT result from 1970

A series of experiments at SLAC (performed by SLAC-MIT collaboration) gave first hints that the partonic hypothesis was valid

- → Cross sections at large angles (momentum transfers) larger than if proton was an amorphous blob-like object
- \rightarrow Analogous to Rutherford's alpha scattering experiments

We observe the excitation of several nucleon resonances⁴⁻⁷ whose cross sections fall rapidly with increasing q^2 . The region beyond $W \approx 2$ GeV exhibits a surprisingly weak q^2 dependence. This Letter describes the experimental procedure and reports cross sections for $W \ge 2$ GeV. Discussion of the results and a detailed description of the resonance region will follow.⁸

Phys.Rev.Lett. 23 (1969) 930-934



Beam energy up to $\sim 20 \text{ GeV}$



Scaling – SLAC-MIT result from 1970

A series of experiments at SLAC (performed by SLAC-MIT collaboration) gave first hints that the partonic hypothesis was valid



SLAC-PUB 796 (1970)





SLAC-MIT also performed initial L-T separations, suggesting *R* was not large \rightarrow L-T separations experimentally challenging – precise extractions came later



Phys.Rev. D5 (1972) 528



Phys.Rev.Lett. 61 (1988) 1061

QPM and QCD

The quark parton model is the asymptotic limit of the real theory of strong interactions \rightarrow QCD

- In reality structure functions (and parton distributions) are not Q² independent – even for large values of Q²
- Struck quark radiates hard gluons leads to logarithmic Q² dependence

 Q^2 evolution can be described by DGLAP equations:

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Non singlet quark distributions:
$$q^{NS} = q - \bar{q}$$

$$\frac{dq^{NS}(x,Q^2)}{d\ln Q^2} = \frac{\alpha_s}{2\pi} \int_x^1 \frac{dy}{y} q^{NS}(y,Q^2) P_{qq}(\frac{x}{y})$$
Gluon quark singlet distributions: $q^S = \sum_i q_i + \bar{q}_i$

$$\frac{d}{d\ln Q^2} \begin{pmatrix} q^S(x,Q^2) \\ G(x,Q^2) \end{pmatrix} = \frac{\alpha_s}{2\pi} \int_x^1 \frac{dz}{z} \begin{pmatrix} P_{qq}(z) & N_f P_{qG}(z) \\ P_{Gq}(z) & P_{GG}(z) \end{pmatrix} \begin{pmatrix} q^S(\frac{x}{z},Q^2) \\ G(\frac{x}{z},Q^2) \end{pmatrix}$$

DGLAP = Dokshitzer-Gribov-Lipatov-Altarelli-Parisi

Q^2 Dependence of F_2

- Overall, Q² dependence of F₂ well-described by NLO DGLAP evolution
- Note that near x=0.1-0.2, the Q² dependence is rather small → early SLAC measurements
- At small *x*, *Q*² dependence becomes quite large





Q² Dependence of PDFs



K.A. Olive et al. (Particle Data Group), Chin. Phys. C, 38, 090001 (2014).

DGLAP evolution allows us to use measurements at an arbitrary scale and evolve them to another \rightarrow PDFs not scale independent



Experimental Challenges - Kinematics

Large *x* typically pursued at fixed target machines

- → Can reach large Q², but need large luminosities
- → Large energies required to avoid resonance region at largest *x*





Colliders excellent for accessing smallest values of *x*

 \rightarrow As x shrinks, ever increasing energies needed to achieve even modest Q² range

Experimental Challenges - Radiative Corrections

Radiative corrections pose additional experimental challenge for the analysis of DIS data

→ Reliable RC requires knowledge of the process of interest over a wide kinematics region since events can "radiate in" to the acceptance



d) Bremsstrahlung

e) Multi–Photon Emission



Other processes (elastic scattering) can also contribute to experimental yield



Figures from V. Tvaskis (PhD Thesis)

Radiative Corrections

Radiative effects can be broken into 2 contributions:

- Radiation in field of nucleus from which electron scatters → Internal
- Radiation if field of other nuclei → External

External typically only an issue for fixed target experiments



Cross sections must be extracted iteratively – updating the "Born E' (GeV) model" at every iteration

 \rightarrow In the end, the need to avoid large radiative corrections can limit kinematic reach

Typical requirement: y<0.85



Figures from V. Tvaskis (PhD Thesis)

Polarized DIS

In addition to unpolarized structure functions, polarized targets and beams are sensitive to polarized structure functions: $g_1(x)$ and $g_2(x)$

Longitudinally polarized target, longitudinally polarized beam:

$$\frac{d\sigma}{d\Omega dE'}(\downarrow\uparrow-\uparrow\uparrow) = \frac{4\alpha^2}{MQ^2}\frac{E'}{\nu E}\left[(E+E'\cos\theta)g_1(x,Q^2) + \frac{Q^2}{\nu}g_2(x,Q^2)\right]$$

