

Thia Keppel
CTEQ Summer School



Lecture Scheme

in·ter·face

'in(t)ərˌfās/ *noun*

1. a point where two systems, subjects, etc., meet and interact.

DAY 1

- Introduction
- History and Basics of Electron Scattering – *Some Reminders*
- Jefferson Lab
- 1D to 3D Nucleon Structure
 - Form Factors and PDFs
 - Large x
- Nucleons in the Nuclear Medium

DAY 2

- *Finish What I Didn't Yet From Day 1!*
- The Electron Ion Collider



Particle and Nuclear Physics - Related Questions

HOW DID OUR UNIVERSE BEGIN?

Some 13.8 billion years ago, our entire visible universe was contained in an unimaginably hot, dense point, the size of a marble. Since then it has expanded—defying gravity all the way.

Inflation
In the first fraction of a second, space expanded faster than the speed of light. The universe grew from a size smaller than a proton to the size of a grapefruit.

Steady building blocks
The universe expanded, cooled, and particles began to form. First came quarks, then protons and neutrons, and finally atoms.

First nuclei
As the universe cooled, the first nuclei of hydrogen and helium formed. This process is called nucleosynthesis.

First atoms, first light
As electrons began orbiting nuclei, the universe became transparent. This is the Cosmic Microwave Background radiation.

The "dark ages"
For 380,000 years, the universe was dark and cold. Only the faint glow of the Cosmic Microwave Background radiation was visible.

Gravity wins: first stars
Dense gas clouds collapsed under their own gravity and stars were born. The first stars were massive and short-lived.

Antigravity wins
After being slowed for billions of years by gravity, cosmic expansion accelerated again. The universe is now expanding at an ever-increasing rate.

Today
The universe continues to expand, becoming ever less dense. As a result, new stars and galaxies are forming.

HOW WILL IT END?

Which will win in the end, gravity or antigravity? It seems unlikely—especially given the power of dark energy, a kind of antigravity. Perhaps the acceleration in expansion caused by dark energy will trigger a big rip that shreds everything, from galaxies to atoms. If not, the universe may expand for hundreds of billions of years, long after all stars have died.



COSMIC QUESTIONS

In the 20th century the universe became a story—a scientific one. It had always been seen as static and eternal. Then astronomers observed other galaxies flying away from ours, and Einstein's general relativity theory implied space itself was expanding—which meant the universe had once been denser. What had seemed eternal now had a beginning and an end. But what beginning? What end? Those questions are still open.

WHAT IS OUR UNIVERSE MADE OF?

Stars, dust, and gas—the stuff we can discern—make up less than 5 percent of the universe. Their gravity can't account for how galaxies hold together. Scientists figure about 24 percent of the universe is a mysterious dark matter—perhaps exotic particles formed right after inflation. The rest is dark energy, an unknown energy field or property of space that counteracts gravity, providing an explanation for observations that the expansion of space is accelerating.



WHAT IS THE SHAPE OF OUR UNIVERSE?

Einstein discovered that a star's gravity curves space around it. But is the whole universe curved? Might space close up on itself like a sphere or curve the other way, opening out like a saddle? By studying cosmic background radiation, scientists have found that the universe is poised between the two; just dense enough with just enough gravity to be almost perfectly flat, at least the part we can see. What lies beyond we can't know.



DO WE LIVE IN A MULTIVERSE?

What came before the big bang? Maybe other big bangs. The uncertainty principle holds that even the vacuum of space has quantum energy fluctuations. Inflation theory says our universe exploded from such a fluctuation—a random event that, odds are, had happened many times before. Our cosmos may be one in the sea of others just like ours—or nothing like ours. These other cosmos will very likely remain forever inaccessible to observation; their possibilities limited only by our imagination.



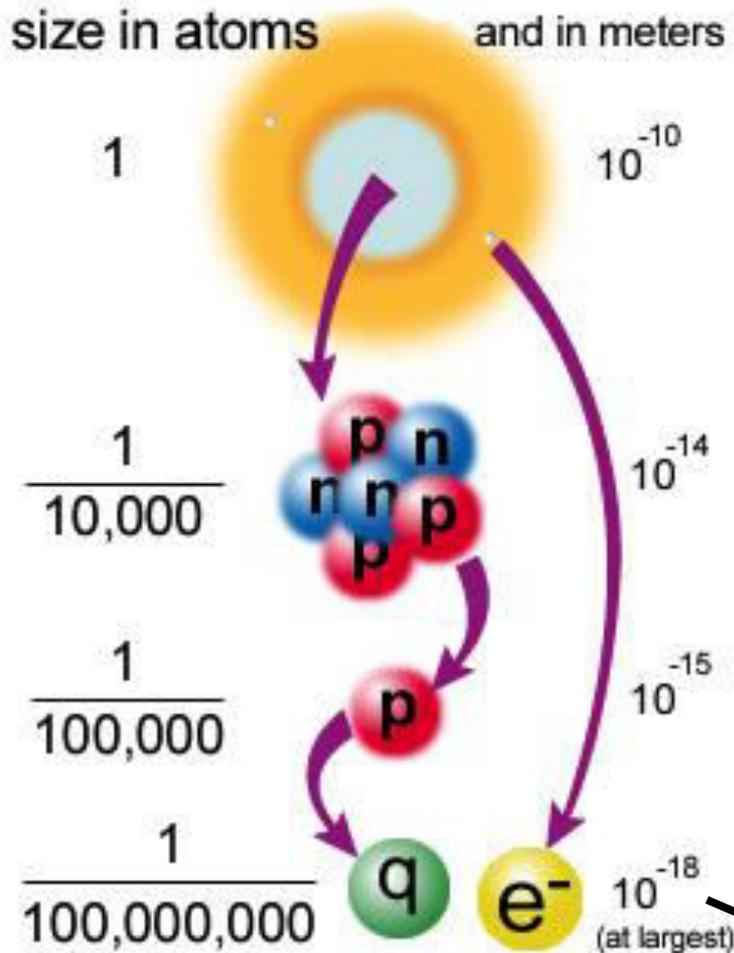
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Nuclear Physics Seeks to:

- Understand the fundamental structure of visible matter (quarks, gluons,..)
- Understand how hadrons (mesons, nucleons,..) and nuclei are formed

How to probe the nucleons / quarks?



- Electron/lepton scattering experiments employ high momentum point-like leptons, + electromagnetic interactions, **which are well understood**, to probe hadronic structure **(which isn't)**.

High energy electrons are a great tool for the job!



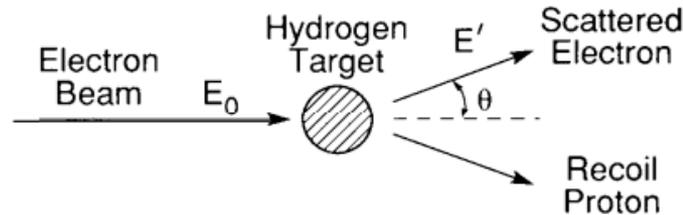
short distance \rightarrow large momentum
(Uncertainty Principle!)

$$d_{\text{probed}} \propto \tilde{\lambda} = \frac{\hbar}{p} \approx 10^{-18} \text{ m}$$

Simplest Nucleus: Is the Proton Point-Like?

➤ Do **protons** have size?

1948-50 – Schiff, Rosenbluth: suggest use of **elastic electron-proton scattering** to probe the proton



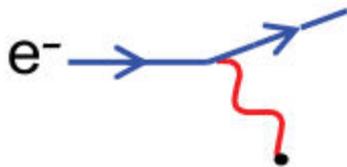
$$q = (E_0 - E', \vec{q})$$

$$E' = \frac{E_0}{1 + \frac{2E_0}{M} \sin^2 \frac{\theta}{2}}$$

electron is left with less energy after meeting the proton

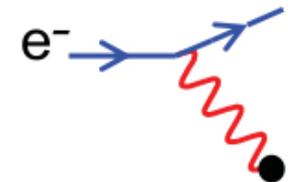
$$Q^2 = 4E_0 E' \sin^2 \frac{\theta}{2}$$

square of four-momentum transfer: connected to the probe's ability of resolving the structure of the proton



probe's ability of resolving structure $\sim \frac{\hbar}{Q}$

proton when $\frac{\hbar}{Q} \gg$ than its size

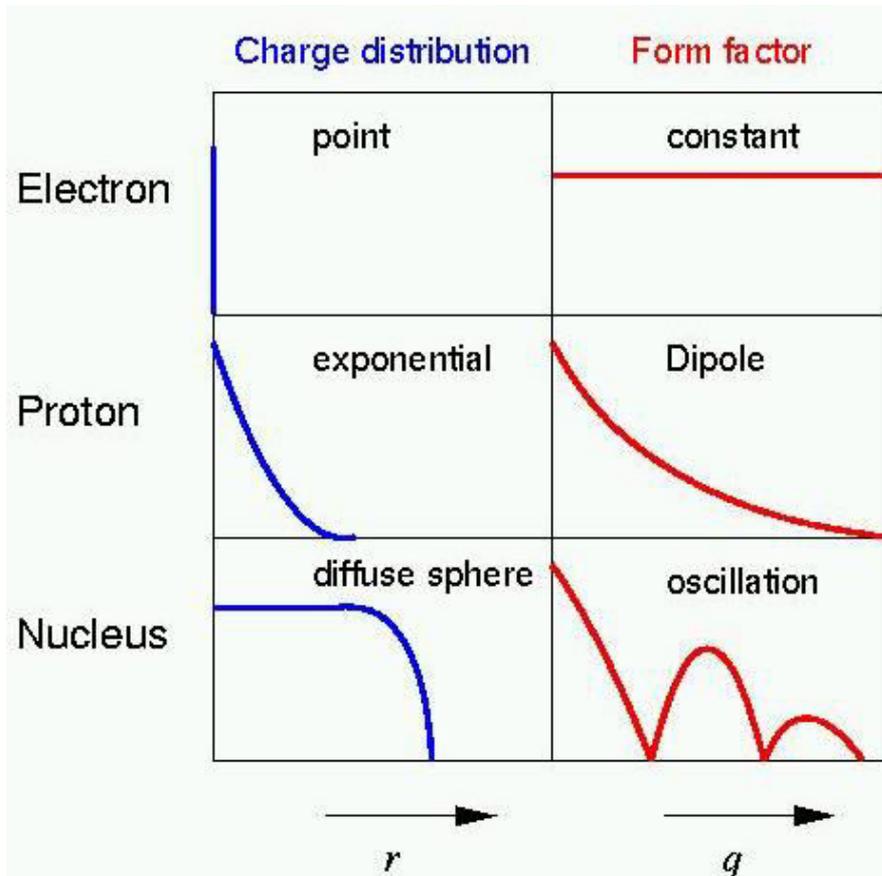


same proton when $\frac{\hbar}{Q} \sim$ its size

Charge and Magnetic Moment Distributions

Probability of elastic interaction: $\frac{d\sigma}{d\Omega} / \left(\frac{d\sigma}{d\Omega}\right)_{point} = \left[\frac{G^2_E(Q^2) + \tau G^2_M(Q^2)}{1 + \tau} + 2\tau G^2_M(Q^2) \tan^2 \frac{\theta}{2} \right] \quad \tau = \frac{Q^2}{4M^2}$

- Form Factors are (in some limit) Fourier transforms of charge and magnetic moment distributions



- ▶ Elastic cross section

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{exp}} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} |F(q^2)|^2$$

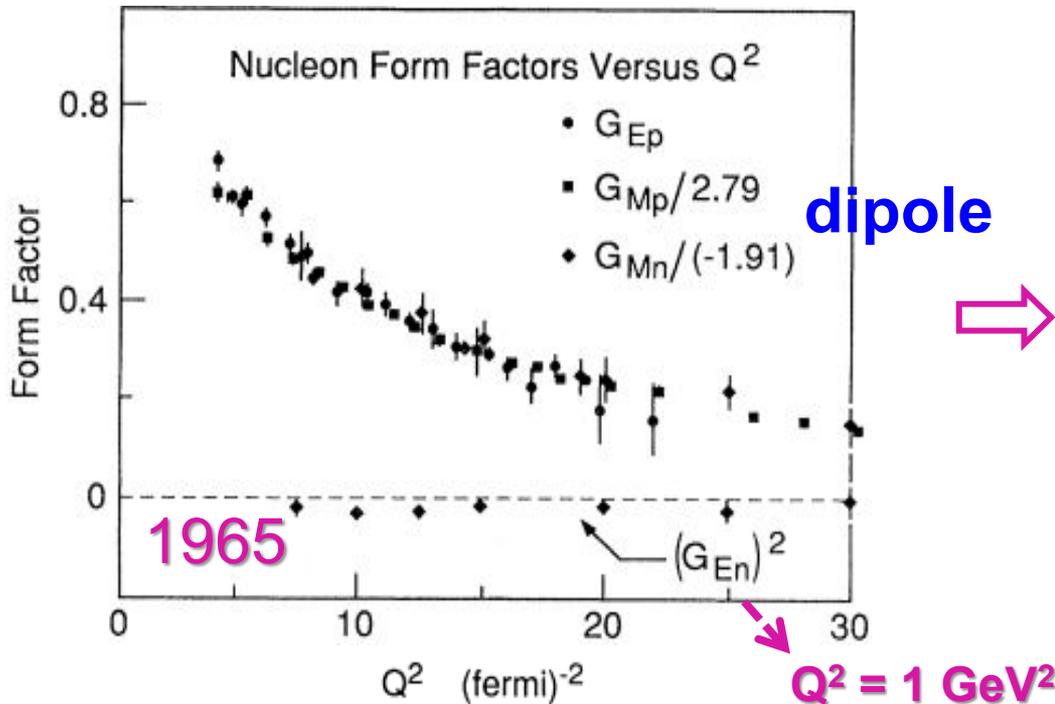
- ▶ Form factor

$$F(q^2) = \int e^{iqx/\hbar} \rho(x) d^3x$$

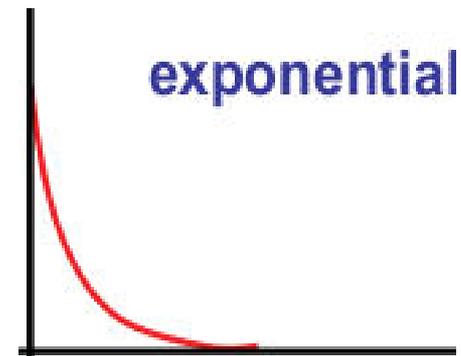
How Do the Charge and Magnetic Moment Distribute?

Probability of elastic interaction: $\frac{d\sigma}{d\Omega} / \left(\frac{d\sigma}{d\Omega} \right)_{point} = \left[\frac{G^2_E(Q^2) + \tau G^2_M(Q^2)}{1 + \tau} + 2\tau G^2_M(Q^2) \tan^2 \frac{\theta}{2} \right] \quad \tau = \frac{Q^2}{4M^2}$

- The Q^2 dependence of form factors was measured...



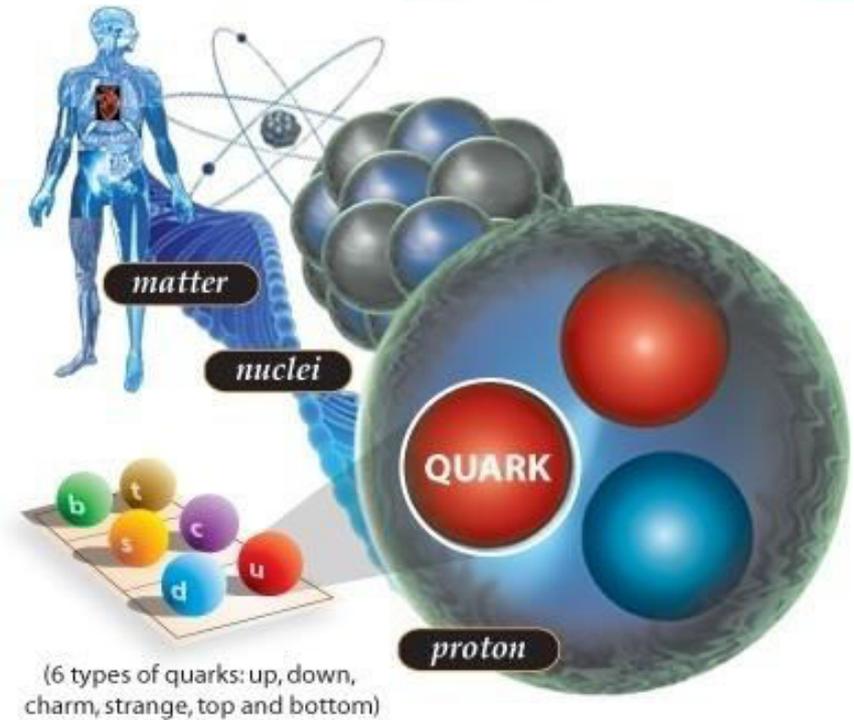
Distribution of Charge or Magnetic Moment



Caveat: The Form Factor as the Fourier transformation of a charge distribution is a non-relativistic concept.

Actually, highly relativistic...

- Protons and neutrons swirl in a heavy atomic nucleus with speeds of **up to some $\frac{3}{4} c$** . More commonly, their speed is some $\frac{1}{4}$ the speed of light. They are “strong-forced” to reside in a small space.

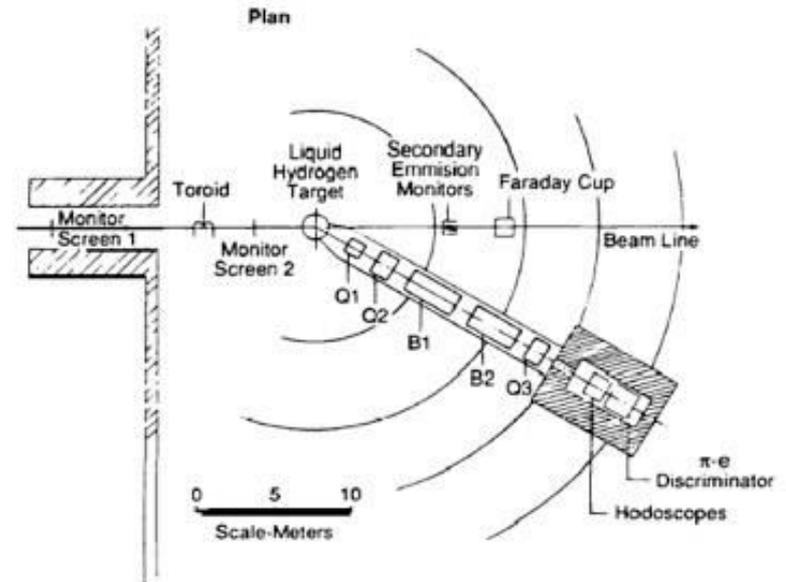
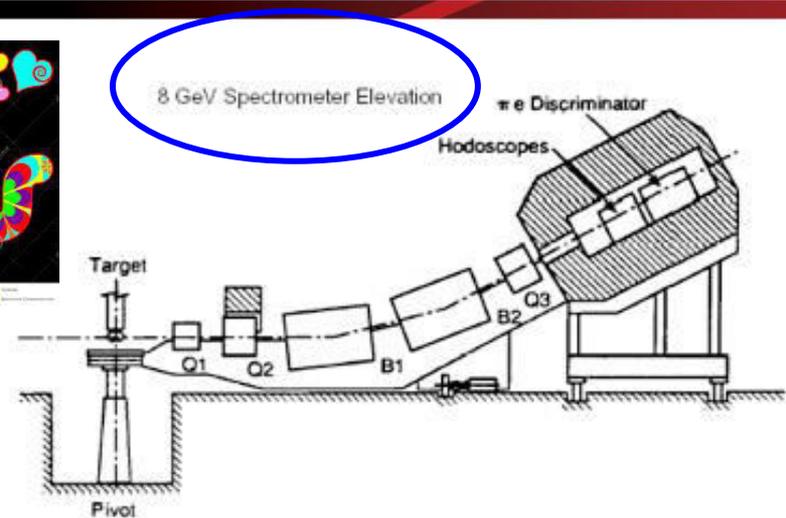


- Quarks (and gluons) are “confined” to the even smaller space inside protons and neutrons. Because of this, they swirl around with **the speed of light**.

