

# Chapter 1

1. (a) Expressing the radius of the Earth as

$$R = (6.37 \times 10^6 \text{ m})(10^{-3} \text{ km/m}) = 6.37 \times 10^3 \text{ km},$$

its circumference is  $s = 2\pi R = 2\pi(6.37 \times 10^3 \text{ km}) = 4.00 \times 10^4 \text{ km}$ .

(b) The surface area of Earth is  $A = 4\pi R^2 = 4\pi (6.37 \times 10^3 \text{ km})^2 = 5.10 \times 10^8 \text{ km}^2$ .

(c) The volume of Earth is  $V = \frac{4\pi}{3} R^3 = \frac{4\pi}{3} (6.37 \times 10^3 \text{ km})^3 = 1.08 \times 10^{12} \text{ km}^3$ .

4. (a) Using the conversion factors 1 inch = 2.54 cm exactly and 6 picas = 1 inch, we obtain

$$0.80 \text{ cm} = (0.80 \text{ cm}) \left( \frac{1 \text{ inch}}{2.54 \text{ cm}} \right) \left( \frac{6 \text{ picas}}{1 \text{ inch}} \right) \approx 1.9 \text{ picas}.$$

- (b) With 12 points = 1 pica, we have

$$0.80 \text{ cm} = (0.80 \text{ cm}) \left( \frac{1 \text{ inch}}{2.54 \text{ cm}} \right) \left( \frac{6 \text{ picas}}{1 \text{ inch}} \right) \left( \frac{12 \text{ points}}{1 \text{ pica}} \right) \approx 23 \text{ points}.$$

9. The volume of ice is given by the product of the semicircular surface area and the thickness. The area of the semicircle is  $A = \pi r^2/2$ , where  $r$  is the radius. Therefore, the volume is

$$V = \frac{\pi}{2} r^2 z$$

where  $z$  is the ice thickness. Since there are  $10^3 \text{ m}$  in  $1 \text{ km}$  and  $10^2 \text{ cm}$  in  $1 \text{ m}$ , we have

$$r = (2000 \text{ km}) \left( \frac{10^3 \text{ m}}{1 \text{ km}} \right) \left( \frac{10^2 \text{ cm}}{1 \text{ m}} \right) = 2000 \times 10^5 \text{ cm}.$$

In these units, the thickness becomes

$$z = 3000 \text{ m} = (3000 \text{ m}) \left( \frac{10^2 \text{ cm}}{1 \text{ m}} \right) = 3000 \times 10^2 \text{ cm}$$

which yields  $V = \frac{\pi}{2} (2000 \times 10^5 \text{ cm})^2 (3000 \times 10^2 \text{ cm}) = 1.9 \times 10^{22} \text{ cm}^3$ .

21. If  $M_E$  is the mass of Earth,  $m$  is the average mass of an atom in Earth, and  $N$  is the number of atoms, then  $M_E = Nm$  or  $N = M_E/m$ . We convert mass  $m$  to kilograms using Appendix D ( $1 \text{ u} = 1.661 \times 10^{-27} \text{ kg}$ ). Thus,

$$N = \frac{M_E}{m} = \frac{5.98 \times 10^{24} \text{ kg}}{(40 \text{ u})(1.661 \times 10^{-27} \text{ kg/u})} = 9.0 \times 10^{49}.$$

28. If we estimate the “typical” large domestic cat mass as 10 kg, and the “typical” atom (in the cat) as  $10 \text{ u} \approx 2 \times 10^{-26} \text{ kg}$ , then there are roughly  $(10 \text{ kg})/(2 \times 10^{-26} \text{ kg}) \approx 5 \times 10^{26}$  atoms. This is close to being a factor of a thousand greater than Avogadro’s number. Thus this is roughly a kilomole of atoms.

41. Using the (exact) conversion  $1 \text{ in} = 2.54 \text{ cm} = 0.0254 \text{ m}$ , we find that

$$1 \text{ ft} = 12 \text{ in.} = (12 \text{ in.}) \times \left( \frac{0.0254 \text{ m}}{1 \text{ in.}} \right) = 0.3048 \text{ m}$$

and  $1 \text{ ft}^3 = (0.3048 \text{ m})^3 = 0.0283 \text{ m}^3$  for volume (these results also can be found in Appendix D). Thus, the volume of a cord of wood is  $V = (8 \text{ ft}) \times (4 \text{ ft}) \times (4 \text{ ft}) = 128 \text{ ft}^3$ . Using the conversion factor found above, we obtain

$$V = 1 \text{ cord} = 128 \text{ ft}^3 = (128 \text{ ft}^3) \times \left( \frac{0.0283 \text{ m}^3}{1 \text{ ft}^3} \right) = 3.625 \text{ m}^3$$

which implies that  $1 \text{ m}^3 = \left( \frac{1}{3.625} \right) \text{ cord} = 0.276 \text{ cord} \approx 0.3 \text{ cord}$ .

47. We convert meters to astronomical units, and seconds to minutes, using

$$1000 \text{ m} = 1 \text{ km}$$

$$1 \text{ AU} = 1.50 \times 10^8 \text{ km}$$

$$60 \text{ s} = 1 \text{ min.}$$

Thus,  $3.0 \times 10^8 \text{ m/s}$  becomes

$$\left( \frac{3.0 \times 10^8 \text{ m}}{\text{s}} \right) \left( \frac{1 \text{ km}}{1000 \text{ m}} \right) \left( \frac{\text{AU}}{1.50 \times 10^8 \text{ km}} \right) \left( \frac{60 \text{ s}}{\text{min}} \right) = 0.12 \text{ AU/min.}$$