Transversely polarized target, longitudinally polarized beam:

$$\frac{d\sigma}{d\Omega dE'}(\downarrow \to -\uparrow \to) = \frac{4\alpha^2 \sin\theta}{MQ^2} \frac{E'^2}{\nu^2 E} \left[\nu g_1(x,Q^2) + 2Eg_2(x,Q^2)\right]$$



g₁ in Quark Parton Model

In QPM, g_1 is weighted sum of polarized quark distributions

$$F_{1}(x) = \frac{1}{2} \sum_{i} e_{i}^{2} q_{i}(x) \qquad g_{1}(x) = \frac{1}{2} \sum_{i} e_{i}^{2} \Delta q_{i}(x)$$
Unpolarized
$$\Delta q(x) = q^{\uparrow}(x) - q^{\downarrow}(x)$$
parallel to
target spin
antiparallel



World data* on F_2 and g_1





Great increase in amount of data on g_1 in recent years – sill not even close to F_2

, *COMPASS data on g_1 missing

Quark contribution to spin of the nucleon

Using quark parton model, g_1 of proton and neutron, can extract quark contribution to nucleon spin

$$\Delta q = \int_0^1 dx \Delta q(x)$$

EMC (*Phys. Lett. B* **206** (2): 364) estimated quark contribution to spin of proton to be (assuming $\Delta s = 0$)

$$\Delta\Sigma$$
=0.14 ± 0.09 (stat) +/- 0.21 (sys)

Spin Crisis!



More recent HERMES result (Phys. Rev. D 75 (2007) 012007)

 $\Delta\Sigma$ =0.330 ± 0.011(theo.) ± 0.025(exp.) ± 0.028(evol.)



g₂ Polarized Structure Function

 g_2 does not have a simple interpretation in the Quark Parton Model

 \rightarrow Can be written as a sum of 2 terms

$$g_2(x,Q^2) = g_2^{WW}(x,Q^2) + \bar{g}_2(x,Q^2)$$

Twist-2 term (Wandzura and Wilczek)

$$g_2^{WW}(x,Q^2) = -g_1(x,Q^2) + \int_x^1 g_1(x,Q^2) \frac{dy}{y}$$

Twist-3 + Twist-2

$$\bar{g}_2(x,Q^2) = -\int_x^1 \frac{\partial}{\partial y} \left[\frac{m_q}{M} h_T(y,Q^2) + \xi(y,Q^2)\right] \frac{dy}{y}$$

Quark gluon correlations



g₂Spin Structure Function

New measurements from JLAB

 $x^2g_2^p$ Proton – Hall C



Second moment of \overline{g}_2

 d_2 moment directly sensitive to "interesting" part of g_2

$$d_2 = \int_0^1 dx x^2 [3g_2(x) + 2g_1(x)] = 3 \int_0^1 dx x^2 \bar{g}_2(x)$$

Neutron



Jellei Juli Lau

DIS at Large x

- At large *x*, cross sections are small \rightarrow low rates
 - High luminosity required historically the purview of fixed-target facilities
- Moderate energies available at high luminosity, fixed target accelerators implies moderate Q² measurements at sometimes rather low W
 - In this kinematic regime, so-called target mass corrections can be important
- Additional complication comes about in extraction of neutron cross sections and structure functions
 - Nuclear effects



Target Mass Corrections

 $x = \frac{Q^2}{2p \cdot a}$ For massless quarks and targets (or $Q^2 \rightarrow \infty$) Bjorken scaling variable is the light-cone momentum fraction of target carried by parton

Finite Q², light-cone momentum fraction given by Nachtmann variable

$$\xi = \frac{2x}{1 + \sqrt{1 + 4x^2 M^2 / Q^2}}$$

A prescription for target mass corrections can be derived in terms of the Operator Product Expansion and moments of the structure functions → Result is "master equation"

$$F_2^{TMC}(x,Q^2) = \frac{x^2}{\xi^2 r^3} F_2^{(0)}(\xi,Q^2) + \frac{6M^2 x^3}{Q^2 r^4} h_2(\xi,Q^2) + \frac{12M^4 x^4}{Q^4 r^5} g_2(\xi,Q^2)$$

Weighted integrals over $F_2^{(0)}$

Target Mass Corrections





Effects of target mass corrections can be quite large – highly Q² dependent

J. Phys. G: Nucl. Part. Phys. 35 (2008) 053101 34

Neutron Structure Functions

 Structure function information from the neutron is crucial for understanding the quark structure of nucleons

$$\frac{F_2^n}{F_2^p} = \frac{1 + 4d_v(x)/u_v(x)}{4 + d_v(x)/u_v(x)}$$

 No free neutron targets – typically deuterium targets are used and the very simple approximation is used:

$$F_2^D = F_2^p + F_2^n$$

- At low x (x<0.3), nuclear effects are small this approximation introduces minimal error
- At larger x, this assumption becomes increasingly incorrect



CJ12 PDFs

Nuclear effects in deuteron lead to significant uncertainties in quark PDFs at large *x*

 \rightarrow This has been studied in some depth by the CTEQ-JLAB collaboration



J. F. Owens, A. Accardi and W. Melnitchouk, Phys. Rev. D 87, 094012 (2013)



Extraction of Neutron Structure Functions



Early extraction of the *n/p* ratio tried to incorporate a model including corrections for Fermi smearing

For example, see: Phys.Rev. D20 (1979) 1471-1552

Bodek et al., Phys. Rev. Lett. 30, 1087 (1973) E. M. Riordan et al., Phys. Rev. Lett. 33, 561 (1974) J. S. Poucher et al., Phys. Rev. Lett. 32, 118 (1974).