Higher energy e-p and e-d elastic scattering at SLAC



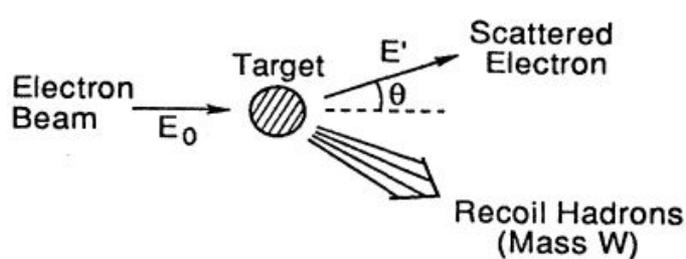
J. Friedman, H. Kendall, R. Taylor
Nobel Prize 1990



Matter Puzzle: What's Inside the Proton?

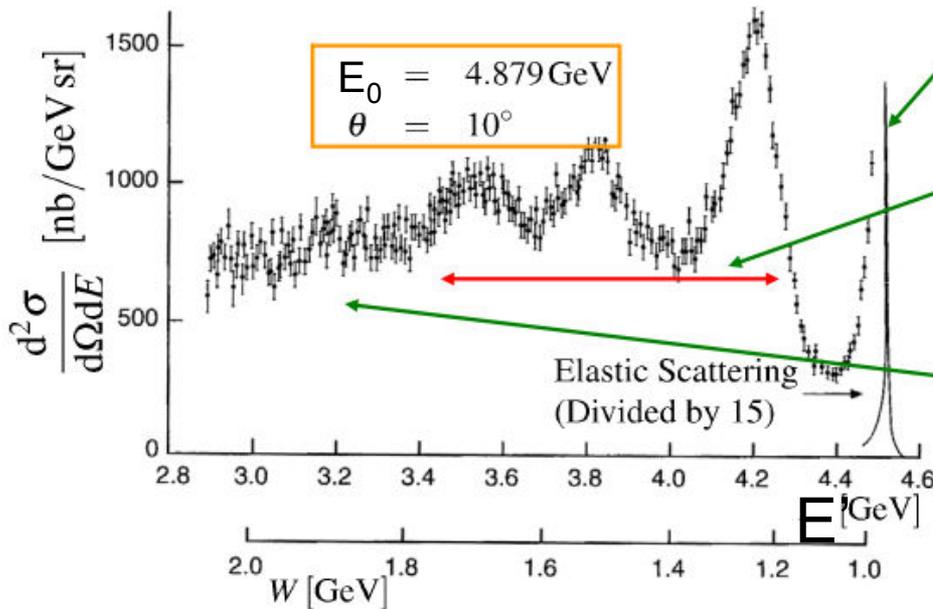
➤ Is the **proton elementary**?

To find out increase the probe's ability of resolving structure (decrease $\frac{\hbar}{Q}$)



$$E' = \frac{E_0 - \frac{W^2 - M^2}{2M}}{1 + \frac{2E_0}{M} \sin^2 \frac{\theta}{2}} \quad \nu = E_0 - E' \quad y = \frac{\nu}{E_0} \quad x = \frac{Q^2}{2M\nu}$$

$$W^2 = M^2 + 2M\nu - Q^2$$



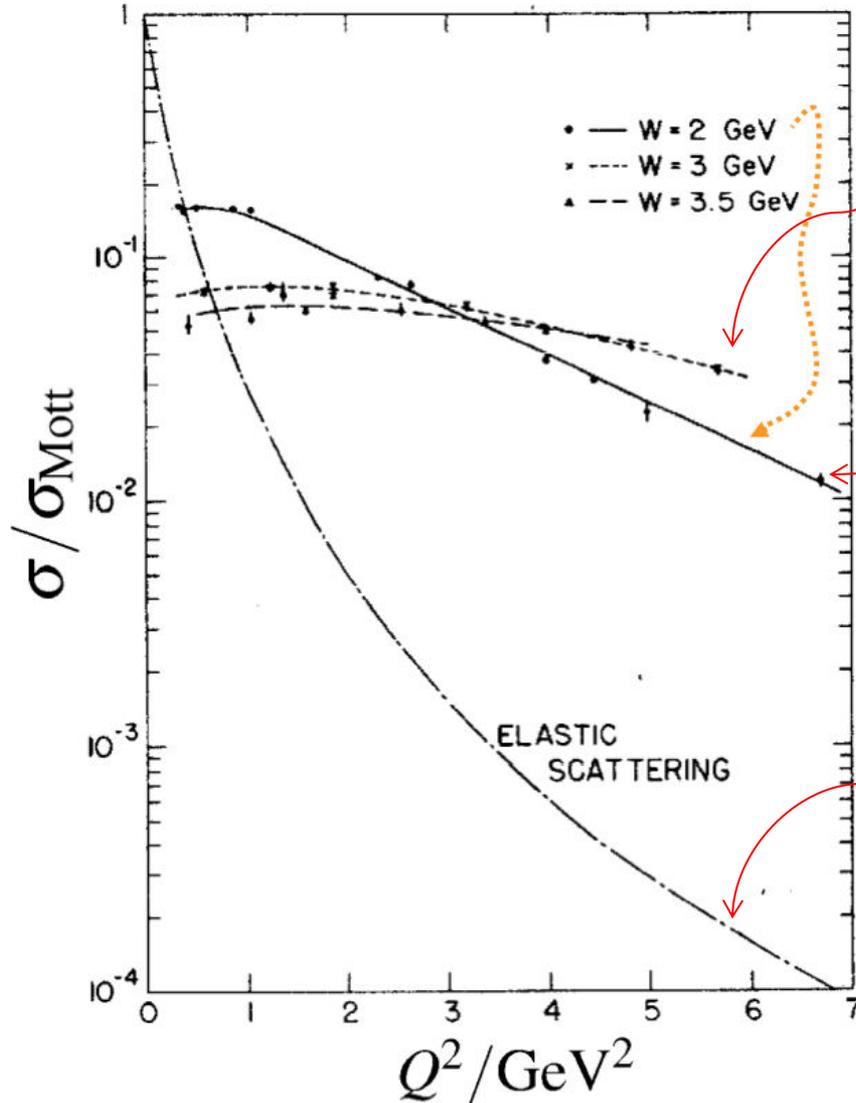
Elastic scattering: proton stays intact, $W = M$

Inelastic scattering: proton gets excited, produce excited states or proton's resonances, $W = M_{resonance}$

Deep inelastic scattering: proton breaks up and we end up with a many particle final state, $W = \text{large}$

Looking deep inside the Proton

M. Breidenbach et al.,
Phys. Rev. Lett. 23 (1969) 935



- **Deep Inelastic scattering** cross sections almost independent of Q^2 !
i.e. "Form factor" $\rightarrow 1$

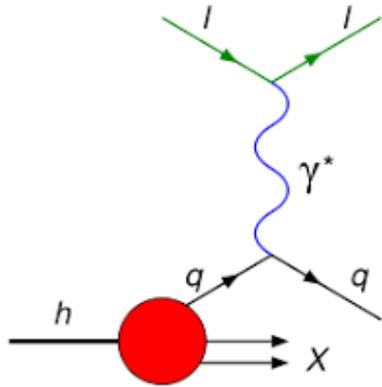
Scattering off point-like objects within the proton

- **Inelastic scattering** cross sections only weakly dependent on Q^2

- **Elastic scattering** falls off rapidly with Q^2 due to the proton not being point-like (i.e. form factors)

$$\frac{\sigma}{\sigma_{\text{Mott}}} = \left(\frac{1}{(1 + Q^2/0.71)^2} \right)^2 \propto Q^{-8}$$

Structure Functions in Deep Inelastic Electron-Nucleon Scattering

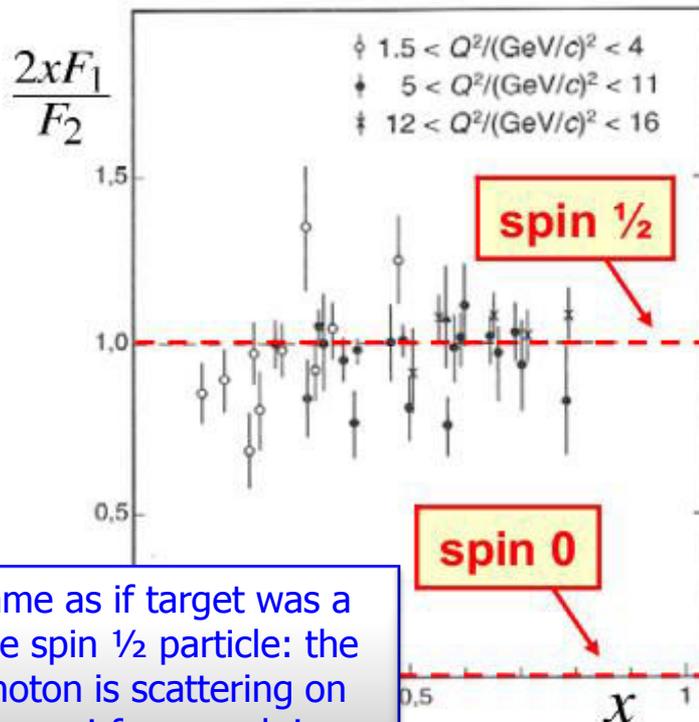


Probability of **inelastic** interaction:

$$\frac{d^2\sigma}{d\Omega dE'} = \frac{\alpha^2}{4E_0^2 \sin^4 \frac{\theta}{2}} \cos^2 \frac{\theta}{2} \left[\frac{1}{v} F_2(x, Q^2) + \frac{2}{M} F_1(x, Q^2) \tan^2 \frac{\theta}{2} \right]$$

Unpolarized “*Structure Functions*”
 $F_1(x, Q^2)$ and $F_2(x, Q^2)$:

- Account for the sub-structure of the protons and neutrons
- x = fraction of nucleon momentum carried by struck quark
- Give access to *partonic structure* of the nucleon, i.e.

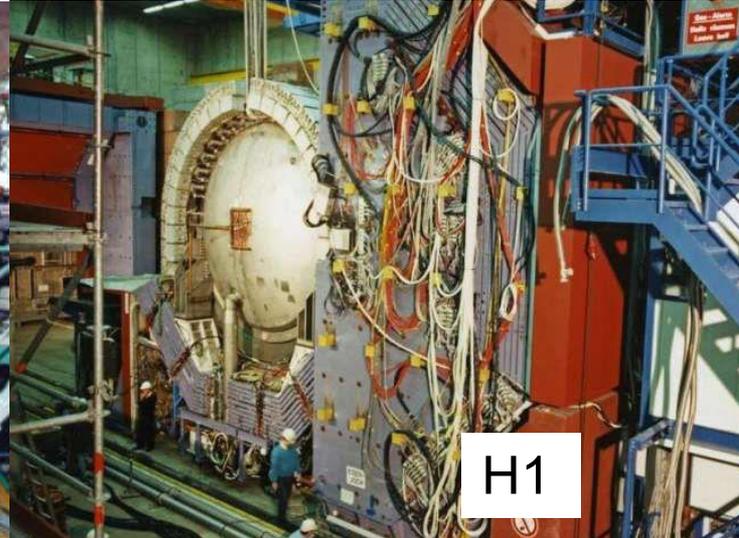
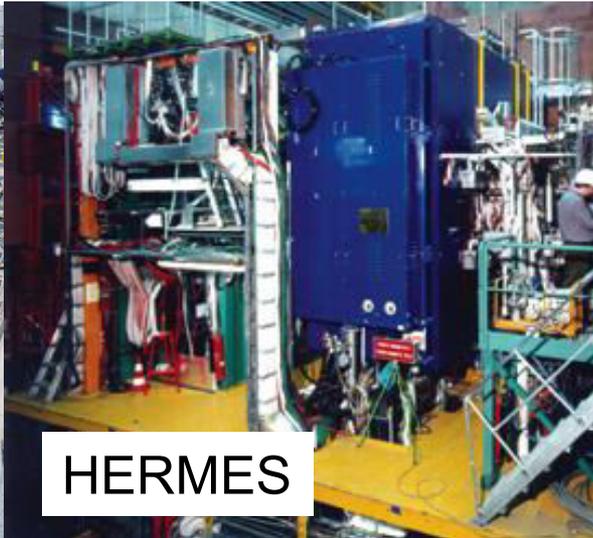


$$F_2^p = x \left[\frac{4}{9}(u + \bar{u}) + \frac{1}{9}(d + \bar{d}) + \frac{1}{9}(s + \bar{s}) \right]$$

- Comparing the DIS cross section formula with the Mott and Dirac elastic cross sections for particles of mass $m = xM$ and **spin 1/2**
- *If point-like constituents were spin zero particles, we would expect F_1 to be zero*

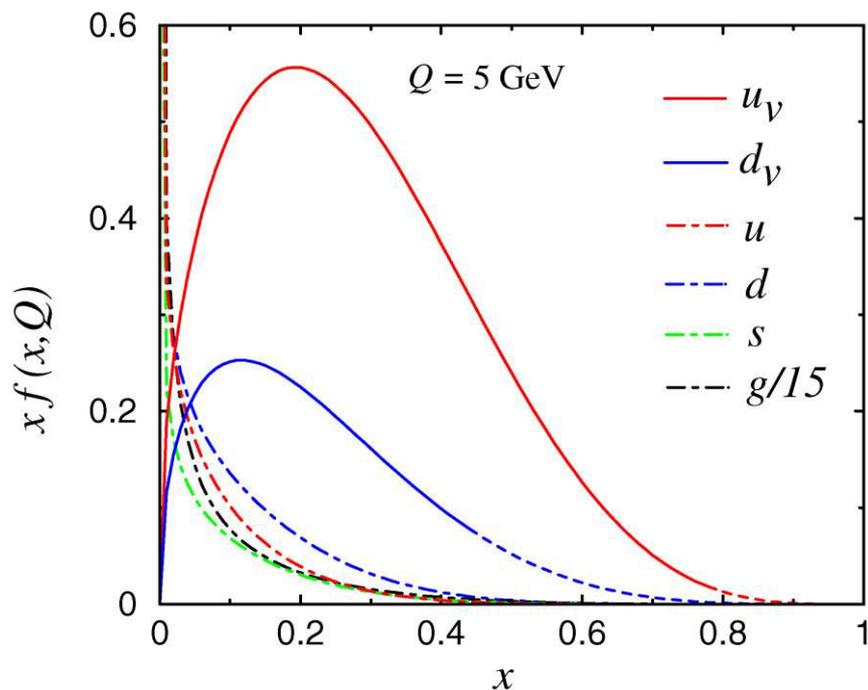
Fast forward....

30+ years of charged lepton Deep Inelastic Scattering at multiple laboratories including SLAC (to ~2000), CERN 80-90s EMC, NMC, BCDMS..), DESY (90s – 21st century H1, ZEUS,...), and more!

