

# Chapter 23

## Electric Charge

Some observations:

- Electric charge appears to come in two "flavors." Call them
  - vanilla and chocolate
  - up and down
  - positive and negative

It doesn't matter which is which!

- Like charges repel each other while unlike charges attract each other.

One kind of charge is applied to rubber by stroking it with hair (wool, fur, human hair)

negative on rubber

positive charge on fur

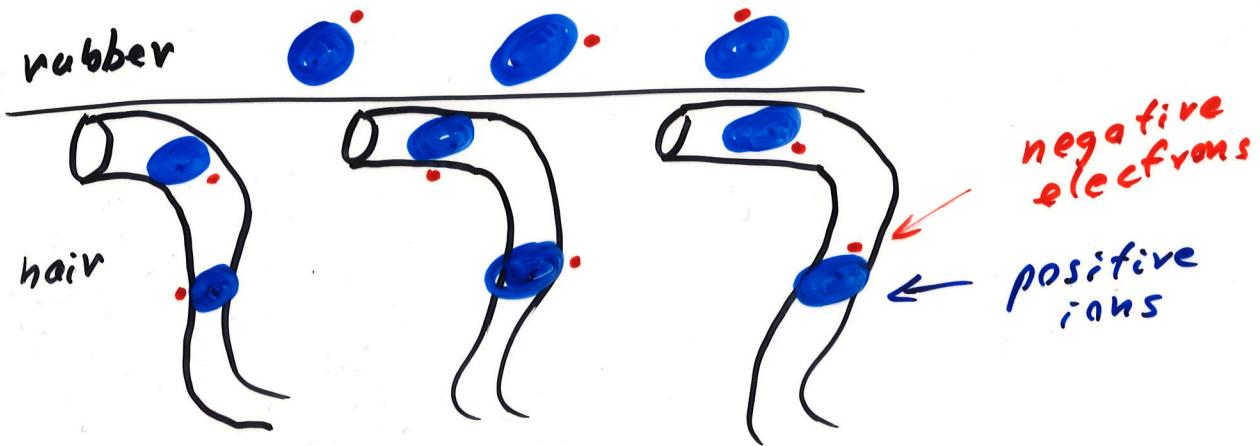
The other kind of charge is applied to glass by stroking it with silk.

positive on glass

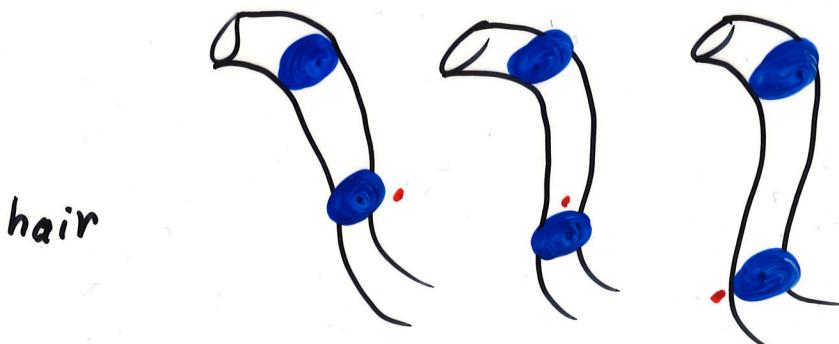
negative on silk

Charge is conserved.

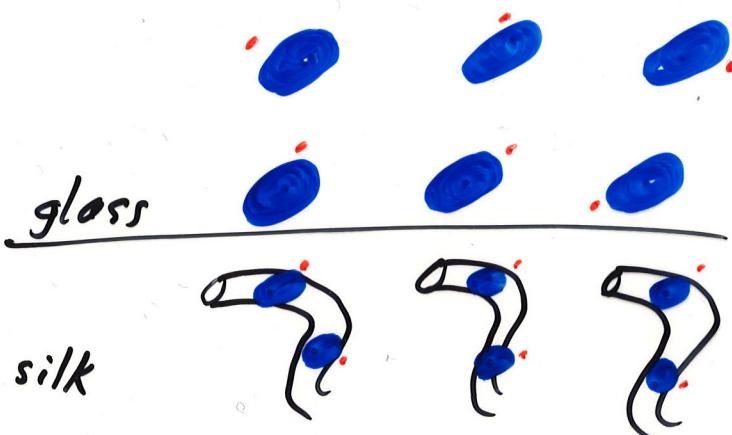
What's really going on here?  
Microscopically:



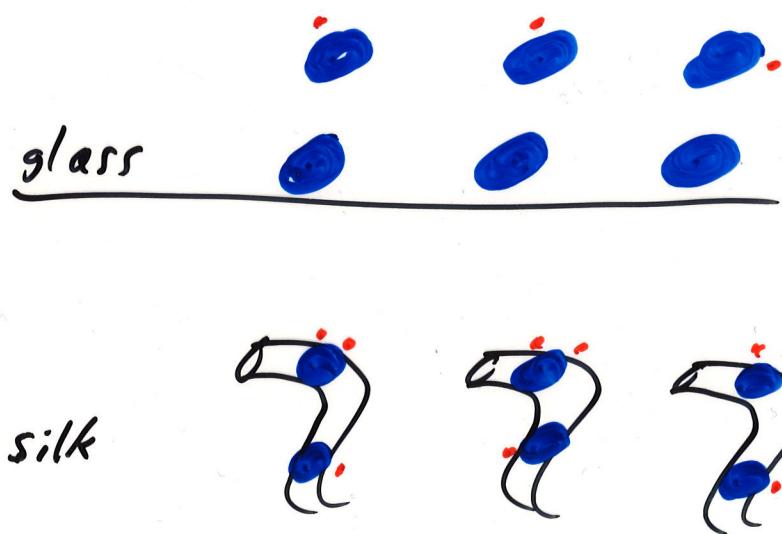
Electrons from the hair remain on the surface of the rubber. By convention, electrons are said to have negative charge.



Again, microscopically:

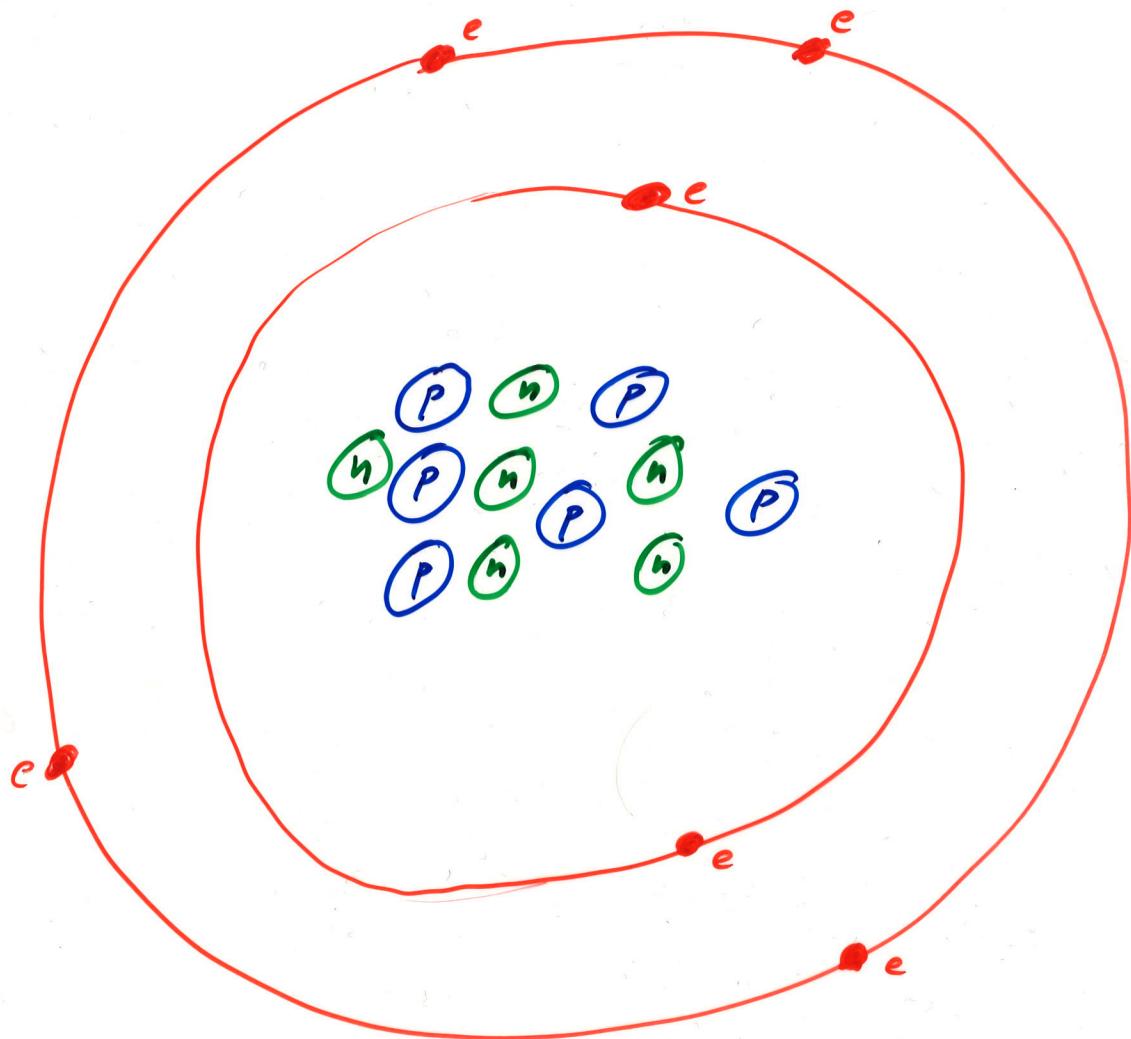


Silk removes electrons from the surface of the glass, leaving the glass positively charged.



