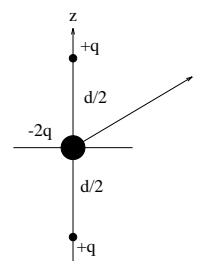


1. Show how to recover the field for the discrete case from the expression for the field in the continuous case using $\rho(\vec{r}) = \sum_i q_i \delta^3(\vec{r} - \vec{r}_i)$.

2. Prove that

$$\frac{\vec{r} - \vec{r}'}{|\vec{r} - \vec{r}'|^3} = -\vec{\nabla} \left(\frac{1}{|\vec{r} - \vec{r}'|} \right) .$$

This is most easily done by writing $\vec{r} = \sum_i x_i \vec{e}_i$, $\vec{r}' = \sum_i x'_i \vec{e}_i$ (with $\vec{e}_i \cdot \vec{e}_j = \delta_{ij}$), and noting that in Cartesian coordinates $\vec{\nabla} = \sum_i \vec{e}_i \frac{\partial}{\partial x_i}$.



3. Consider the distribution of point charges shown in the diagram.
 - (a) What is the charge density $\rho(\vec{r})$ for the system?
 - (b) What is the potential $\Phi(\vec{r})$?
 - (c) Find the leading non-zero term for $r \gg d$.
 - (d) What is the power of $(\frac{d}{r})$ in the next term after the one above?
 - (e) Take the limits $q \rightarrow \infty$ and $d \rightarrow 0$ so that the first term is finite but all other terms vanish ("point quadrupole"). What must be the relationship between q and d for this result to occur?
4. Calculate the first three multipole tensors (monopole, dipole, and quadrupole) of a uniformly charged spheroid whose symmetry semi-axis is a and whose transverse semi-axis is b . The charge density ρ is constant within the spheroid and zero without. The equation for the surface of the spheroid is

$$\begin{aligned} x &= b \sin \theta \cos \phi \\ y &= b \sin \theta \sin \phi \\ z &= a \cos \theta \end{aligned} \quad \text{or} \quad \frac{x^2}{b^2} + \frac{y^2}{b^2} + \frac{z^2}{a^2} = 1 .$$