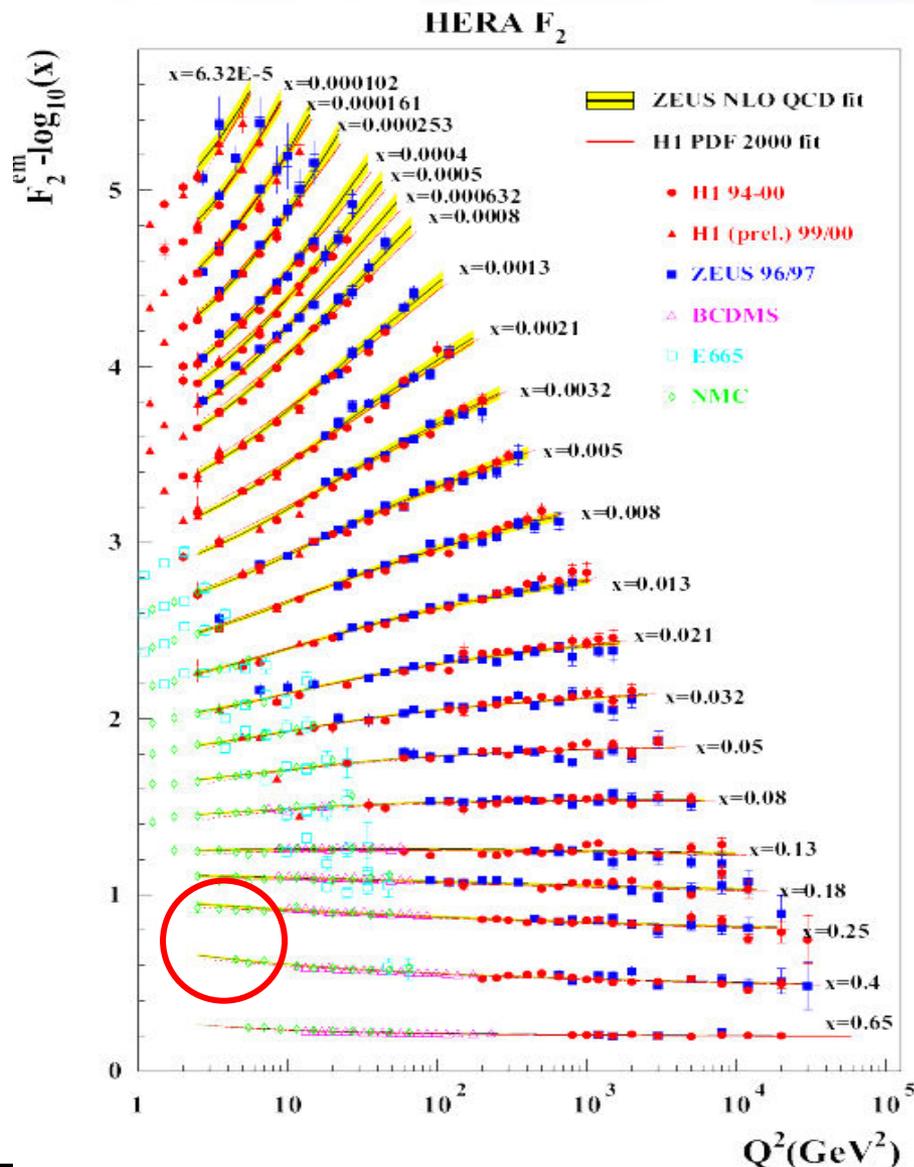


Q^2 Evolution of the F_2 Proton Structure Function

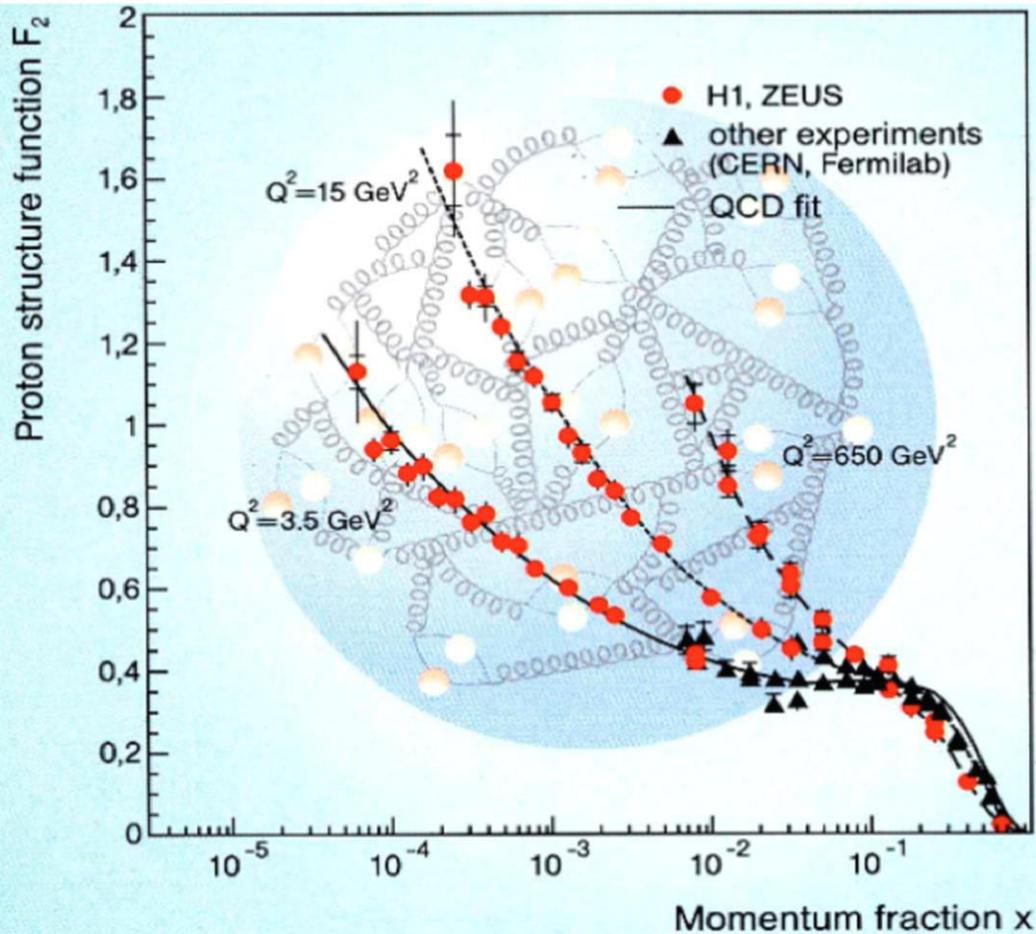
F_2^p Structure Function measured over impressive range of x and Q^2



Allows extraction of *Parton Distribution Functions* $f(x, Q^2)$ - think momentum distribution of quarks

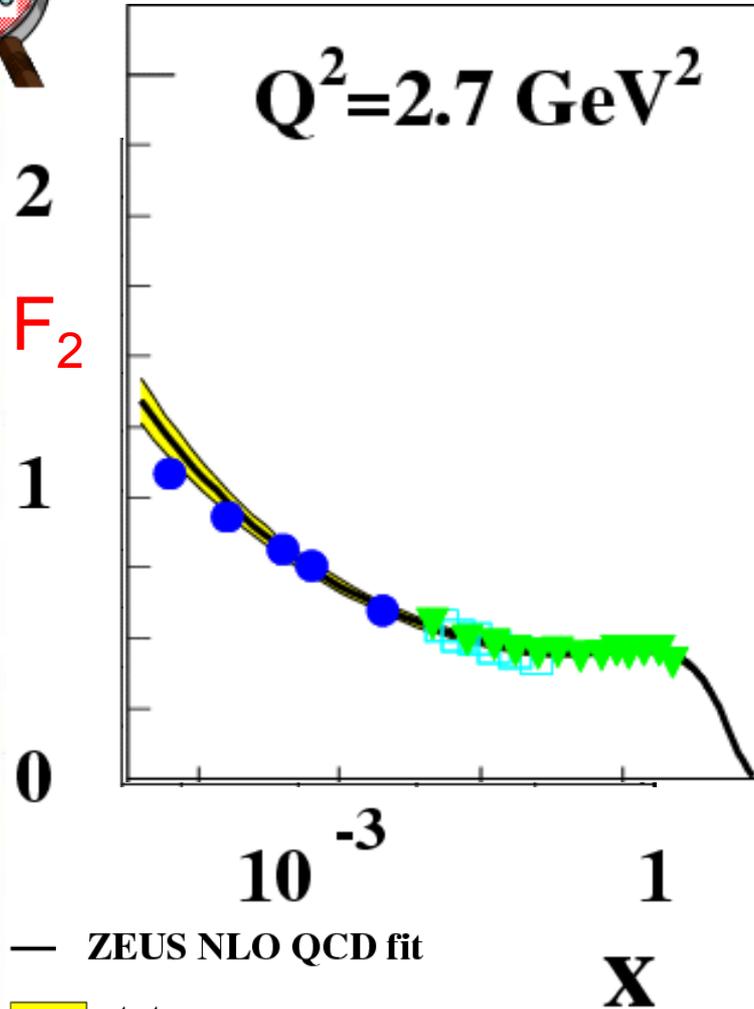
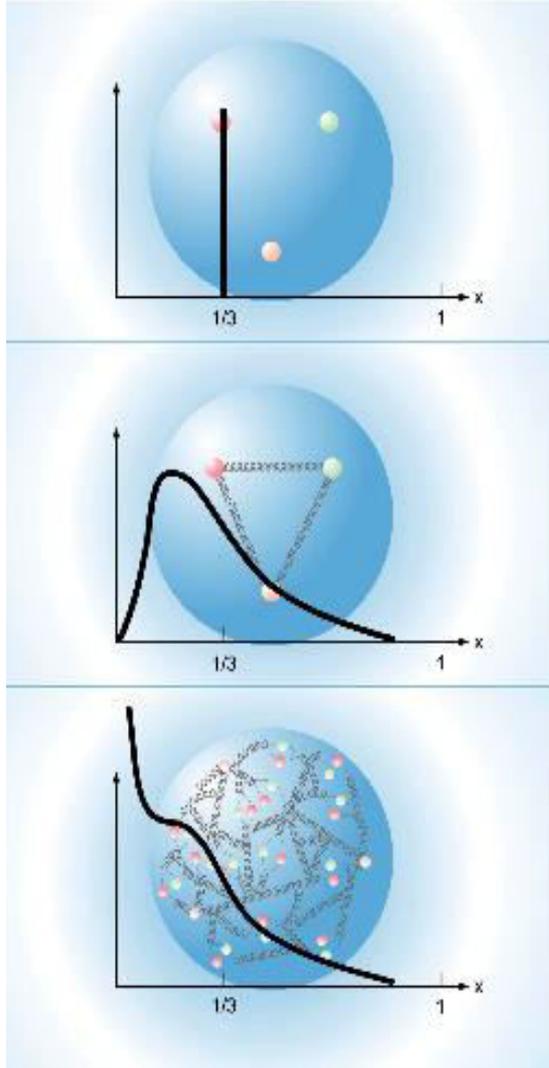
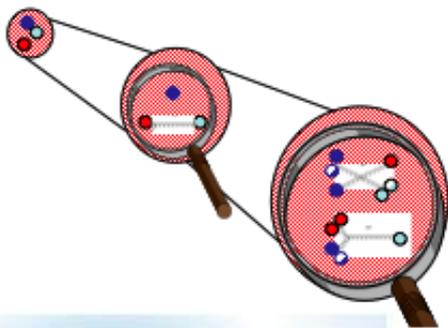


Scaling Violations



- Scaling violation is due to the fact that the quarks radiate gluons that can "materialize" as q-qbar pairs (sea quarks)
- Increasing Q^2 increases the resolution of the probe ($\sim \hbar/\sqrt{Q^2}$) and thus increases the probability of seeing these (abundant) low x partons
- The parton distribution functions (PDFs) can not be calculated from first principle of QCD but **their Q^2 dependence is calculable in perturbative QCD using the DGLAP evolution equations**

Proton Structure Function F_2



Q^2 dependence described by the Dokshitzer-Gribov-Lipatov-Altarelli-Parisi (DGLAP) evolution equations

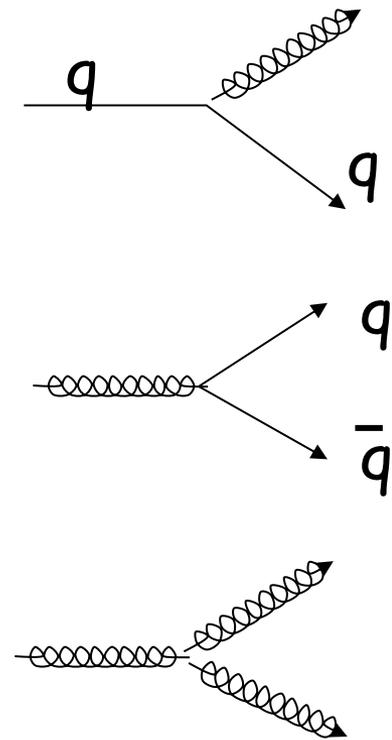
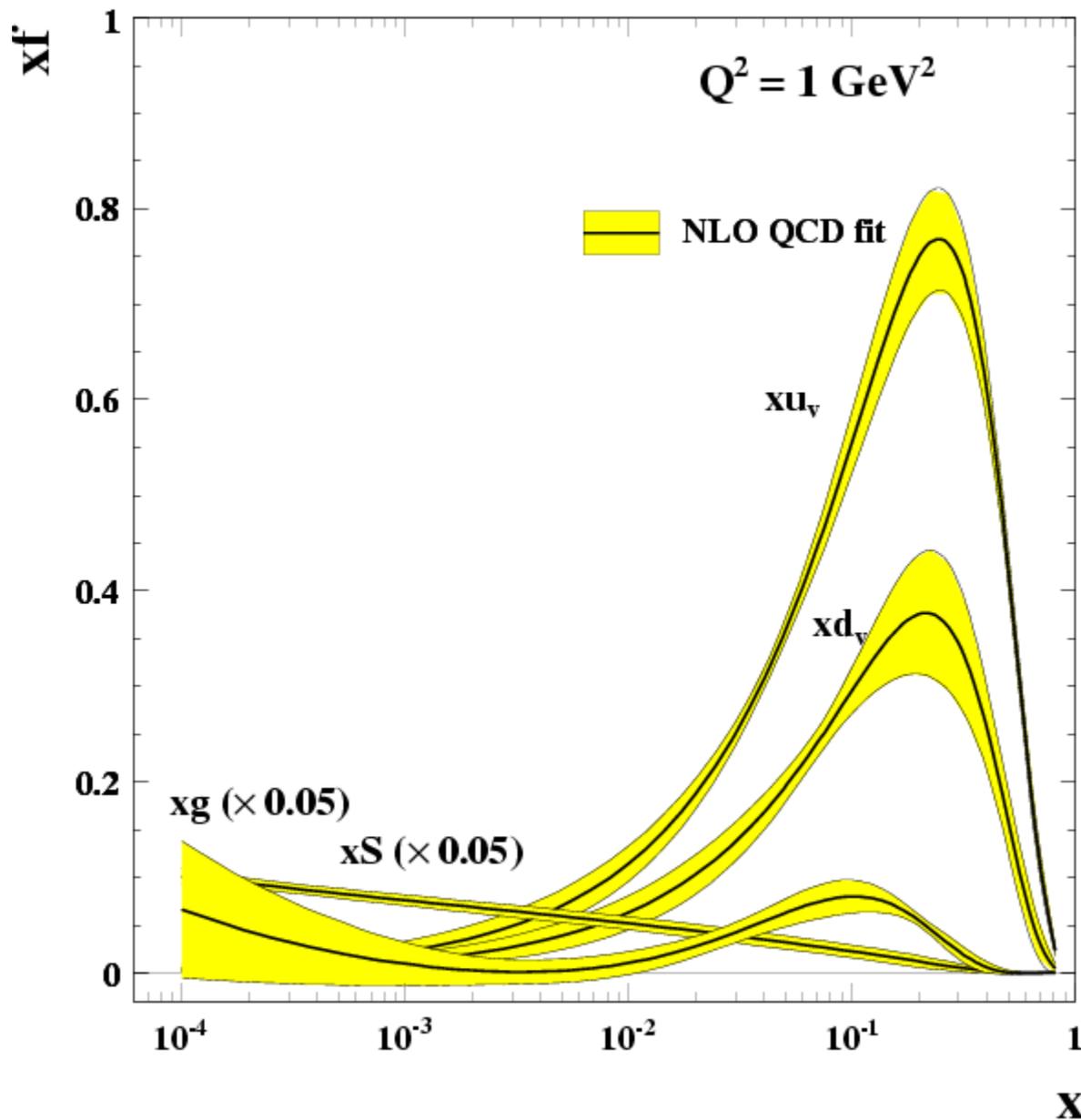
Increasing Q^2 :

- High x decrease
- Low x increase

Allows extraction of Parton Distribution Functions $f(x, Q^2)$ through Q^2 evolution
From high x , low Q to high Q , low x

- ZEUS NLO QCD fit
- tot. error
- ZEUS 96/97
- ▲ BCDMS
- E665
- ▼ NMC

Parton Distribution Functions and QCD Evolution



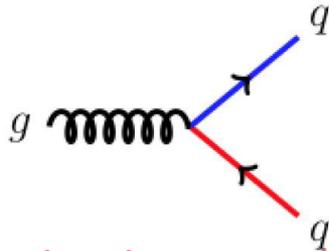
Valence quarks maximum around $x=0.2$; $f(x) \rightarrow 0$ for $x \rightarrow 1$ and $x \rightarrow 0$

Sea quarks and gluons - contribute at low values of x

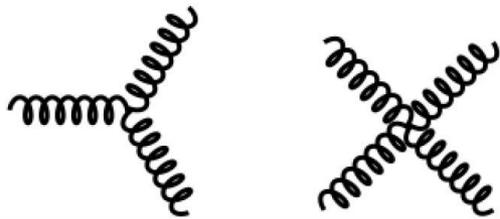
Quantum Chromo Dynamics

Gluons are the messengers for the quark-quark interactions

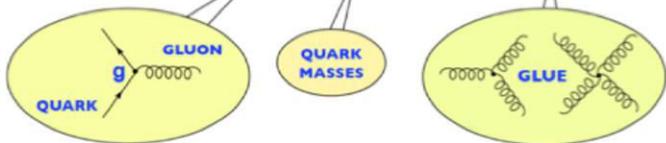
Quantum Chromo Dynamics (QCD) is the theory that governs their behaviour



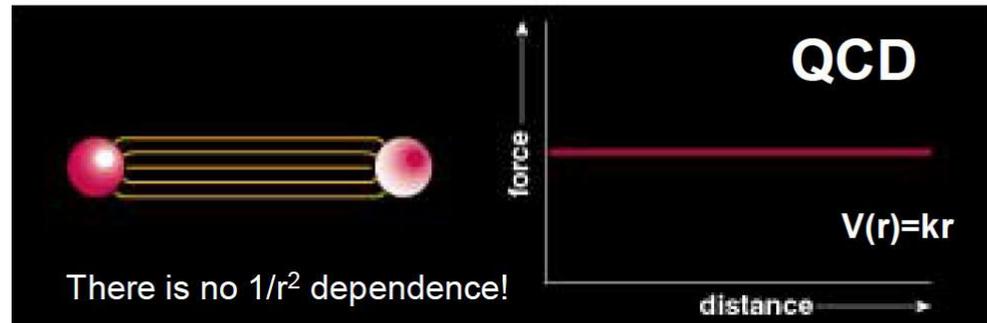
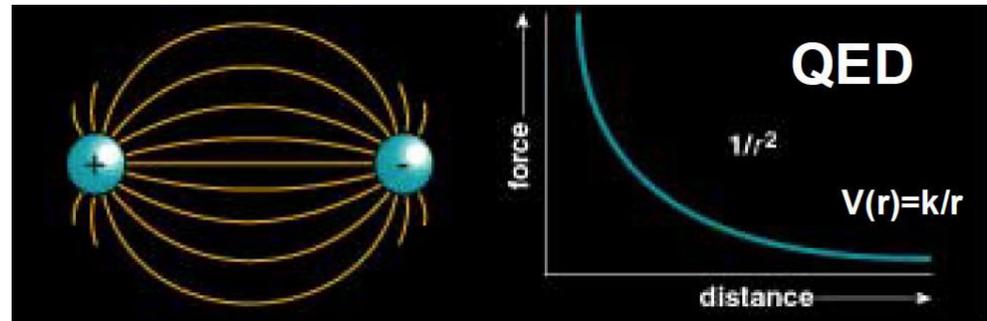
Gluons carry color charge, and we can draw 3- and 4- gluon diagrams (self-interaction)



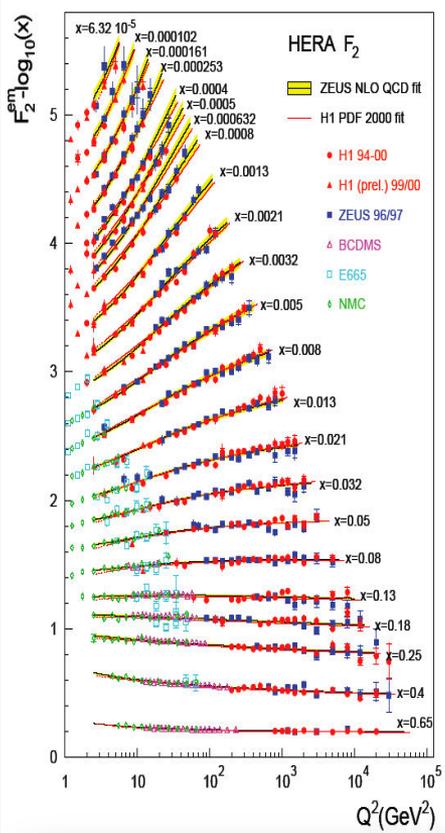
$$\mathcal{L}_{QCD} = \bar{\psi}(i\gamma_{\mu}D^{\mu} - m)\psi - \frac{1}{4}G_{\mu\nu}G^{\mu\nu}$$



The strong force does not get weaker with large distances (opposite to the EM force) and blows up at distances around 10^{-15} m (the radius of the nucleon)

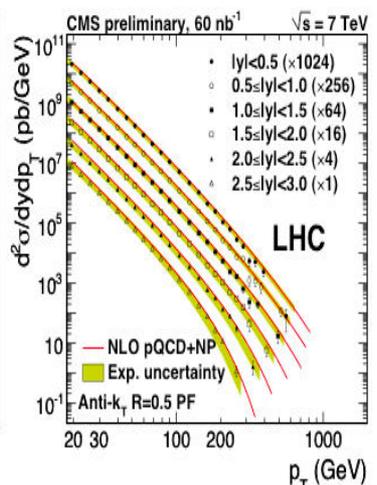
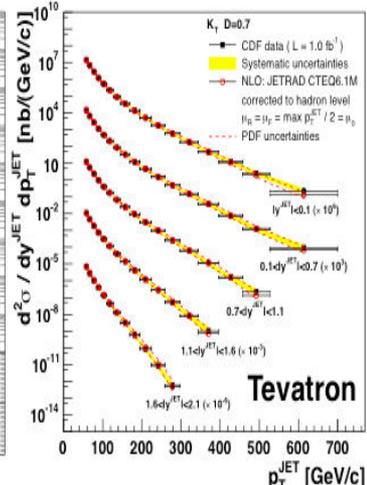
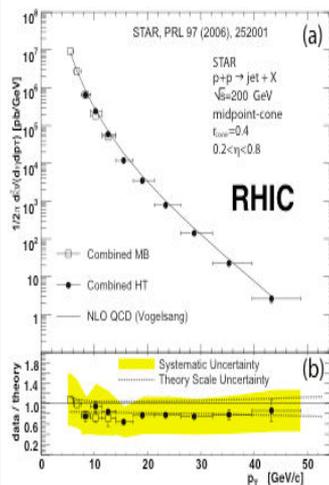
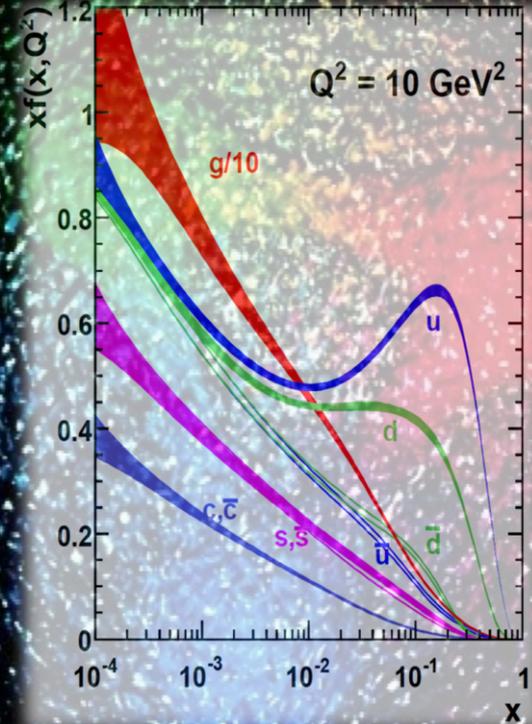


QCD Success !