# The Atom

(e.g. Carbon)



Not to scale!

(P) proton - positively charged

(n) neutron - zero charge (neutral)

e- electron - negatively charged

The atom is electrically neutral.

All of the forces that you studied  
in Mechanics (1303) except gravity  
were electrical in origin.

- contact forces
  - normal force
  - friction
  - viscous drag
- string tension
- Hooke's Law spring force

## More Observations

Newton's Law of Universal Gravitation

### Gravity

magnitude:  $F_G = \frac{G M_1 M_2}{(r_{12})^2}$

direction: along the line joining the masses

always attractive

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### Electric Force

Coulomb's Law

magnitude:  $F_E = \frac{k |q_1| |q_2|}{(r_{12})^2}$

direction: along the line joining the charges

attractive if  $\begin{cases} q_1 \text{ positive, } q_2 \text{ negative} \\ q_1 \text{ negative, } q_2 \text{ positive} \end{cases}$

repulsive if  $\begin{cases} q_1 \text{ positive, } q_2 \text{ positive} \\ q_1 \text{ negative, } q_2 \text{ negative} \end{cases}$

$G$  is the gravitational constant.

$$G = 6.67 \times 10^{-11} \frac{N \cdot m^2}{kg^2} \quad (\text{in MKS units})$$

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$k$  is the electrostatic constant.

$$k = 8.99 \times 10^9 \frac{N \cdot m^2}{C^2}$$

for later convenience

$$k = \frac{1}{4\pi\epsilon_0} \quad \epsilon_0 = \frac{1}{4\pi k}$$

$\epsilon_0$  (epsilon nought) is the  
permittivity of free space

$$\epsilon_0 = 8.85 \times 10^{-12} \frac{C^2}{N \cdot m^2}$$

$$F_e = \frac{1}{4\pi\epsilon_0} \frac{|q_1| |q_2|}{(r_{12})^2}$$

Vector nature of  $\vec{F}_e$

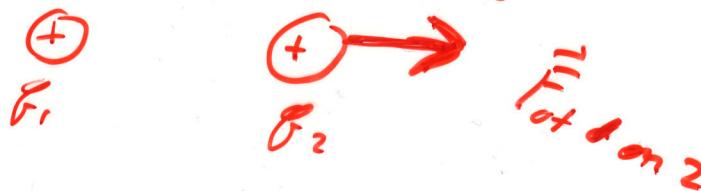
$$\vec{F}_{\text{of } 1 \text{ on } 2} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{(r_{12})^2} \hat{r}_{12}$$

$q_1, q_2$  can be positive or negative

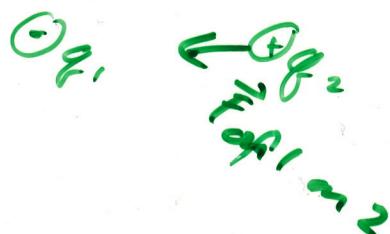
$r_{12}$  is the distance between  $q_1$  and  $q_2$

$\hat{r}_{12}$  is a unit vector pointing from  $q_1$  to  $q_2$

Ex.



$$\hat{r}_{12} \cdot \hat{r}_{12} = 1$$



# The MKS unit of charge

is the coulomb (C)

1C is an enormous amount of charge.

Ex Find the force ~~between~~ two 1C charges separated by 1 m.

$$\begin{aligned} F_e &= k \frac{(q_1)(q_2)}{(r_{12})^2} = 8.99 \times 10^9 \frac{\text{N} \cdot \text{m}^2}{\text{C}^2} \frac{(1\text{C})(1\text{C})}{(1\text{m})^2} \\ &= \approx 9 \times 10^9 \text{ N} \left( \frac{0.225 \text{ lb}}{1\text{N}} \right) \\ &= 2 \times 10^9 \text{ lbs} \left( \frac{1 \text{ ton}}{2000 \text{ lbs}} \right) \\ &= 10^6 \text{ tons.} \end{aligned}$$

The coulomb (C) is not one of the fundamental units (base units):

meter m

kilogram kg

second s

ampere A (amp) unit of current

The coulomb is a derived unit

$$1 \text{ C} = 1 \text{ A} \cdot \text{s}$$

like the newton (N)

$$1 \text{ N} = 1 \frac{\text{kg} \cdot \text{m}}{\text{s}^2}$$

Electric charge is a **scalar** quantity, like mass. The only difference is that mass is always positive while charge can be positive or negative.

