Vector Bosons at Hadron Colliders

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CTEQ-Fermilab School Pontificia Universidad Católica del Perú - August 2012

INTRODUCTION

Vector Bosons in the SM, Weak Currents, TGCs

DRELL-YAN PROCESSES

Clean Signals at HC's, Factorization, Precision Observables

PAIR PRODUCTION

V+gamma, Radiation Zero, Quantum Corrections, Tools

ASSOCIATE PRODUCTION WITH JETS

Jets, V+Jets at Tevatron & LHC, Polarization

$$\mathcal{L}_{SM} = \begin{array}{c} \mathcal{L}_{YM} + \mathcal{L}_{f} + \mathcal{L}_{H} + \mathcal{L}_{Yuk} & \text{Yang-Mills Piece} \\ \mathcal{L}_{YM} = \mathcal{L}_{QCD} + \mathcal{L}_{I_{w}} + \mathcal{L}_{Y} \\ = -\frac{1}{4} \sum_{a=1}^{8} G_{\mu\nu}^{a} G^{a\mu\nu} - \frac{1}{4} \sum_{i=1}^{3} F_{\mu\nu}^{i} F^{i\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} \\ \hline \text{Color} & \text{Weak Isospin} & \text{Hypercharge} \\ \text{SU(3)} & \text{SU(2)} & \text{U(1)} \end{array}$$

$$\mathcal{L}_{SM} = \mathcal{L}_{YM} + \mathcal{L}_{f} + \mathcal{L}_{H} + \mathcal{L}_{Yuk} \quad \text{Yang-Mills Piece}$$

$$\mathcal{L}_{YM} = \mathcal{L}_{QCD} + \mathcal{L}_{I_{w}} + \mathcal{L}_{Y}$$

$$= -\frac{1}{4} \sum_{a=1}^{8} G^{a}_{\mu\nu} G^{a\mu\nu} - \frac{1}{4} \sum_{i=1}^{3} F^{i}_{\mu\nu} F^{i\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu}$$

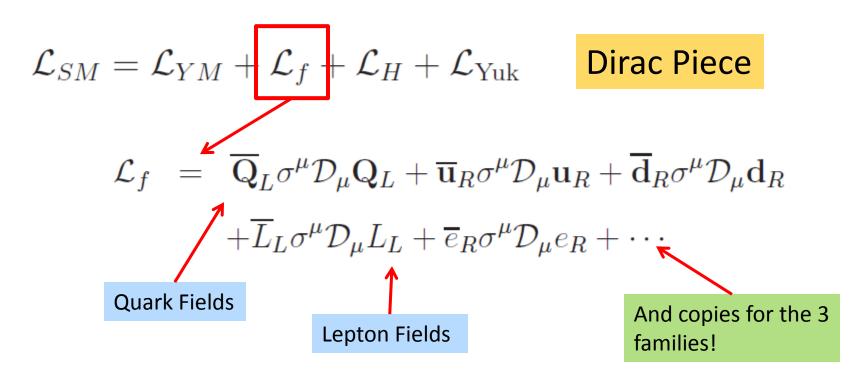
$$G^{a}_{\mu\nu} = \partial_{\mu} A^{a}_{\nu} - \partial_{\nu} A^{a}_{\mu} + g_{1} f^{abc} A^{b}_{\mu} A^{c}_{\nu} \quad \text{Combinations the W's and B}$$

Where the Field Stregth Tensors are:

$$F^i_{\mu\nu} = \partial_\mu W^i_\nu - \partial_\nu W^i_\mu + g_2 \epsilon^{ijk} W^j_\mu W^k_\nu$$

$$B_{\mu\nu} = \partial_{\mu}B_{\nu} - \partial_{\nu}B_{\mu}$$

Combinations of the *W*'s and *B* gauge fields give rise to the physical Weak Vector Bosons and the photon



$$\mathcal{L}_{SM} = \mathcal{L}_{YM} + \mathcal{L}_{f} + \mathcal{L}_{H} + \mathcal{L}_{Yuk} \quad \text{Dirac Piece}$$

$$\mathcal{L}_{f} = \overline{\mathbf{Q}}_{L} \sigma^{\mu} \mathcal{D}_{\mu} \mathbf{Q}_{L} + \overline{\mathbf{u}}_{R} \sigma^{\mu} \mathcal{D}_{\mu} \mathbf{u}_{R} + \overline{\mathbf{d}}_{R} \sigma^{\mu} \mathcal{D}_{\mu} \mathbf{d}_{R}$$

$$+ \overline{L}_{L} \sigma^{\mu} \mathcal{D}_{\mu} L_{L} + \overline{e}_{R} \sigma^{\mu} \mathcal{D}_{\mu} e_{R} + \cdots$$