Measure e-p @ 0.3 TeV (HERA)

p-p and p-p̄ at 0.2, 1.96, and 7 TeV





Quantum ChromoDynamics

2004 David Gross, David Politzer and Frank Wilczek

At short distances

quarks move as though they are free → **Asymptotic freedom**

Physics at short distance is understood through perturbation theory - $\alpha_s(m_Z) = 0.1189(10)$

Perturbative QCD tested up to 1% level

At longer distances

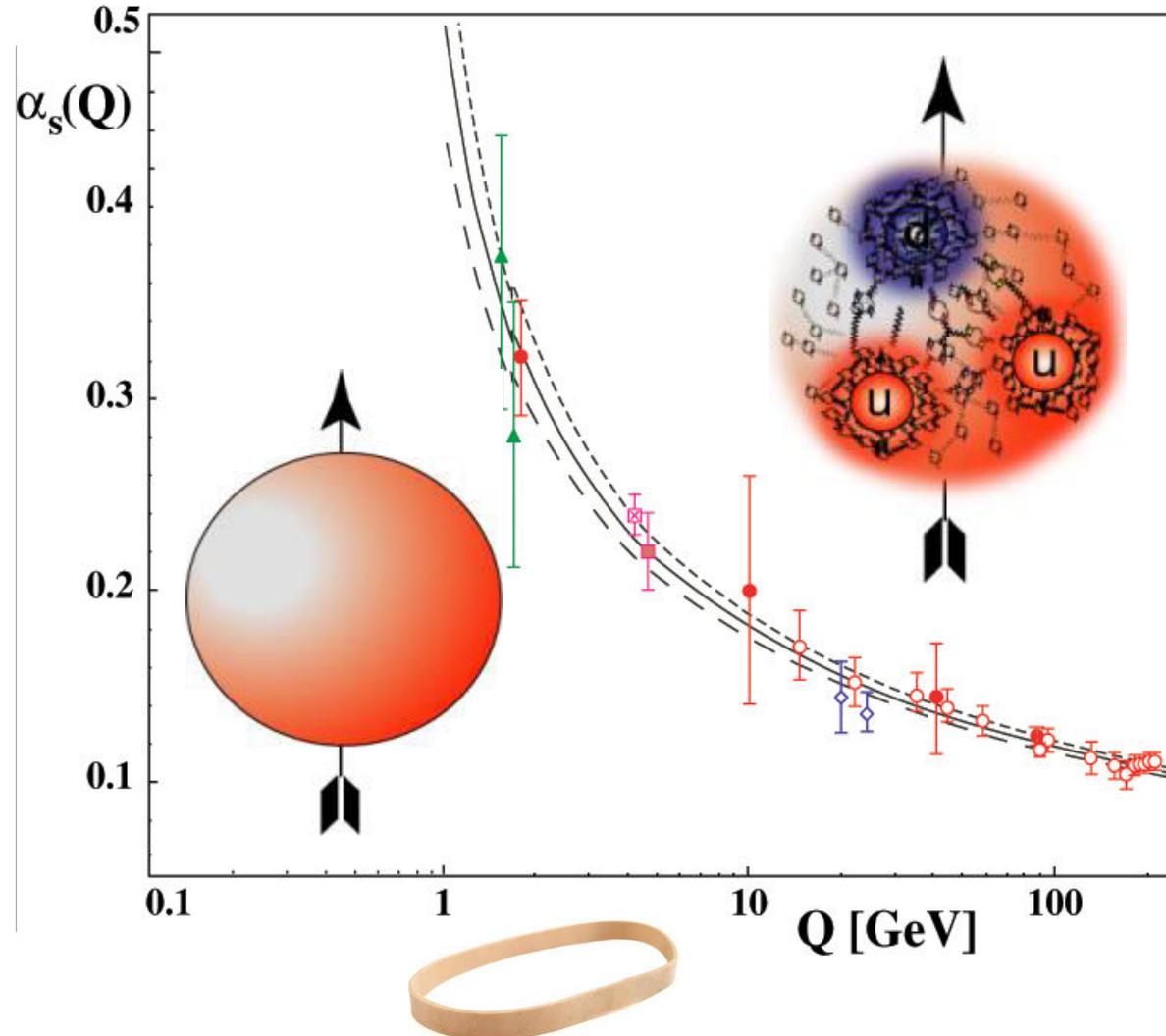
Confinement ensures that only hadronic final states are observed

Quarks can be removed from the proton, but cannot be isolated!!!

We never see a free quark

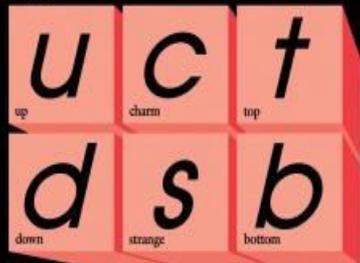
QCD still unsolved in non-perturbative region

Insights into soft phenomena exist through qualitative models and quantitative numerical (lattice) calculations



From the D. Gross Nobel Lecture (2004):

Quarks



Forces



Leptons

“It is sometimes claimed that the origin of mass is the Higgs mechanism that is responsible for the breaking of the electroweak symmetry that unbroken would forbid quark masses. This is incorrect.

Most, 99%, of the proton mass is due to the kinetic and potential energy of the massless gluons and the essentially massless quarks, confined within the proton.”

Lepton Scattering: a Powerful Tool

The best evidence we have for what the nucleon looks like comes from electron scattering experiments

SUCCESS

- Clean probe of hadron structure
- Electron (lepton) vertex well-known from QED
- One can vary the wave-length of the probe to view deeper inside the hadron

$$\lambda \sim \frac{\hbar c}{\sqrt{Q^2}}$$

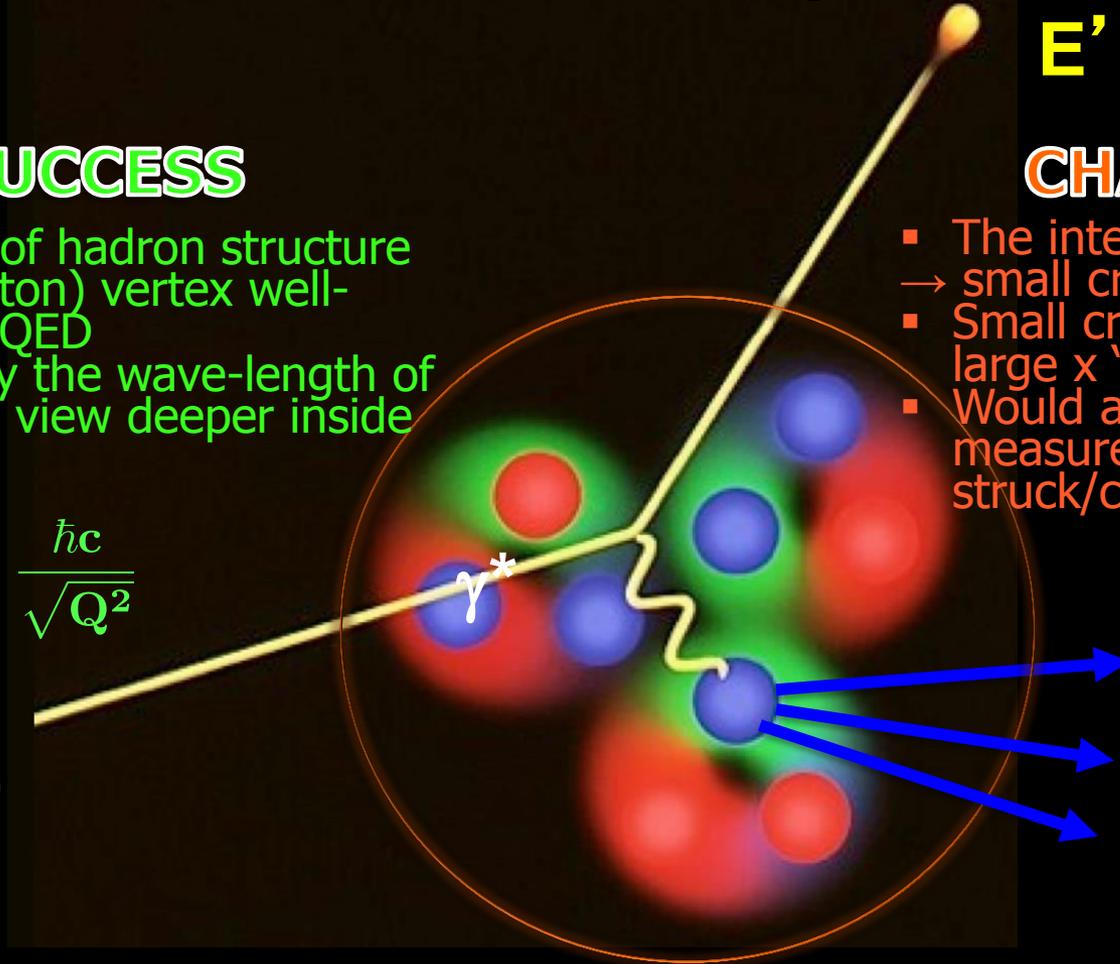
$$\mathbf{E} = (E, \vec{k})$$

$$\mathbf{E}' = (E', \vec{k}')$$

CHALLENGES

- The interaction is weak
→ small cross sections
- Small cross sections also in large x "valence" regime
- Would also like coincidence measurements with struck/created hadrons

Hadrons



Jefferson Lab Continuous Electron Beam Accelerator Facility



1995 - 2012...

Energy 0.4 — 6.0 GeV

- 200 μA , polarization 85%
- Simultaneous delivery 3 halls

- 500+ PhDs completed
- On average 22 US PhDs per year, roughly 25-30% of US PhDs in nuclear physics
- 1530 users in FY2016, ~1/3 international from 37 countries

~2016 -

Energy 0.4 — **12.0 GeV**

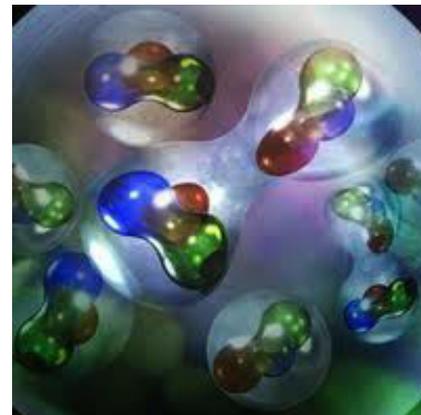
- 150 μA , polarization ~85%
- Simultaneous delivery 4 halls
- FY18: First try simultaneous **delivery to 4 halls – A, B, C, D**

*“Part of what we will tell you this semester is wrong.
The problem is that we do not know what part.”*

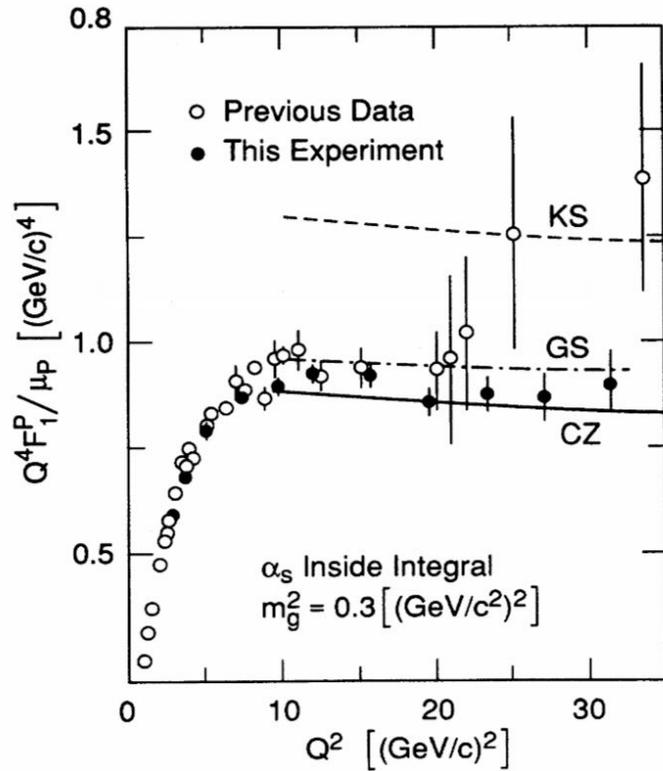
- Multiple sources

“True wisdom is knowing what you don't know”

- Confucius

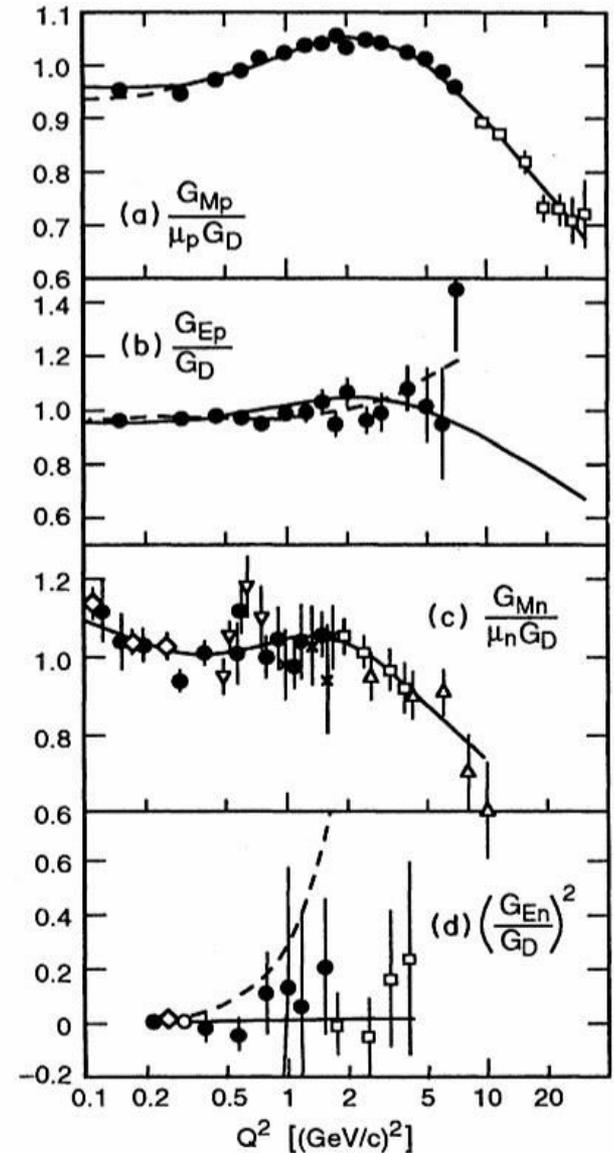


Pre-JLab Results for the Form Factors



Sill et al, 1993

Bosted et al, 1995

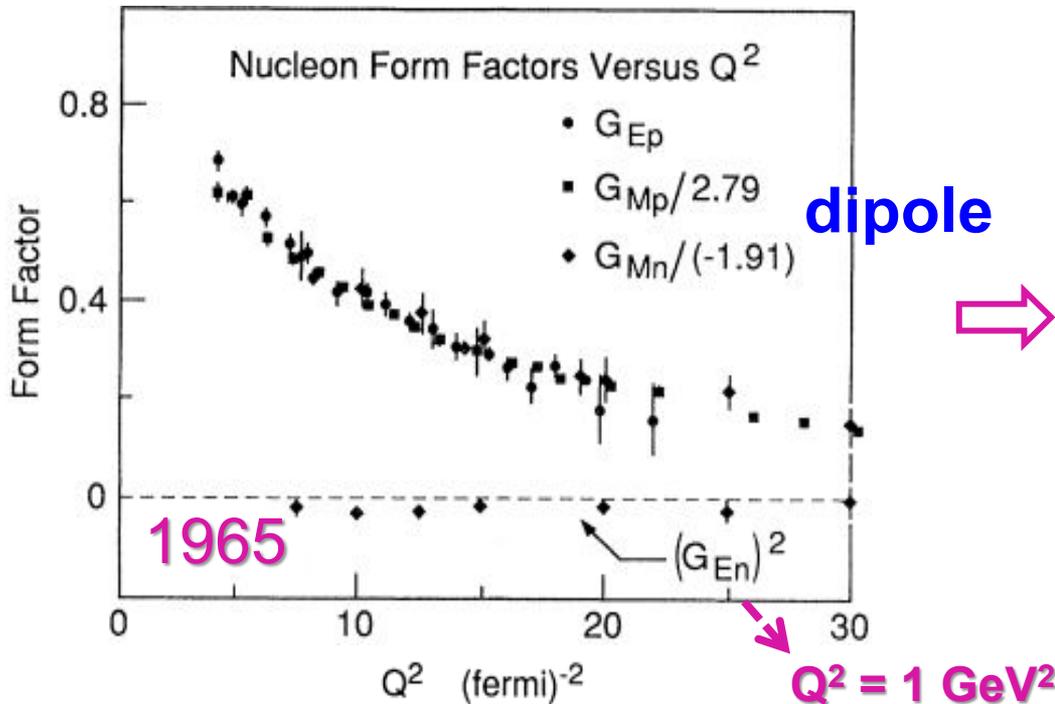


Note log scale!

