



$$f(t) = \begin{cases} t & , 0 \leq t \leq 1 \\ 2-t & , 1 \leq t \leq 3 \\ t-4 & , 3 \leq t, 4 \end{cases}$$

$$a_0 = \langle 1 | f(t) \rangle = \frac{2}{T} \int_{t=0}^T 1 f(t) dt$$

$$= \frac{1}{2} \left[\int_{t=0}^1 1 \cdot t dt + \int_{t=1}^3 1 (2-t) dt + \int_{t=3}^4 1 \cdot (t-4) dt \right]$$

$$= \frac{1}{2} \left[\left. \frac{t^2}{2} \right|_0^1 + \left. \left(2t - \frac{t^2}{2} \right) \right|_1^3 + \left. \left(\frac{t^2}{2} - 4t \right) \right|_3^4 \right]$$

$$= \frac{1}{2} \left[\left(\frac{1}{2} - 0 \right) + \left(\frac{3}{2} - \frac{3}{2} \right) + \left(-8 + 7\frac{1}{2} \right) \right] = 0$$

$$a_n = \langle \cos(n\omega t) | f(t) \rangle = 0$$

$$b_n = \langle \sin(n\omega t) | f(t) \rangle = \propto \frac{1}{n^2}$$

expect $\frac{1}{2}$ of these $\Rightarrow 0$