

Doppler measurements

$$v_{1\text{ obs}} = v_1 \sin(i) \quad , \quad v_{2\text{ obs}} = v_2 \sin(i)$$

$$v_{1\text{ obs}} = \left(\frac{\text{total distance}}{\text{total time}} \right) \sin(i) = \frac{2\pi r_1}{\tau} \sin(i)$$

$$\frac{v_{1\text{ obs}}}{v_{2\text{ obs}}} = \frac{2\pi r_1 \tau \sin(i)}{2\pi r_2 \sin(i)} = \frac{r_1}{r_2} = \frac{M_2}{M_1}$$

K3: $\frac{G(M_1 + M_2)}{a^3} = \omega^2 = \left(\frac{2\pi}{\tau} \right)^2$

$$a = r_1 + r_2 \quad , \quad r_1 = \frac{v_{1\text{ obs}} \tau}{2\pi \sin(i)}$$

$$\frac{G(M_1 + M_2)}{(r_1 + r_2)^3} = \frac{G(M_1 + M_2)}{\left(\frac{\tau}{2\pi \sin(i)} \right)^3 (v_{1\text{ obs}} + v_{2\text{ obs}})^3} = \frac{(2\pi)^3}{\tau^2}$$

$$(M_1 + M_2) \sin^3(i) = \frac{(v_{1\text{ obs}} + v_{2\text{ obs}})^3 \tau}{2\pi G}$$

unknown

known (measured)