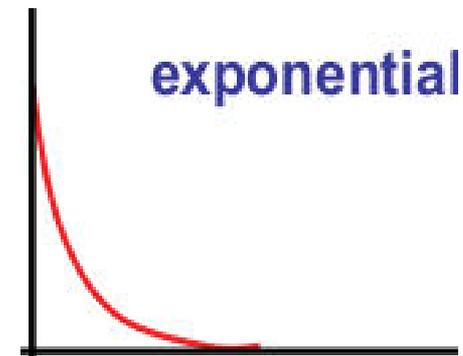
How Do the Charge and Magnetic Moment Distribute?

Probability of elastic interaction: $\frac{d\sigma}{d\Omega} / \left(\frac{d\sigma}{d\Omega} \right)_{point} = \left[\frac{G^2_E(Q^2) + \tau G^2_M(Q^2)}{1 + \tau} + 2\tau G^2_M(Q^2) \tan^2 \frac{\theta}{2} \right] \quad \tau = \frac{Q^2}{4M^2}$

- The Q^2 dependence of form factors was measured...

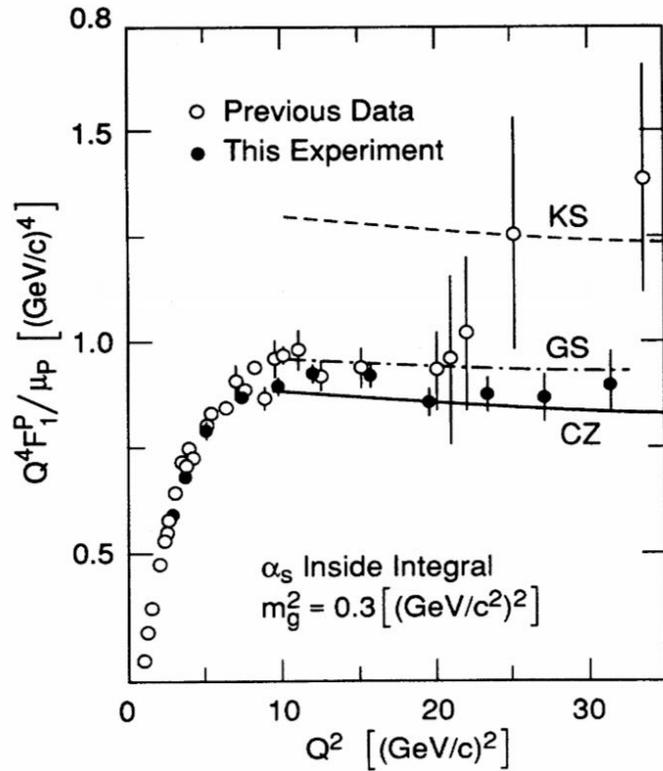


Distribution of Charge or Magnetic Moment



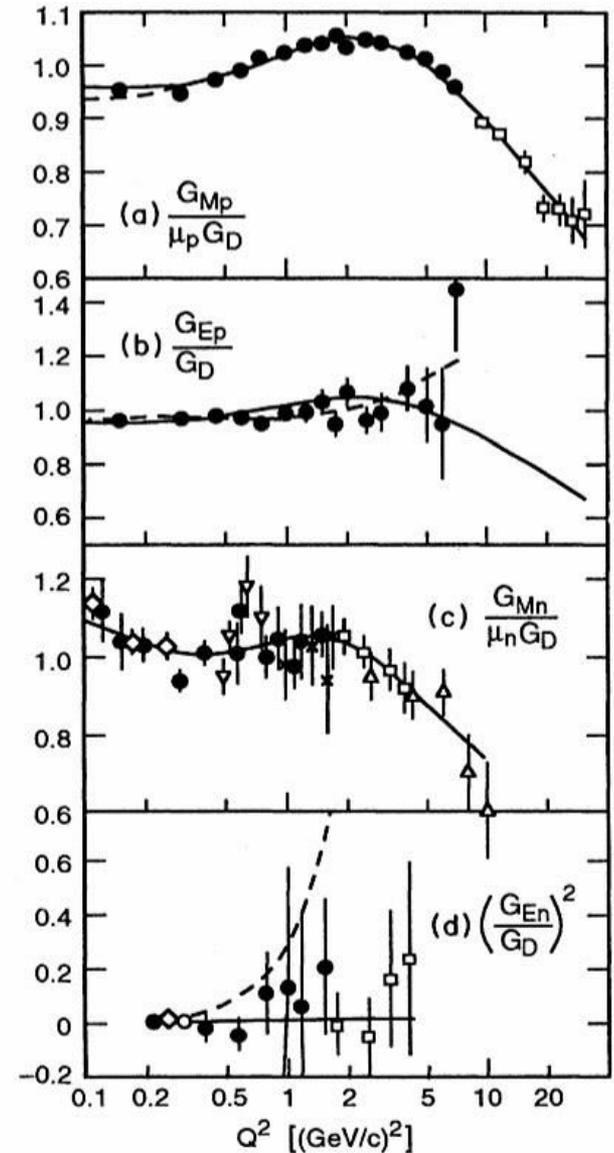
Caveat: The Form Factor as the Fourier transformation of a charge distribution is a non-relativistic concept.

Pre-JLab Results for the Form Factors



Sill et al, 1993

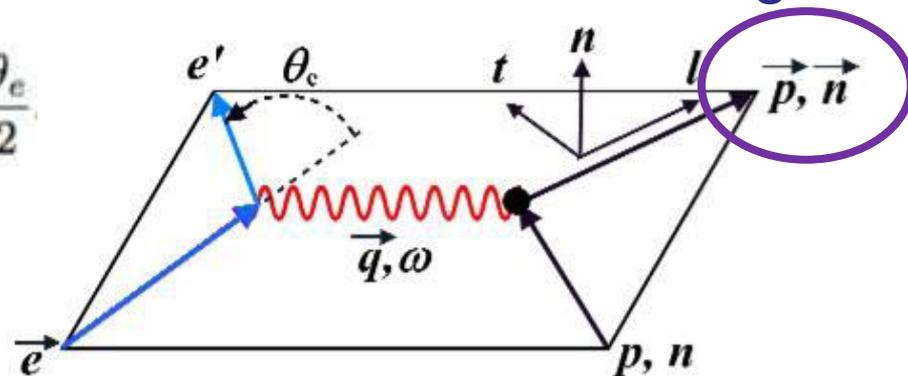
Bosted et al, 1995



Note log scale! slide 28

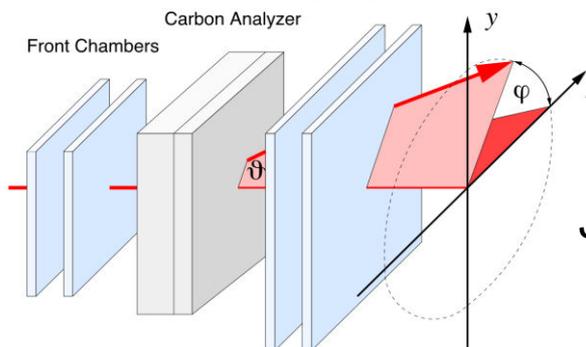
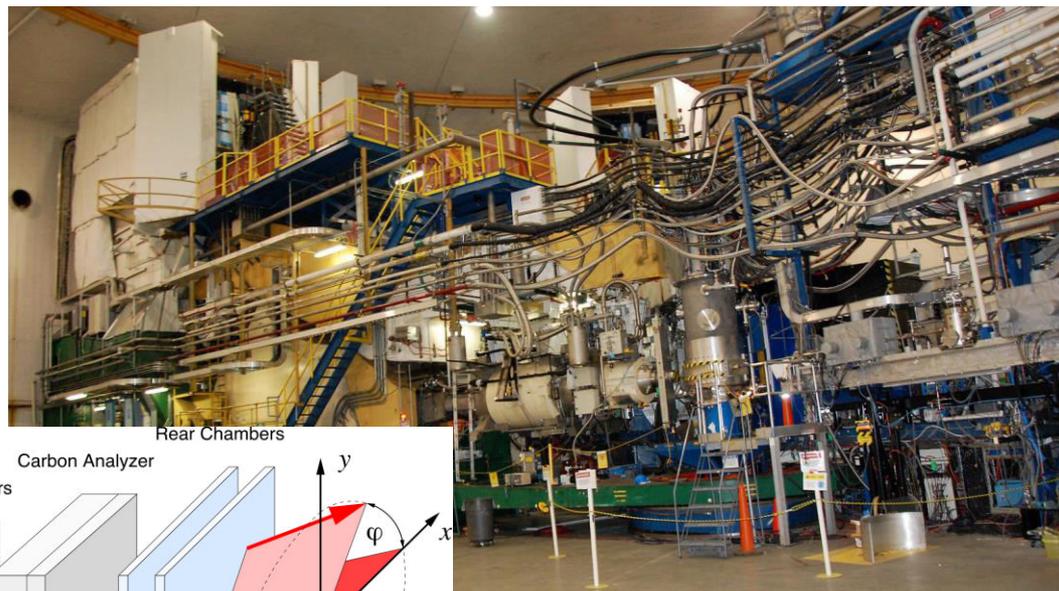
Polarization Transfer in Elastic Electron-Proton Scattering

$$\frac{G_E}{G_M} = -\frac{P_t (E_{beam} + E_e)}{P_l 2M} \tan \frac{\theta_e}{2}$$



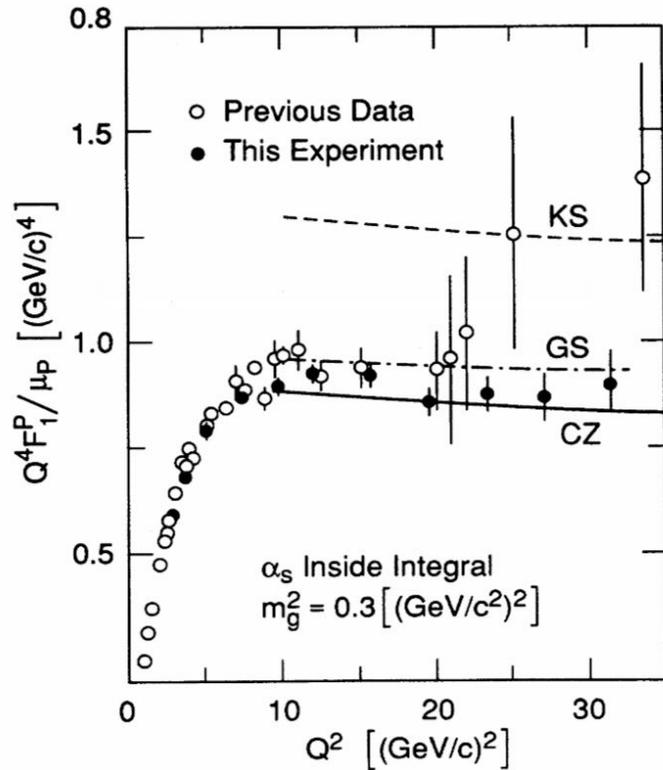
Longitudinally polarized electron beam

- The double-polarization approach obtains the FF ratio by measuring two polarization components simultaneously.
- Employ a combination of spin precession in a magnetic spectrometer and a proton polarimeter.
- A single measurement of the azimuthal angular distribution of the proton scattered in a secondary target gives both the longitudinal, P_l , and transverse, P_t , polarization.



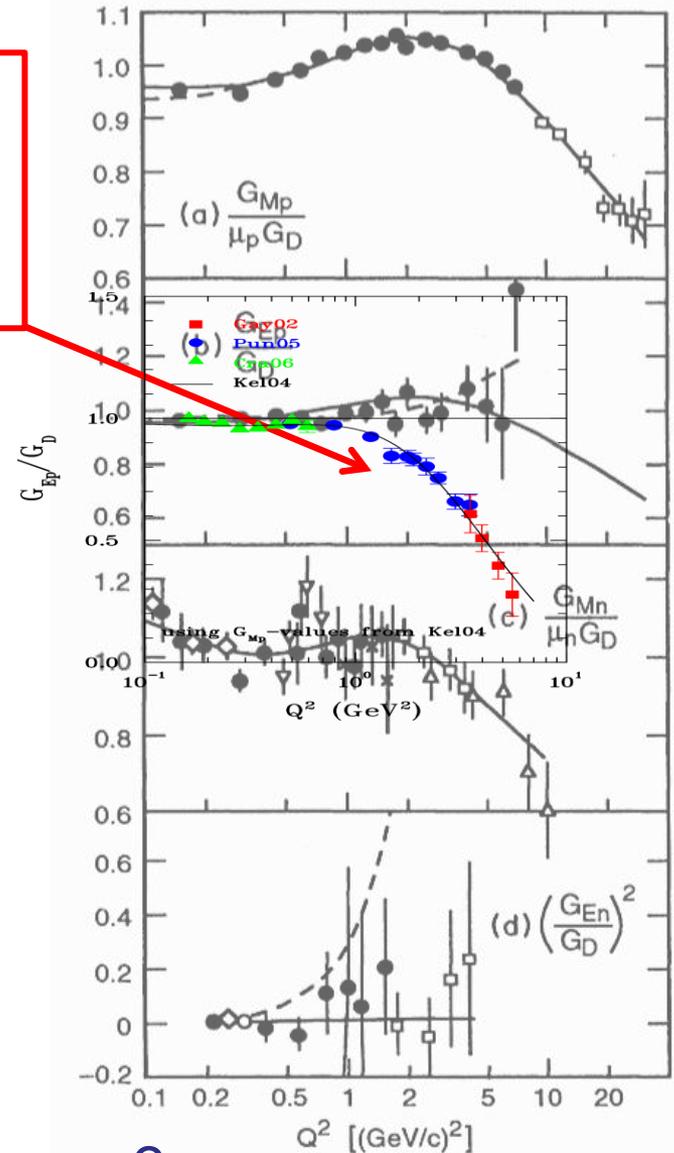
JLab Hall A HRS spectrometer

Surprising Result for the Form Factors...



Jefferson Lab
polarization
transfer
results!!

First paper
800+ citations!

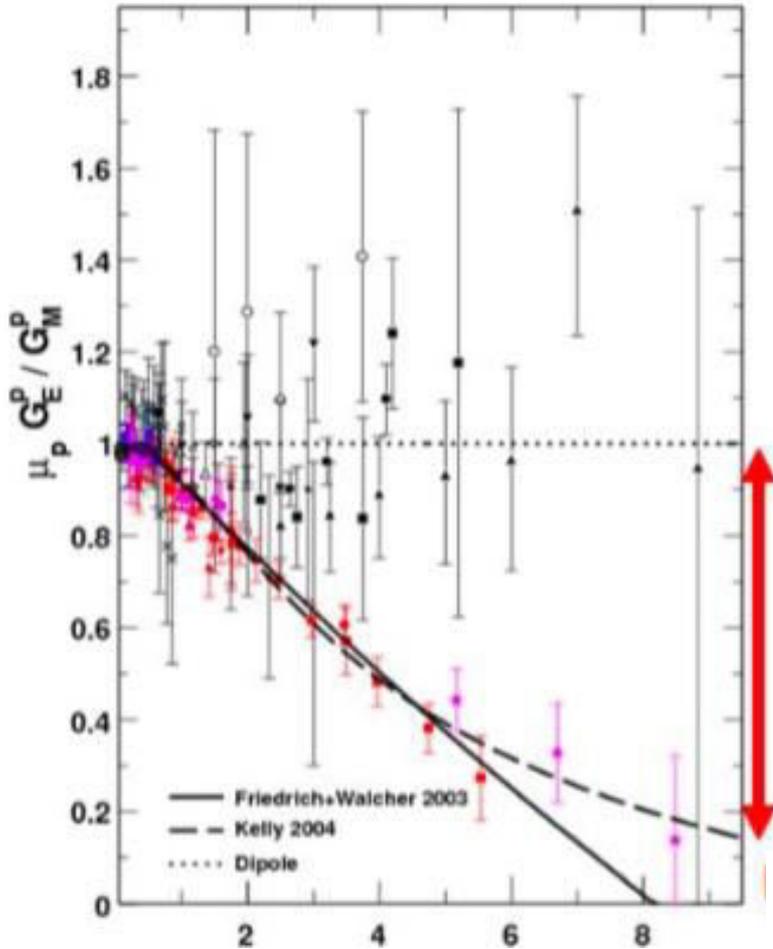


1) $e + p \rightarrow e' + p$
 G_E^p / G_M^p constant

2) $\vec{e} + p \rightarrow e' + \vec{p}$
 G_E^p / G_M^p drops with Q^2

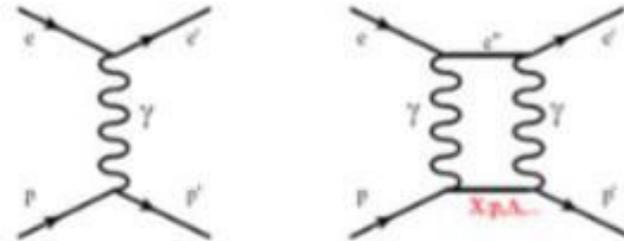
What is going on?...

Proton Form Factor Ratio



Jefferson Lab 2000–today

- All Rosenbluth data from SLAC and Jlab in agreement
- Dramatic discrepancy between Rosenbluth and recoil polarization technique
- Contribution of multiple hard photon exchange accepted explanation



Dramatic discrepancy!

Q^2

In general, polarization observables are rather insensitive to radiative corrections, as they are by definition a ratio of a polarized cross section to an unpolarized one.