Each fermion field have 7 a corresponding covariant derivative:

$$\mathcal{D}_{\mu}\mathbf{Q}_{L} = (\partial_{\mu} + g_{1}\frac{i}{2}A_{\mu}^{a}\lambda^{a} + g_{2}\frac{i}{2}W_{\mu}^{i}\tau^{i} + g_{3}\frac{i}{2}y_{1}B_{\mu})\mathbf{Q}_{L} ,$$

$$\mathcal{D}_{\mu}\mathbf{u}_{R} = (\partial_{\mu} + g_{1}\frac{i}{2}A_{\mu}^{a}\lambda^{a} + g_{3}\frac{i}{2}y_{2}B_{\mu})\mathbf{u}_{R} ,$$

$$\mathcal{D}_{\mu}\mathbf{d}_{R} = (\partial_{\mu} + g_{1}\frac{i}{2}A_{\mu}^{a}\lambda^{a} + g_{3}\frac{i}{2}y_{3}B_{\mu})\mathbf{d}_{R} ,$$

$$\mathcal{D}_{\mu}L_{L} = (\partial_{\mu} + g_{2}\frac{i}{2}W_{\mu}^{i}\tau^{i} + g_{3}\frac{i}{2}y_{4}B_{\mu})L_{L} ,$$

$$\mathcal{D}_{\mu}e_{R} = (\partial_{\mu} + g_{3}\frac{i}{2}y_{5}B_{\mu})e_{R}$$

$$\mathbf{6}$$

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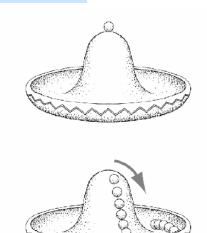
$$\begin{split} \mathcal{L}_{SM} &= \mathcal{L}_{YM} + \mathcal{L}_f + \mathcal{L}_H + \mathcal{L}_{Yuk} & \text{Higgs Lagrangia} \\ \mathcal{L}_H &= (\mathcal{D}_{\mu} H)^{\dagger} (\mathcal{D}^{\mu} H) - V(H) \end{split}$$

With *H* a complex scalar weak isospin doublet:

$$H = \begin{pmatrix} H_1 \\ H_2 \end{pmatrix}$$

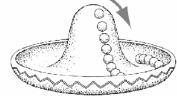
 $V(H) = \mu^2 H^{\dagger} H + \lambda (H^{\dagger} H)^2$

And the Higgs potential given by:



Source of the Spontaneous Symmetry Breaking $(SU(2)XU(1) \rightarrow U(1))$ in the SM

$$\mathcal{L}_{SM} = \mathcal{L}_{YM} + \mathcal{L}_f + \mathcal{L}_H + \mathcal{L}_{Yuk} \qquad \text{Higgs Lagrangian}$$
$$\mathcal{L}_H = (\mathcal{D}_\mu H)^\dagger (\mathcal{D}^\mu H) - V(H)$$
Pick a minimum and expand around it:
$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+h \end{pmatrix}$$
And you end up with effective mass terms the



And you end up with effective mass terms the (weak) gauge fields:

$$\frac{1}{2}(0,v) \left| \frac{1}{2} g_2 W^i_{\mu} \tau^i + \frac{1}{2} g_3 B_{\mu} \right|^2 \begin{pmatrix} 0 \\ v \end{pmatrix}$$

$$\begin{split} \mathcal{L}_{SM} &= \mathcal{L}_{YM} + \mathcal{L}_f + \mathcal{L}_H + \mathcal{L}_{Yuk} & \text{Higgs Lagrangian} \\ \mathcal{L}_H &= (\mathcal{D}_{\mu} H)^{\dagger} (\mathcal{D}^{\mu} H) - V(H) \end{split}$$