Charge adds like a scalar:

Ex.  $3C + (-4C) = -1C$

Ex.  $3\text{ kg} + 5\text{ kg} = 8\text{ kg}$  (mass)

Ex.  $1.2 \text{ kg}\cdot\text{m}^2 + 2.7 \text{ kg}\cdot\text{m}^2 = 3.9 \text{ kg}\cdot\text{m}^2$

(moment of inertia  
or  
rotational inertia)

The forces on one charge due to all the rest add like vectors.

$$\vec{F}_{\text{total}} \text{ on } 1 = \vec{F}_{\text{of } 2 \text{ on } 1} + \vec{F}_{\text{of } 3 \text{ on } 1} + \dots + \vec{F}_{\text{of } 87 \text{ on } 1} + \dots$$

$$\vec{F}_{\text{of } 87 \text{ on } 1} = \frac{1}{4\pi\epsilon_0} \frac{q_{87} q_1}{(r_{87,1})^2} \hat{r}_{87,1}$$

$\hat{r}_{87,1}$  points from  $q_{87}$  to  $q_1$ .

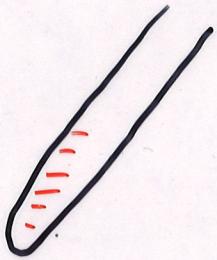
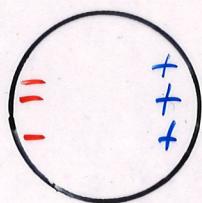
Charge  $q_1$  cannot exert a force on itself!

This additive property of the vector force is called "superposition."

Ex Consider 3 identical positive charges at the corners of an equilateral triangle of side d. What is the force on one charge due to the other two?

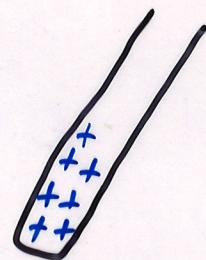
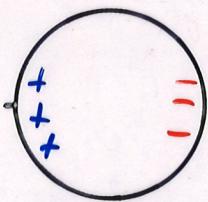
An uncharged metal can is attracted by each kind of charge, never repelled.  
What's going on?

neutral overall →



charge is  
**induced**  
(moved around)  
in the metal can.

neutral overall →

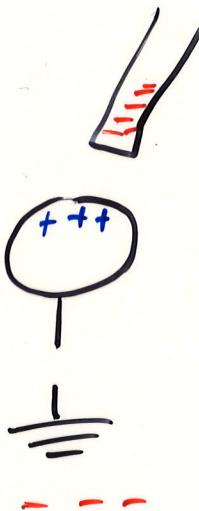
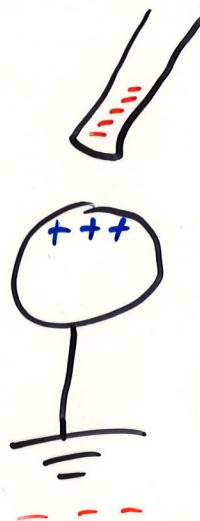
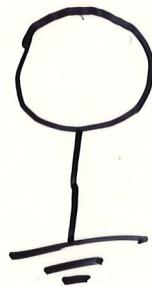


In a conductor, charge can flow freely.

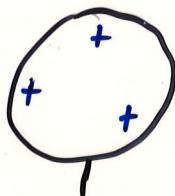
In an insulator, charge is stuck in place.

A conductor that can take as many electrons as it needs from a large supply (like the earth), or give up as many electrons as it needs is said to be **grounded**.

How to charge a conductor without touching it:



Charging by  
induction.



Ex How much charge is in you?

$m = 75 \text{ kg} = 75,000 \text{ g}$  all water

Molecular mass of water  $18_g$

I contain  $\frac{75,000_g}{18_g} = 4100$  moles  
of water

each mole  $6.02 \times 10^{23}$  molecules

I have  $2.5 \times 10^{27}$  molecules

$H_2O$       1e in H      8e in O      }  $10$  electrons  
                        in  $H_2O$  molecule

How many C of negative charge.

$$2.5 \times 10^{27} \cdot 10 \cdot \underbrace{(-1.6 \times 10^{-19} C)}_{\text{charge on electron}} \\ = -4 \times 10^9 C$$