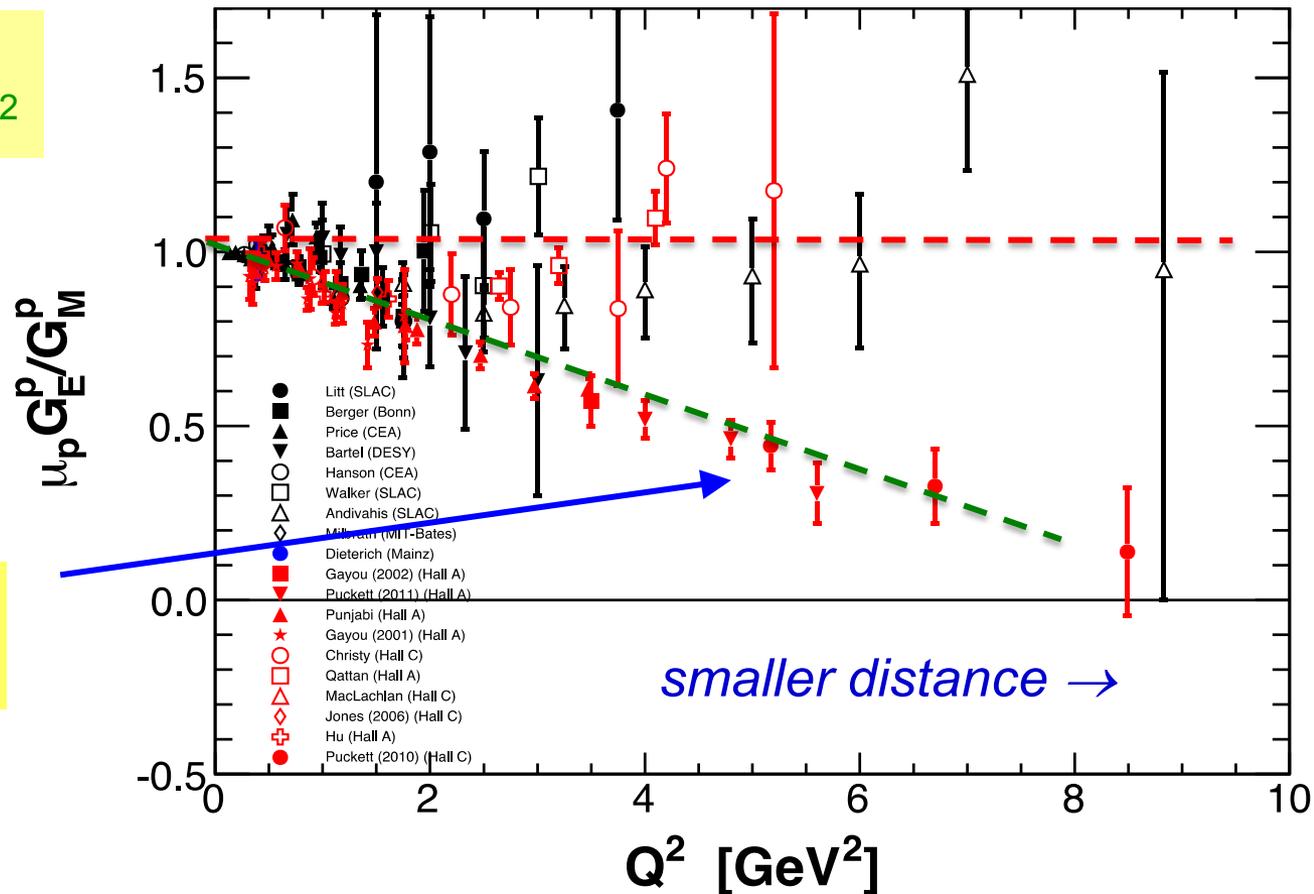
Proton Charge and Magnetization

$$\vec{e} + p \rightarrow e' + \vec{p}$$

G_E^p/G_M^p drops with Q^2

Charge & magnetization distributions in the proton **are different**

charge depletion in interior of proton

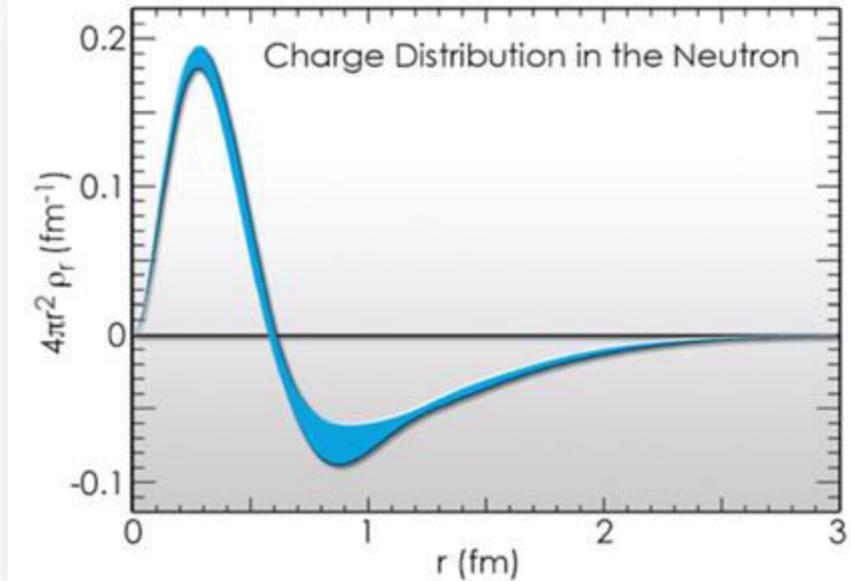
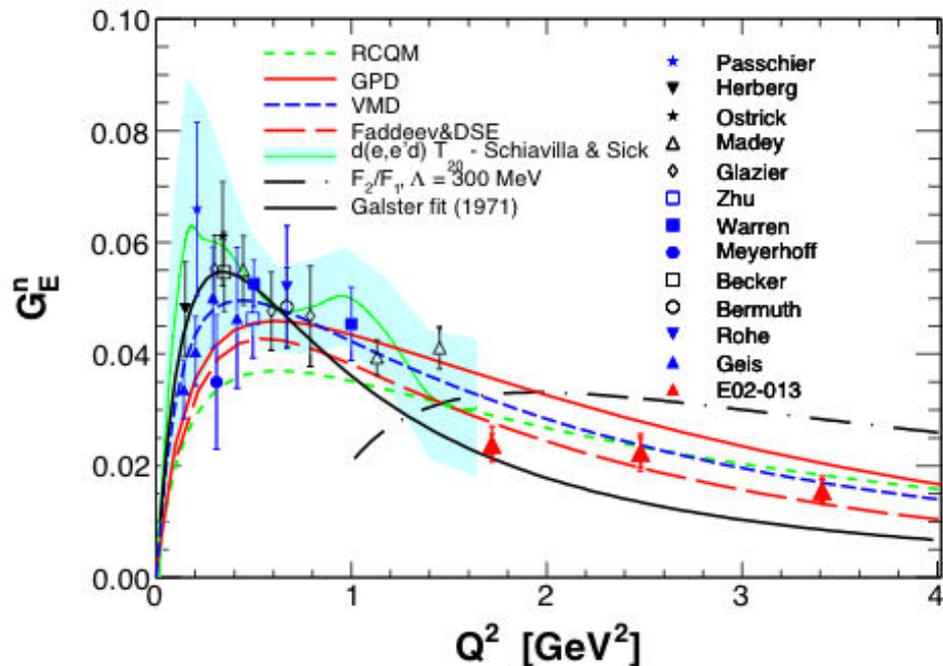


*Orbital motion of quarks play a key role
(Belitsky, Ji + Yuan PRL 91 (2003) 092003)*



Neutron has no charge, but does have a charge distributions: $n = p + \pi^-$, $n = ddu$. Use polarization to access. *“Guarantee” that electron hits a neutron AND electron transfers its polarization to this neutron.*

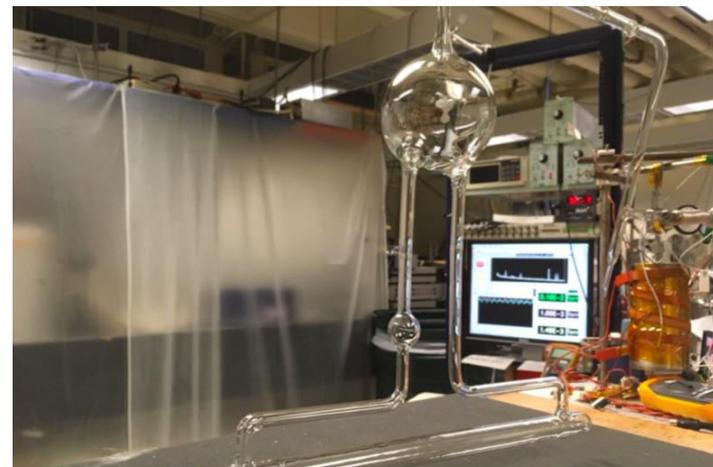
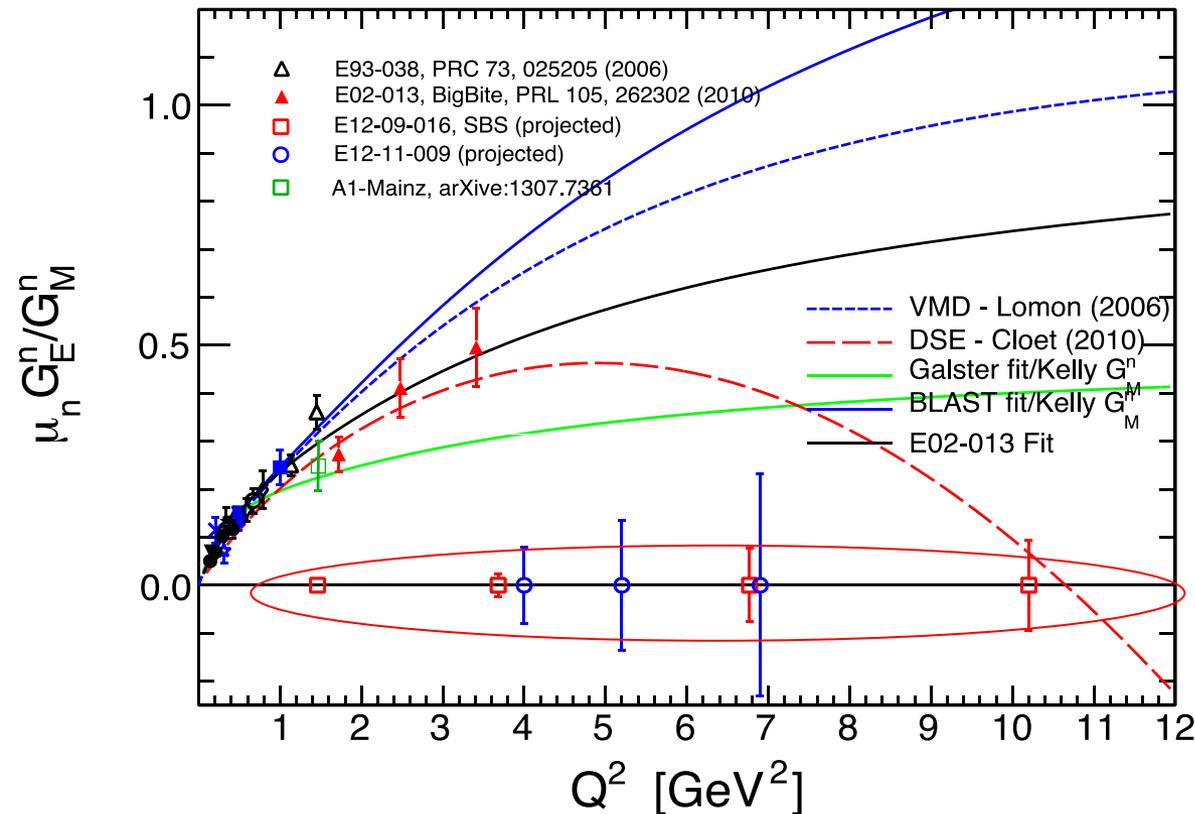
(Polarization Experiments only)



Combining proton and neutron: down quark has more extended spatial charge distribution. Could be due to significant influence of di-quarks?

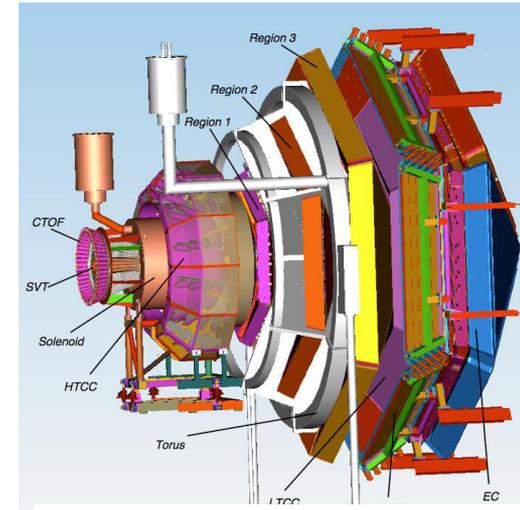
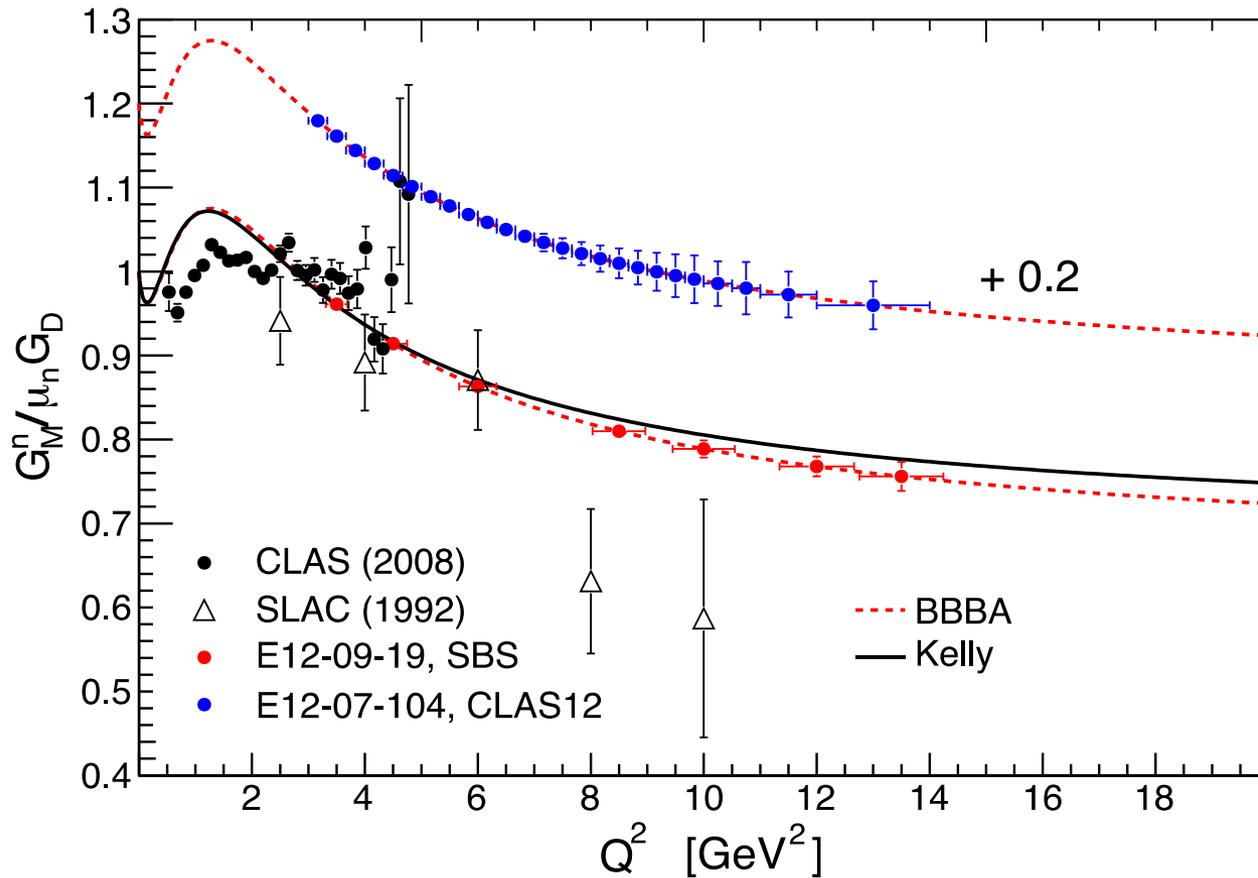
12 GeV G_E^n experiment

Asymmetry in the polarized electron scattering
from the polarized ^3He

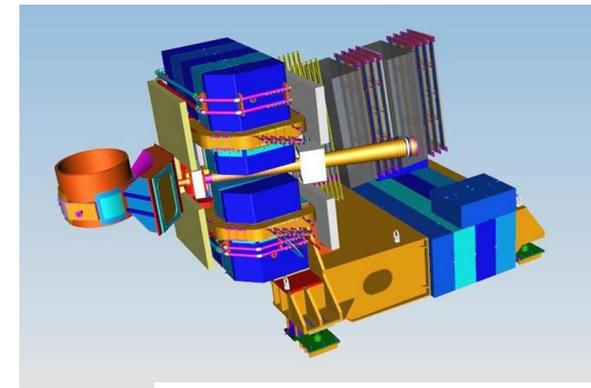


12 GeV G_M^n experiment

Ratio of the cross sections $D(e, e'n)$ and $D(e, e'p)$



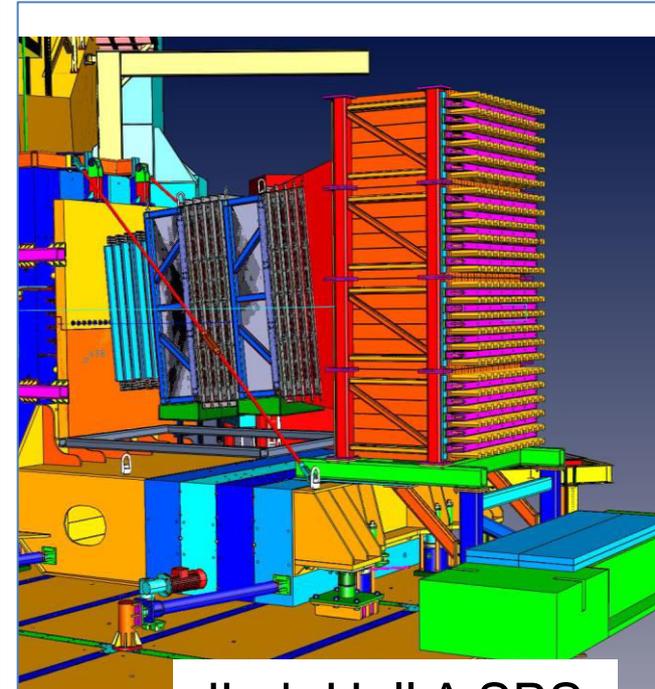
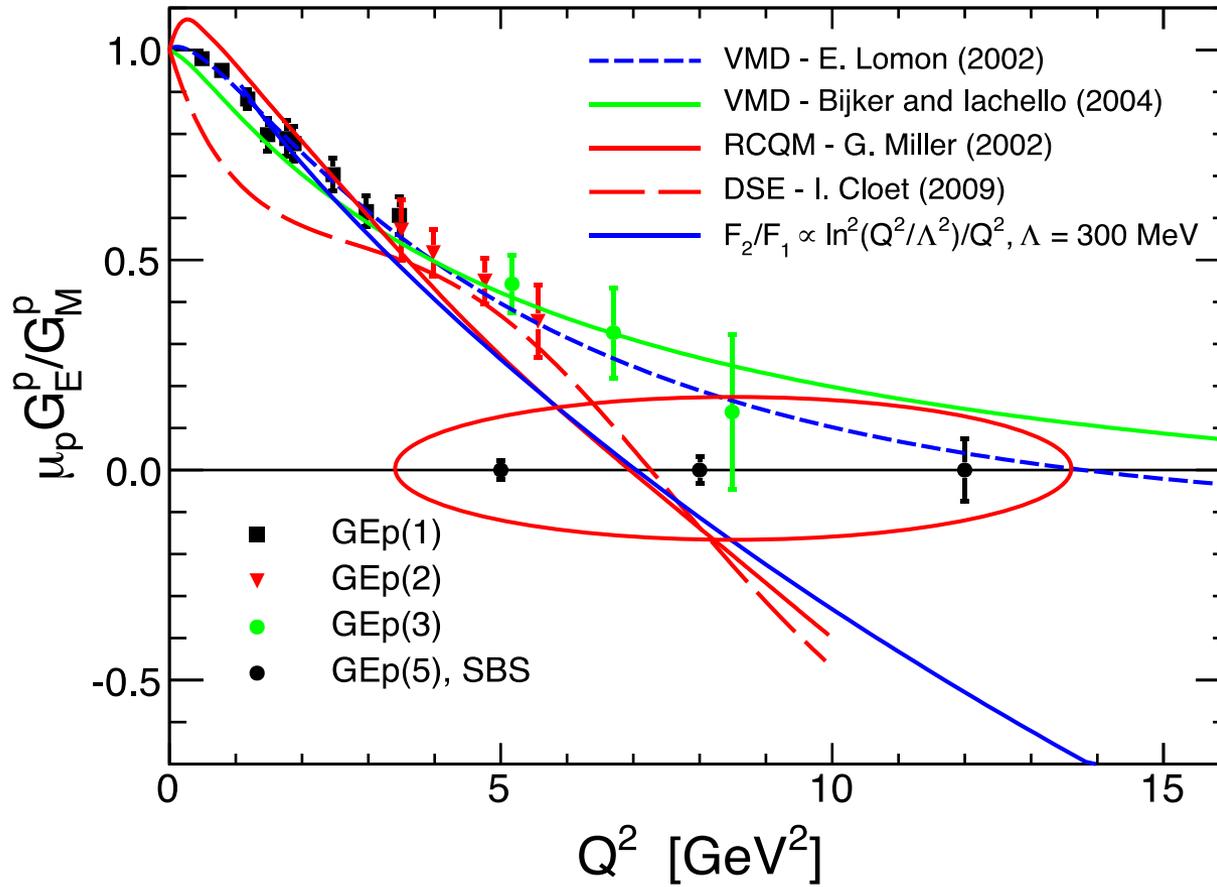
JLab Hall B CLAS12