With the physical Weak gauge bosons and the photon given by:

$$W_{\mu}^{\pm} = \frac{1}{\sqrt{2}} (W_{\mu}^{1} \mp i W_{\mu}^{2}) ,$$

$$Z_{\mu} = \frac{-g_{3}B_{\mu} + g_{2}W_{\mu}^{3}}{\sqrt{g_{2}^{2} + g_{3}^{2}}} ,$$

$$A_{\mu} = \frac{g_{2}B_{\mu} + g_{3}W_{\mu}^{3}}{\sqrt{g_{2}^{2} + g_{3}^{2}}} ,$$
With Masses:
$$M_{W}^{2} = \frac{1}{4}g_{2}^{2}v^{2} ,$$

$$M_{Z}^{2} = \frac{1}{4}(g_{2}^{2} + g_{3}^{2})v^{2} ,$$

$$M_{A}^{2} = 0$$

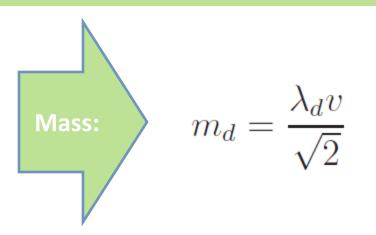
$$M_{W} = 80.4 \text{ GeV}$$

$$M_{Z} = 91.2 \text{ GeV}$$
with $v \approx 174\sqrt{2} \text{ GeV}$

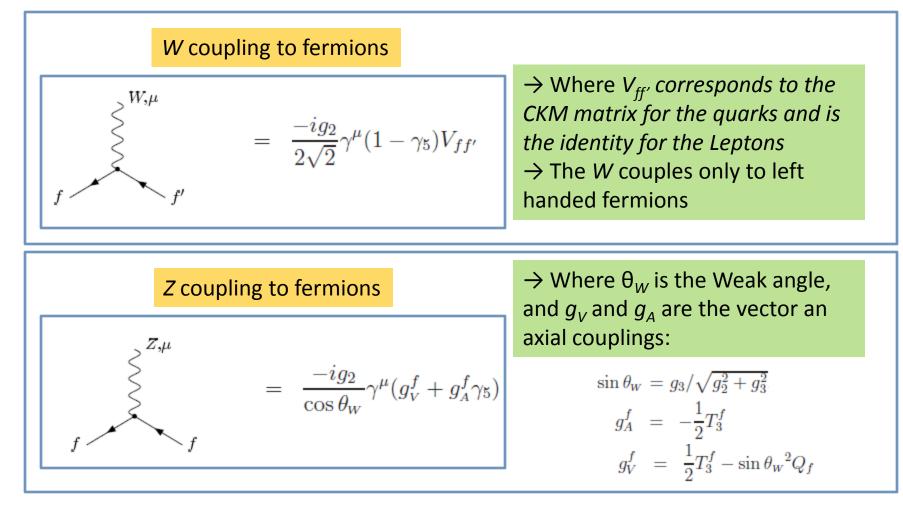
$$\mathcal{L}_{SM} = \mathcal{L}_{YM} + \mathcal{L}_f + \mathcal{L}_H + \mathcal{L}_{Yuk}$$
Yukawa Interactions
$$-\lambda_d \overline{\mathbf{Q}}_L H \mathbf{d}_R + h.c.$$

Yukawa coupling

Which in an economical way end up producing, through the Spontaneous Symmetry breaking, effective masses for the fermion fields!

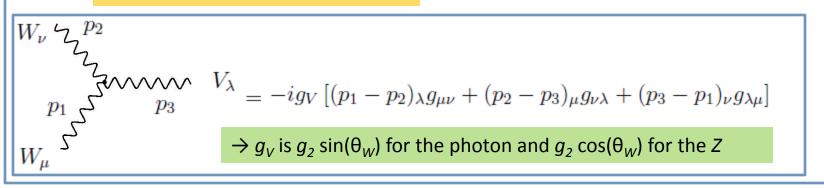


Electro Weak Gauge Bosons Interactions

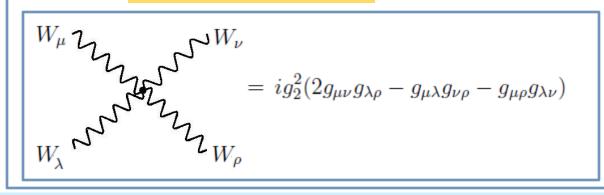


More Interactions...