Extraction of Neutron Structure Functions



Figure from JLab proposal E12-10-103

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Bodek et al., Phys. Rev. Lett. 30, 1087 (1973) E. M. Riordan et al., Phys. Rev. Lett. 33, 561 (1974) J. S. Poucher et al., Phys. Rev. Lett. 32, 118 (1974).

BONUS – d/u via Spectator Tagging

BONUS = Barely Offshell Neutron Scattering

Minimize nuclear effects by measuring DIS cross section from neutrons with low Fermi momentum \rightarrow Tag low momentum "spectator" protons at backward angles; struck neutron almost on-shell







Future Measurements of d/u



JLAB-12 GeV will allow extraction of d/u using a variety of techniques

- 1. Spectator tagging (BONUS)
- 2. PVDIS
- 3. Mirror nuclei ³H/³He



Transition to the perturbative regime

- DIS often viewed as simply a "tool" to gain access to parton distributions in the perturbative regime
- Understanding the transition to this regime is also of key interest, and one of the reasons JLab was built

CEBAF's original mission statement

Key Mission and Principal Focus (1987): The study of the largely unexplored transition between the nucleon-meson and the quark-gluon descriptions of nuclear matter.



The Strong Force at Long and Short Distances





The Quark Parton Model is well defined in the limit of large Q² and large υ (or W²). Empirically, deep inelastic scattering (or quark parton model) descriptions seem to work well down to modest energy scales: Q² ~ 1 GeV², W² ~ 4 GeV².

Why is the Quark-Hadron Transition in QCD so smooth, and occurring at such low energy scales?

The underlying reason is the Quark-Hadron Duality phenomenon.



Quark Hadron Duality At high enough energy:

Hadronic Cross Sections averaged over appropriate energy range

Perturbative Quark-Gluon Theory



Can use either set of complete basis states to describe physical phenomena

In different energy regimes one description is more "economical" than the other: how can we understand the transition between these 2 regimes?



Duality in the F₂ Structure Function

- First observed ~1970 by Bloom and Gilman at SLAC by comparing resonance production data with deep inelastic scattering data
- Integrated F₂ strength in Nucleon Resonance region equals strength under scaling curve. Integrated strength (over all ω') is called Bloom-Gilman integral

Shortcomings:

- Only a single scaling curve and no Q² evolution (Theory inadequate in pre-QCD era)
- No σ_L/σ_T separation \rightarrow F₂ data depend on assumption of R = σ_L/σ_T
- Only moderate statistics





Quark-Hadron Duality

- In the late 90s, a large body of data in the resonance region was acquired at JLab
- High statistics, large phase space allowed the examination of duality with high precision
- Most interesting duality was observed to hold even when looking at individual resonances above Q²=1-2 GeV²!

I. Niculescu et al., PRL85:1182 (2000)





Duality in Separated Structure Functions



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The resonance region is, on average, well described by NNLO QCD fits for separated structure functions as well.

This implies that Higher-Twist (FSI) contributions cancel, and are on average small. "Quark-Hadron Duality"

The result is a smooth transition from Quark Model Excitations to a Parton Model description, or a smooth quark-hadron transition.

This explains the success of the parton model at relatively low W^2 (=4) GeV^2) and Q^2 (=1 GeV^2).

Duality Summary

- In addition to unpolarized proton structure functions, duality has been observed to manifest for:
 - Neutron structure functions
 - Asymmetries $(A^{p}_{1} \text{ and } A^{n}_{1})$
 - Semi-inclusive DIS (SIDIS)
- Other duality-like manifestations
 - Approach to scaling of charged pion form-factor
 - Scaling of deep-exclusive reactions
- The dual nature of these reactions (globally) is not so surprising – its *required*
- But why does it work so well *locally*?
 - Experimentally, we may have done as much as we can need new theoretical insight to understand the detailed behavior



Summary – Part 1

- Deep Inelastic Scattering is a powerful tool for probing the quark-gluon structure of nucleons
- DIS gave us first evidence that the partonic picture of the nucleon was accurate
- Since then, unpolarized and polarized DIS has provided a huge body of data that has constrained PDFs
 - Polarized data not yet achieved same kinematic reach and coverage as unpolarized
- While DIS itself is useful understanding the transition from the non-perturbative to the perturbative regime is a key issue
- What about the 3D structure of nucleons?







Quark Flavor Dependent Effects on Proton

• Measurement of d(x)/u(x) ratio for the proton at high x

$$a_1^p(x) \sim rac{u(x) + 0.912d(x)}{u(x) + 0.25d(x)}$$

- ► A clean measurement free from any nuclear corrections
- Uncertainties of set of PVDIS measurements are shown in the plot (red dots)
 - Provides high precision measurements in range of x