JLab Hall A SBS

12 GeV G_E^p experiment

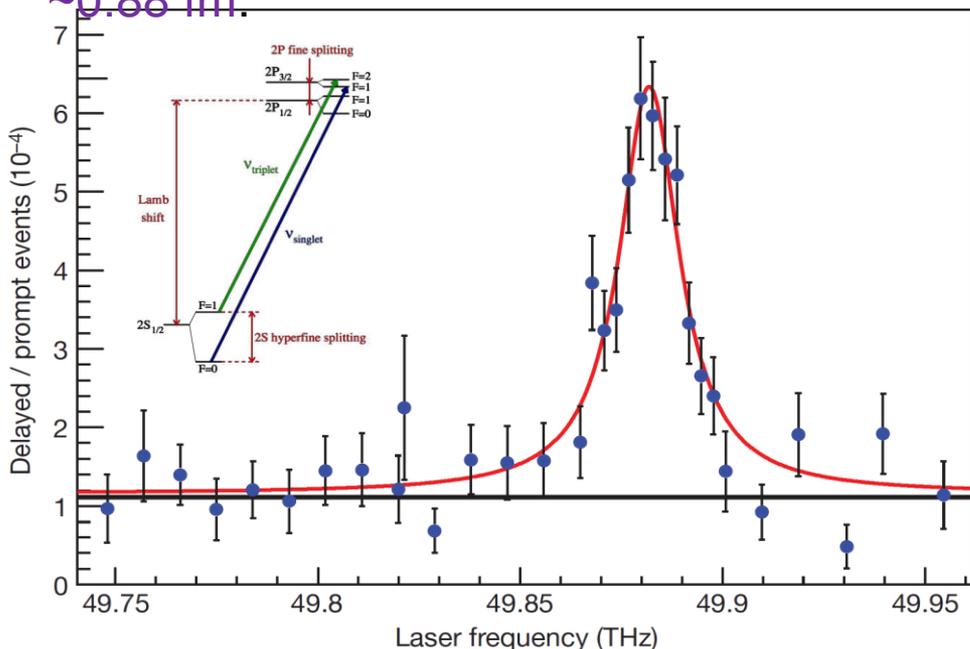
Transverse polarization of the proton
in the polarized electron-proton scattering



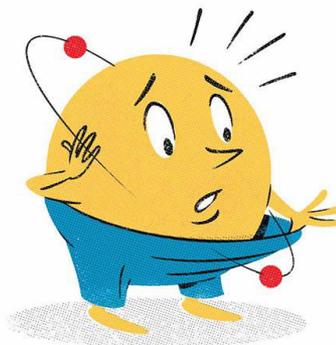
Also measuring at low Q^2 ...

Muonic Hydrogen Data

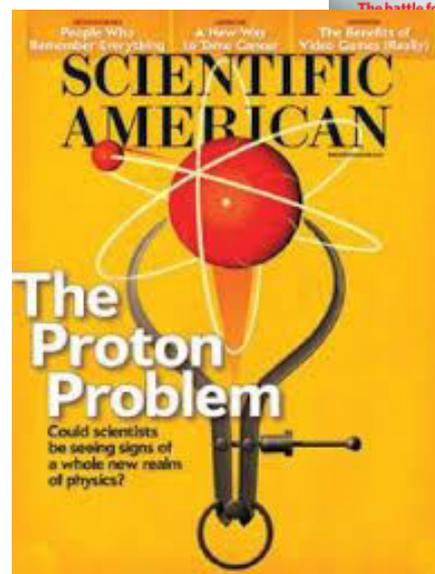
- High precision results from Muonic Lamb shift data give a proton radius of **0.84 fm**.
- This result contradicts many other extractions - *dominantly from electron scattering* - which have determined the proton radius to be **~0.88 fm**.



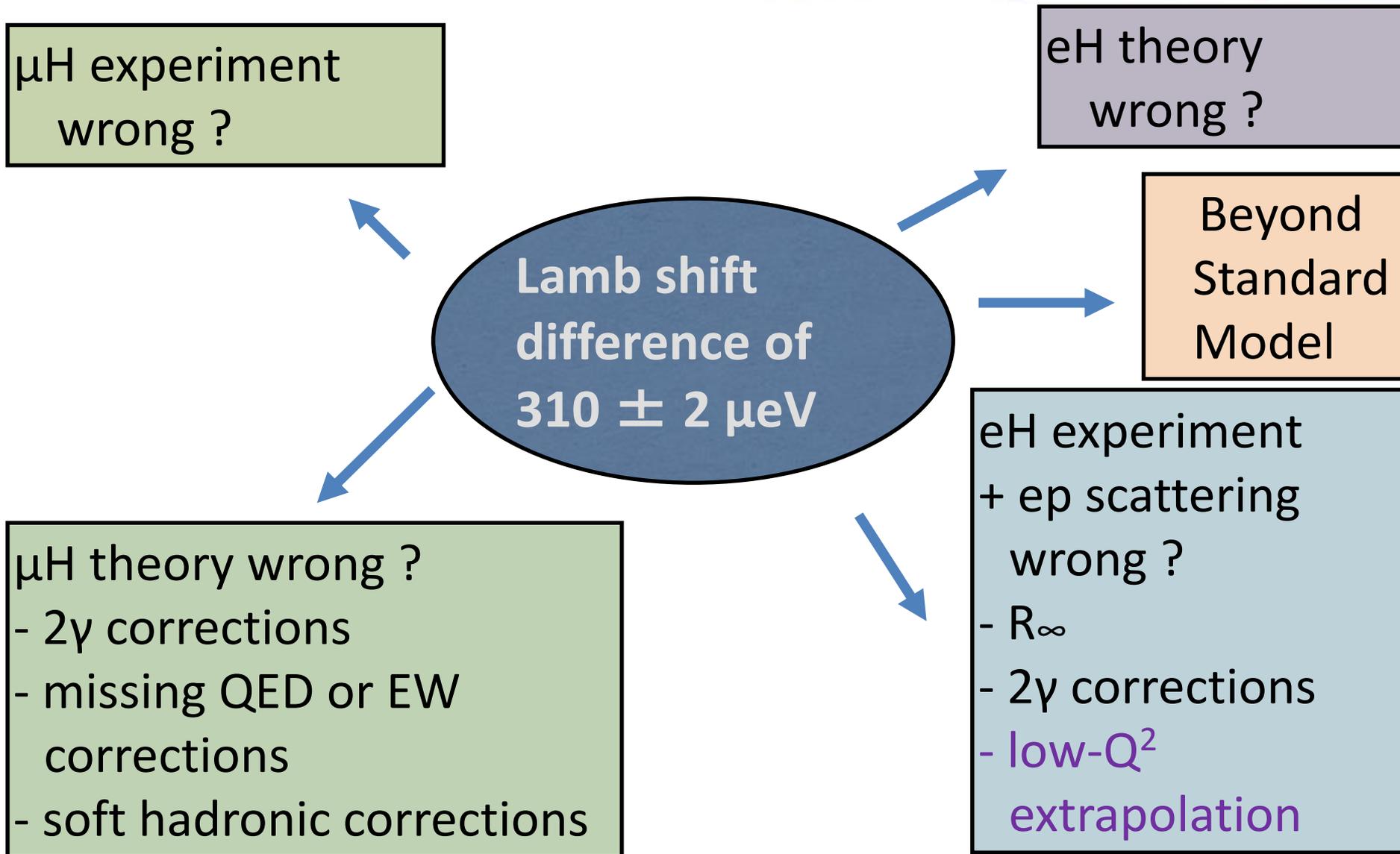
$$E_{2p} - E_{2s} = 209.98 - 5.2262 r_p^2 + 0.0347 r_p^3 \text{ MeV}$$



The
New York
Times



Some Of The Possible Explanations



Need the Slope of $G_E(Q^2)$ Using Low Q^2 Data

$$r_p \equiv \sqrt{\langle r^2 \rangle} = \left(-6 \frac{dG_E(Q^2)}{dQ^2} \Big|_{Q^2=0} \right)^{1/2}$$

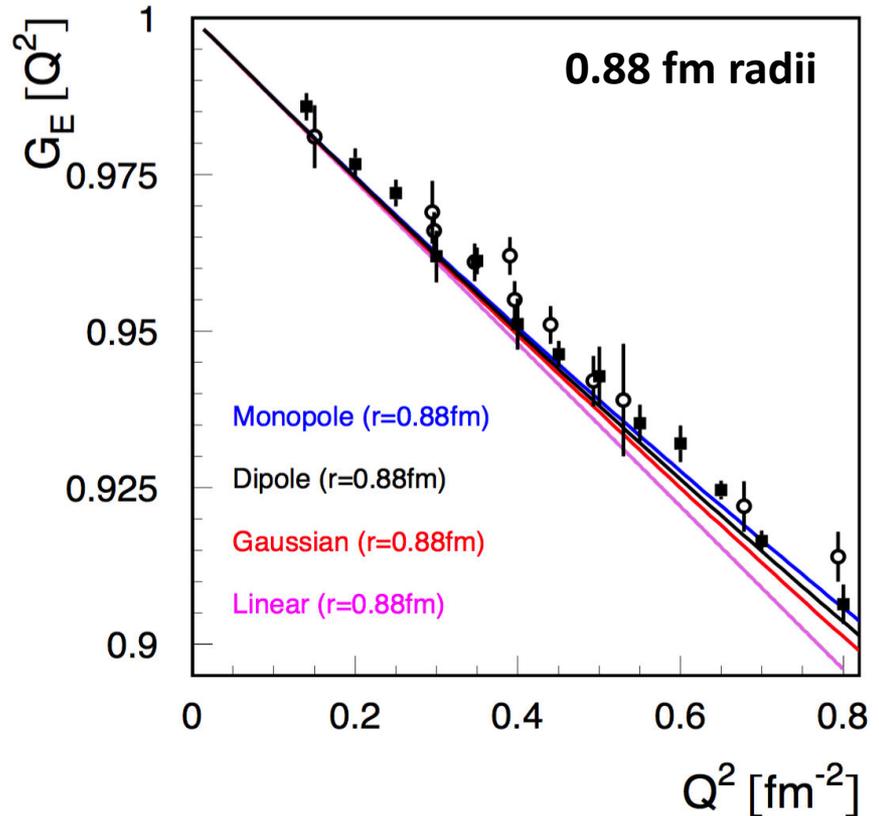
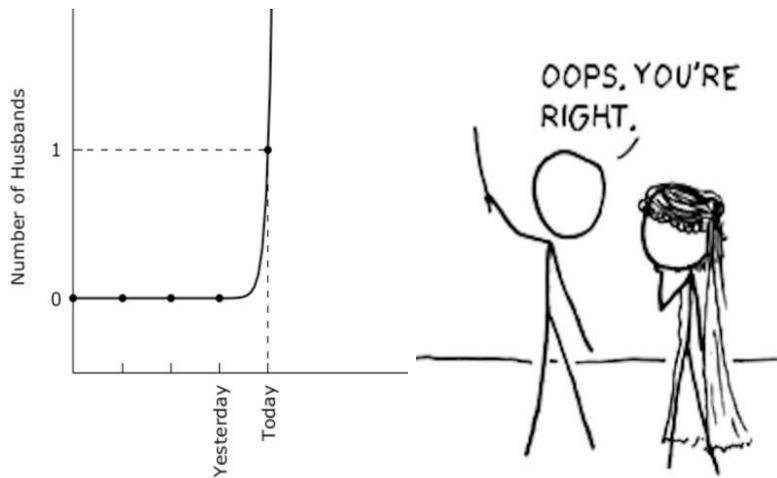
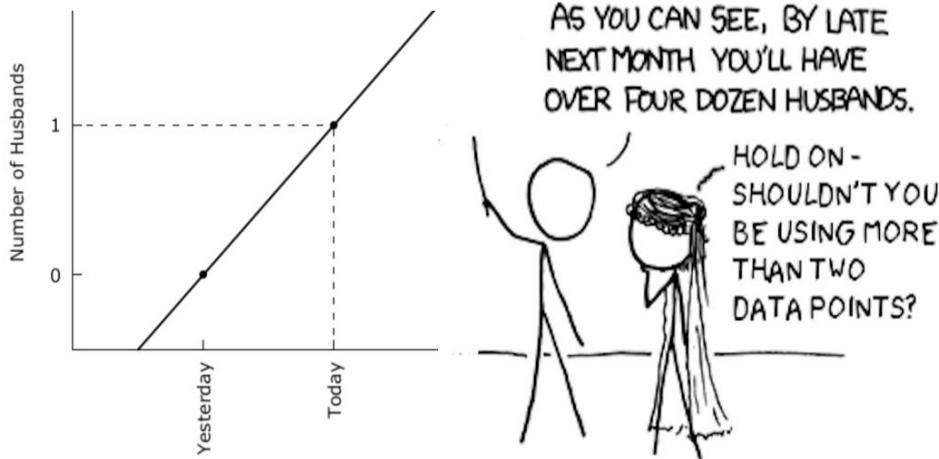
What is going to be what function to use for the fitting & extrapolating?

The answer to this question **STRONGLY** effects the answer!

$Q^2 < (1/0.88 \text{ fm})^2 < 1.2 \text{ fm}^{-2}$ to get the radius of the proton
(equivalent to $\sim 0.05 \text{ GeV}^2$)

Plotting Published Results & Standard Functions

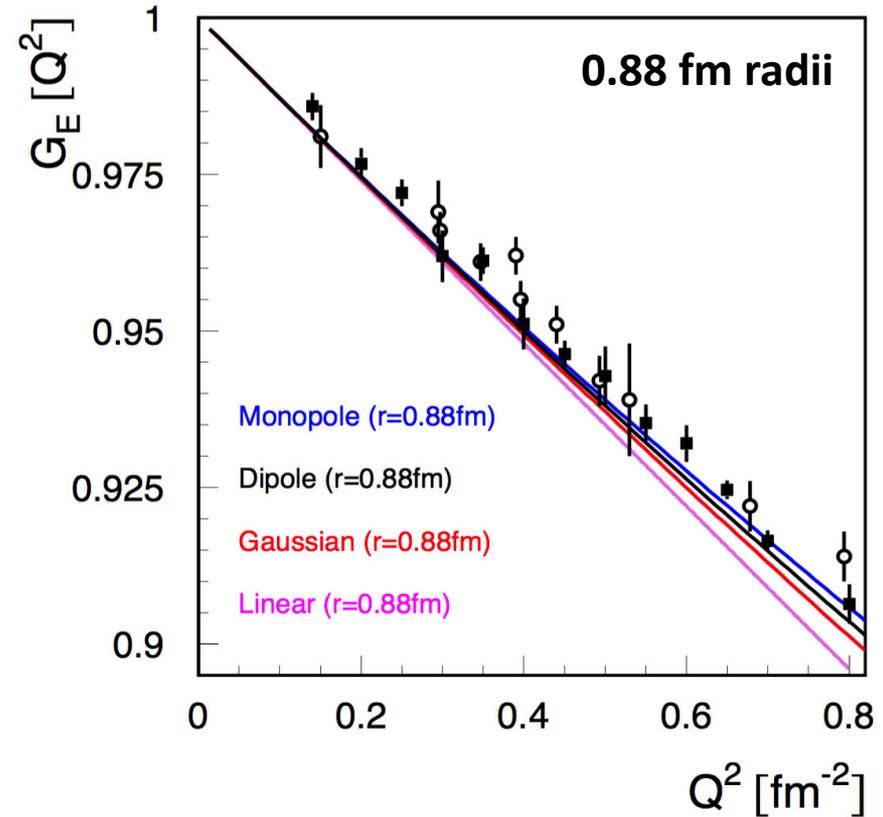
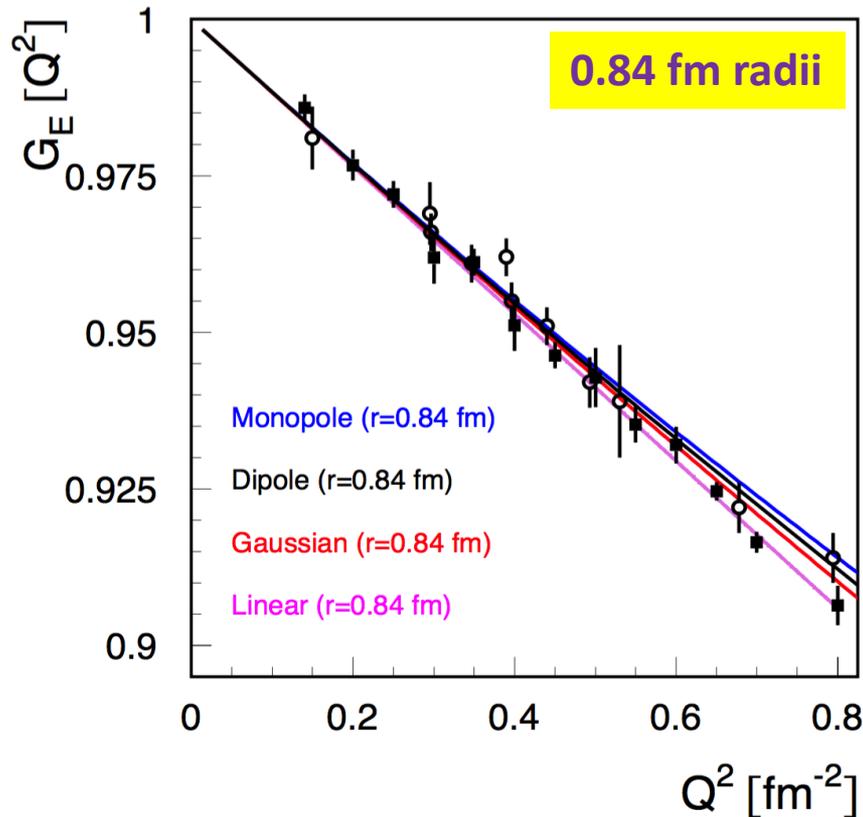
- These are NOT regressions, just the data as published and standard curves. -



Closed Circles Mainz 1980 results and open circles Saskatoon 1974 results.

Plotting Published Results & Standard Functions

- These are NOT regressions, just the data as published and standard curves. -



Note how for a fixed radius, all functions come together as Q^2 gets < 0.4 fm^{-2} .

Need precision data at very low Q^2 !

PRad: JLab Hall B Proton Radius Experiment

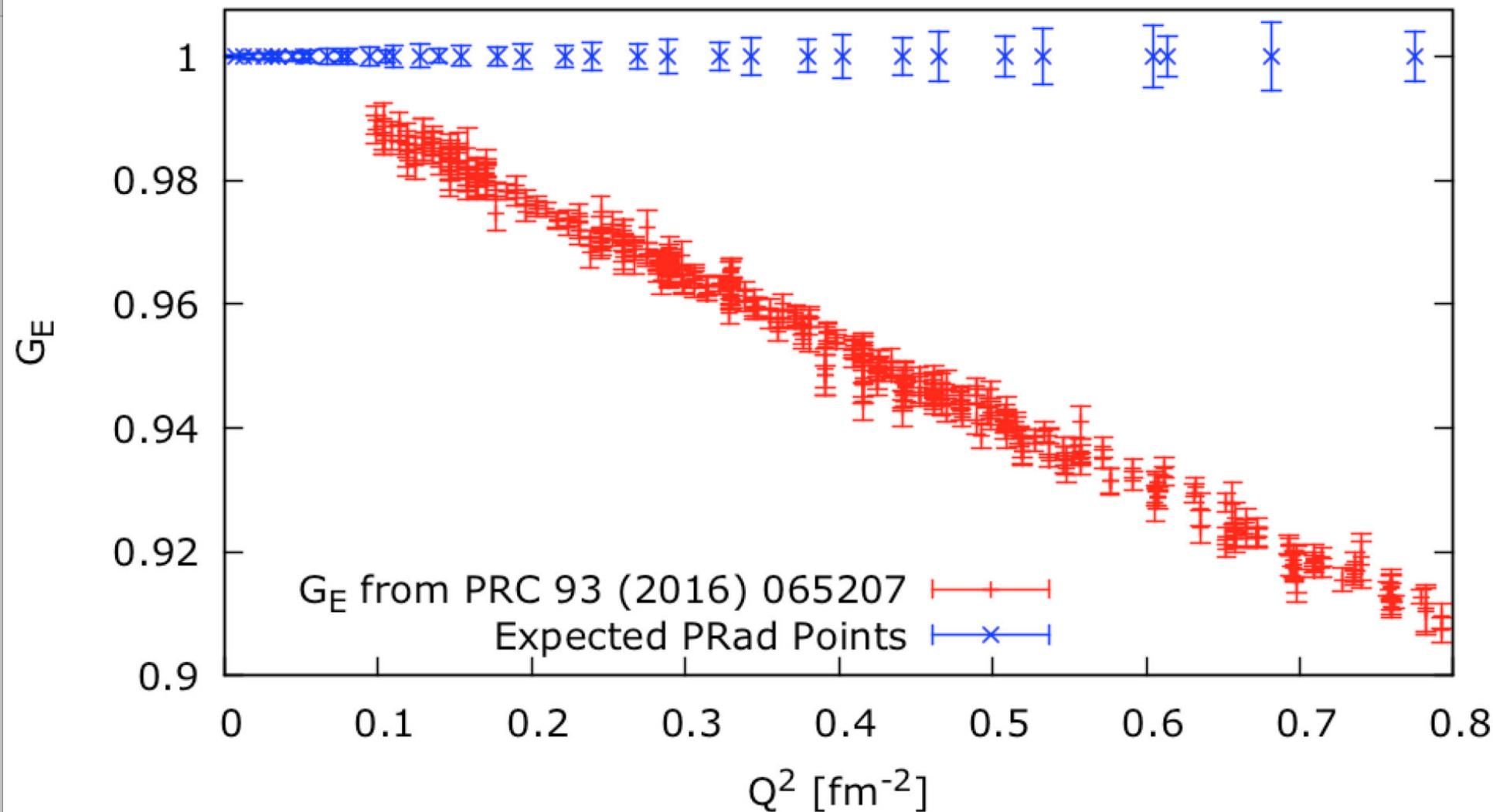
Small angle and small Q^2 to minimize the effects of G_M and provide best measurement of G_E
Gas Target (the proton) and GEM Detectors (scattering angles)



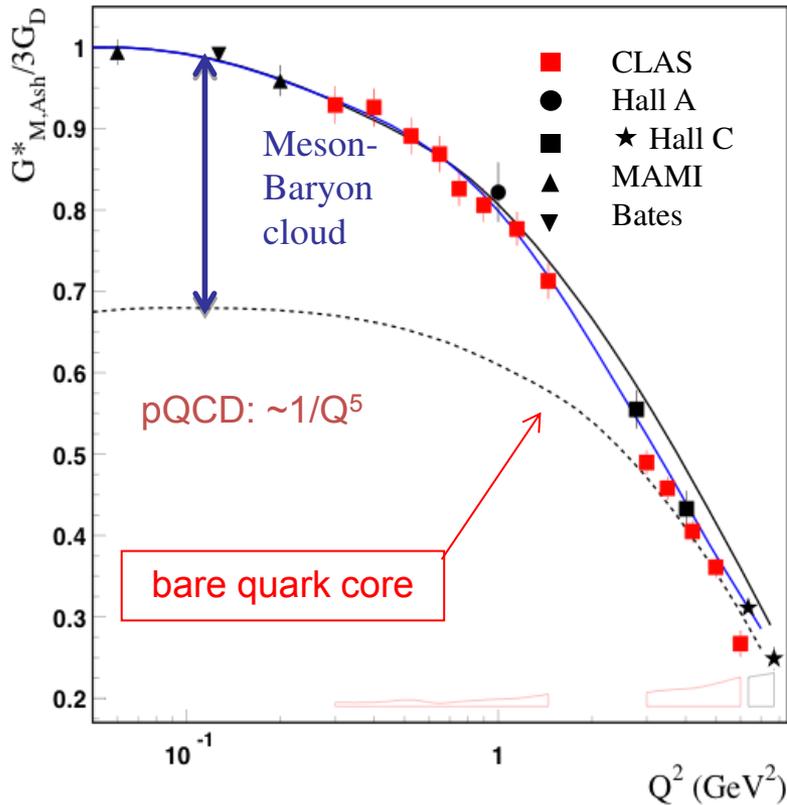
- The Collaboration & Hall B staff managed to get this experiment ready while installing CLAS12
- *The first completed experiment for the upgraded CEBAF accelerator.*



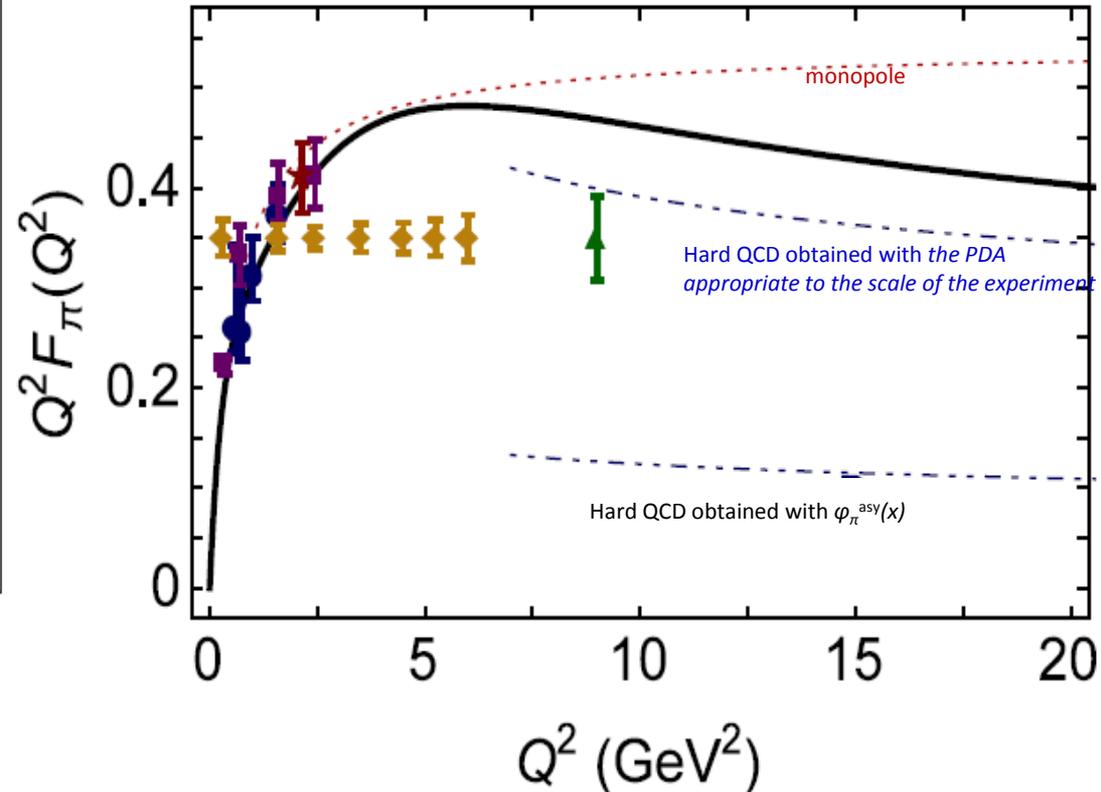
Expected Precision of PRad Data



Other Form Factors – Testing QCD in the Confinement Regime



Pion FF – first quantitative access to hard scattering scaling regime?



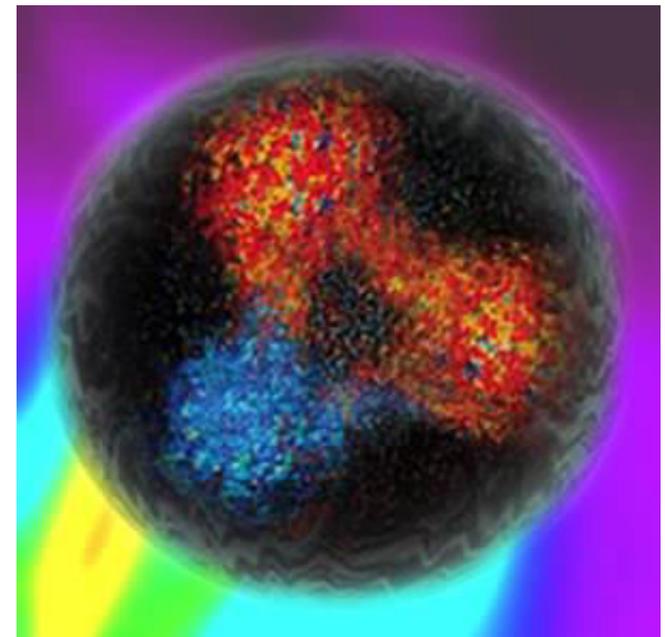
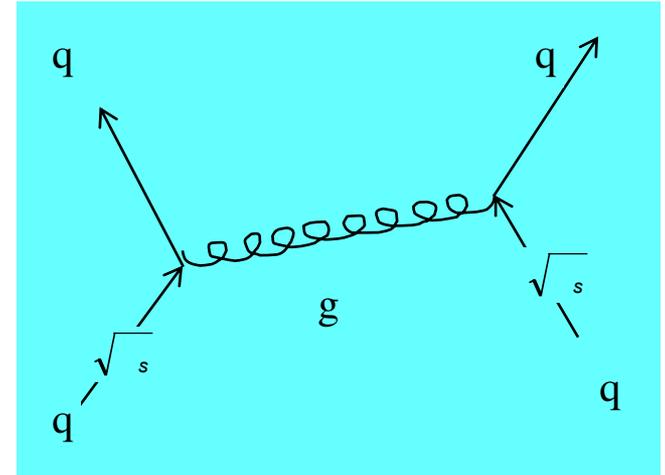
$P_{11}(1232)$ Magnetic Dipole Transition Form Factor

CLAS12 will map numerous Resonances!

Low t = four-momentum transfer squared at the nucleon vertex

QCD and the Mechanism for Confinement

- Field theory for strong interaction:
 - quarks interact by gluon exchange
 - quarks carry a ‘colour’ charge
 - exchange bosons (gluons) carry colour \Rightarrow self-interactions (cf. QED!)
- Hadrons are colour neutral:
 - $R\bar{R}$, $B\bar{B}$, $G\bar{G}$ or RGB
 - leads to confinement:
 $|q\rangle$, $|qq\rangle$ or $|qq\bar{q}\rangle$ forbidden
- Can also have gluonic excitations....



Hall D: Gluonic Excitations and the Mechanism for Confinement

QCD predicts a rich spectrum of as yet to be discovered gluonic excitations - whose experimental verification is crucial for our understanding of QCD in the confinement regime.

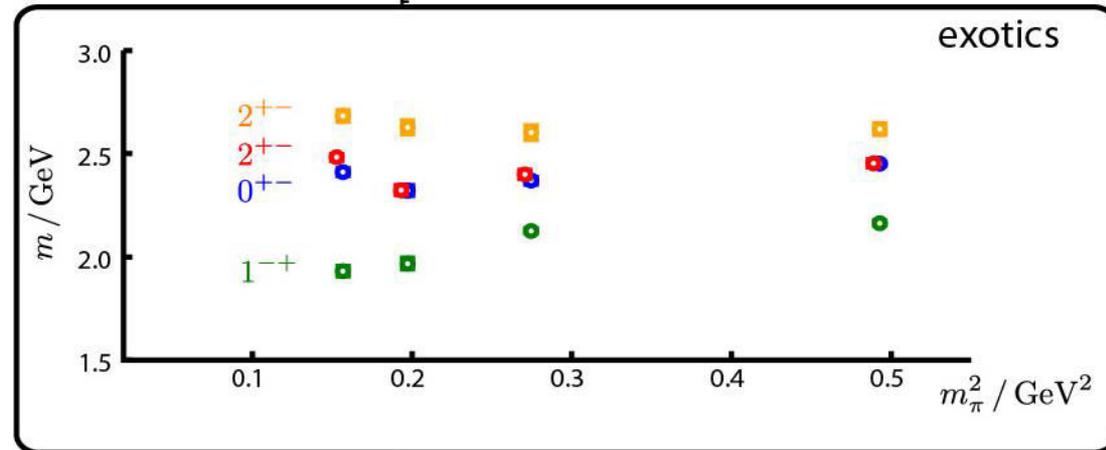
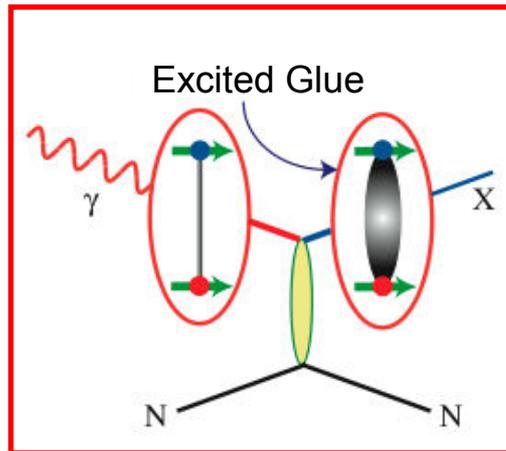
With the upgraded CEBAF, a linearly polarized photon beam, and the **GlueX detector**, Jefferson Lab will be uniquely poised to: - discover these states

- map out their spectrum
- measure their properties

12 GeV electrons

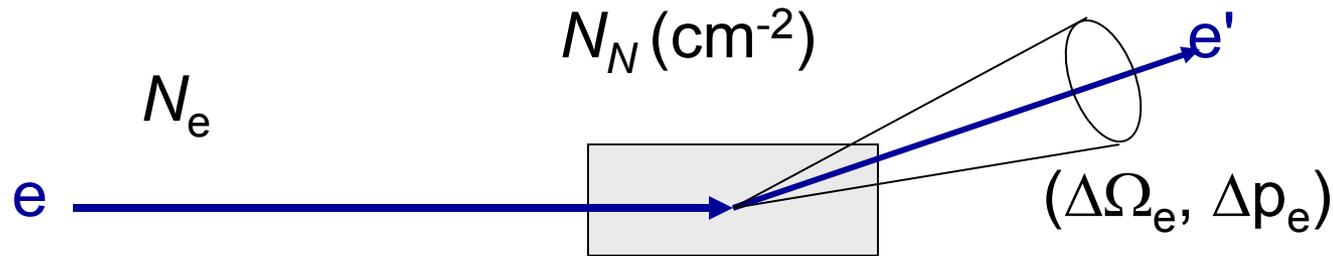
States with Exotic Quantum Numbers

Dudek et al.





Extracting the (e,e') cross section

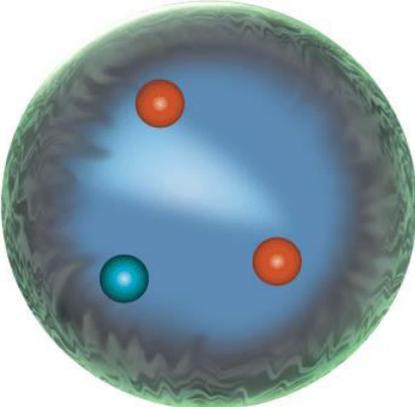


Scattering probability or cross section

$$\left\langle \frac{d^3\sigma}{d\Omega_e dp_e} \right\rangle = \frac{\text{Counts}}{N_e N_N \Delta\Omega_e \Delta p_e}$$



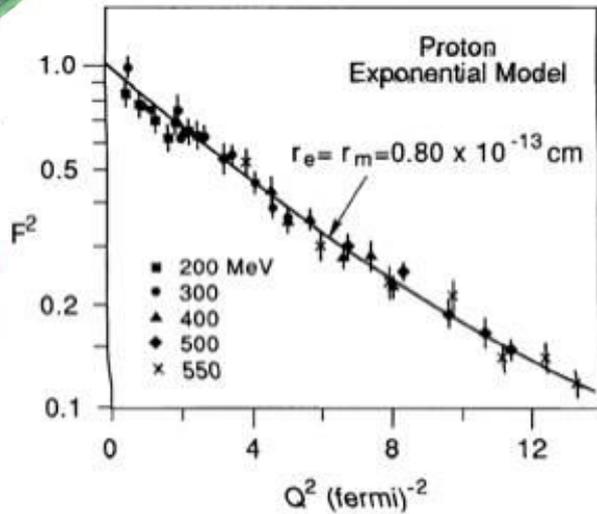
e-p and e-d elastic scattering



$$\frac{d\sigma}{d\Omega} = \frac{a^2}{4E_0^2 \sin^4 \theta/2} \cdot \cos^2 \theta/2 \cdot \frac{E'}{E_0} \left[\frac{G_E^2 + \tau G_M^2}{1 + \tau} + 2\tau G_M^2 \tan^2 \theta/2 \right]$$

Protons have charge distribution

First determination of the proton form factor



Deuterium smeared out by Fermi energy