Triple gauge boson interactions



Four point interactions



 \rightarrow There are more four point interactions of the WWVV type

 \rightarrow The photon couples to fermions as in QED (that is with strength proportional to the fermion charge)

 \rightarrow Although the gluon is of course also a Vector Boson, its phenomenology is set $_{12}$ apart due to QCD confinement

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Vector Bosons

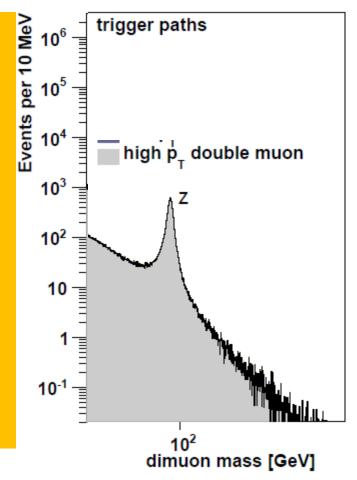
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Drell-Yan Process: Z/W Production

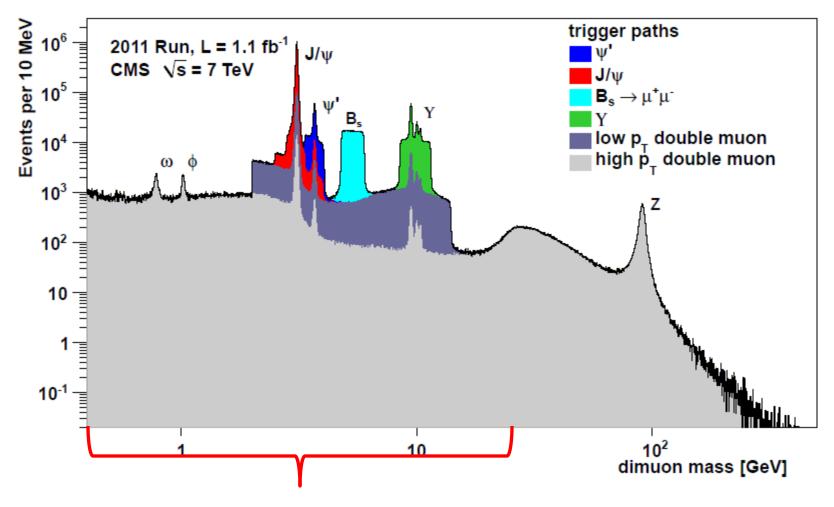
→ Clean Signal at Hadron Colliders:
 lepton pair does not interact strongly
 → Proof of factorization at all orders
 → Then an input for PDF extraction
 → One of the best theoretically
 studied processes at Hadron Colliders
 with uncertainties down to few
 percent level
 → Standard Candle for detector

- → Standard Candle for detector calibration
- \rightarrow Used for Luminosity

measurements

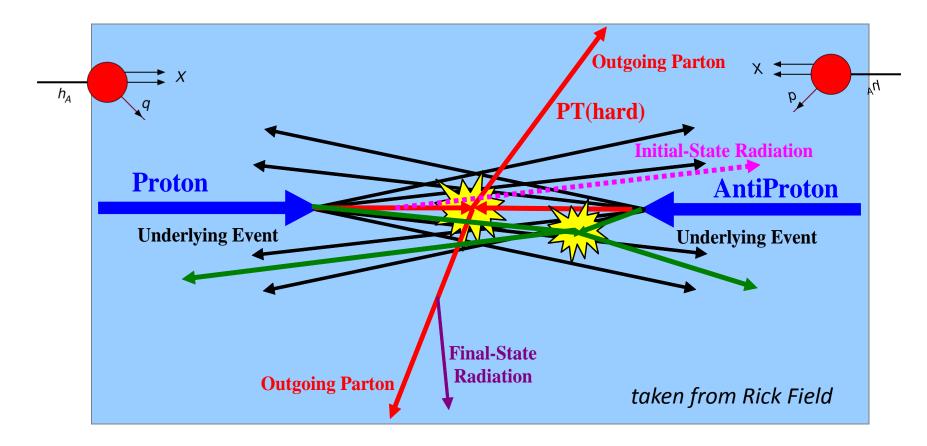


Drell-Yan Process: Z/W Production

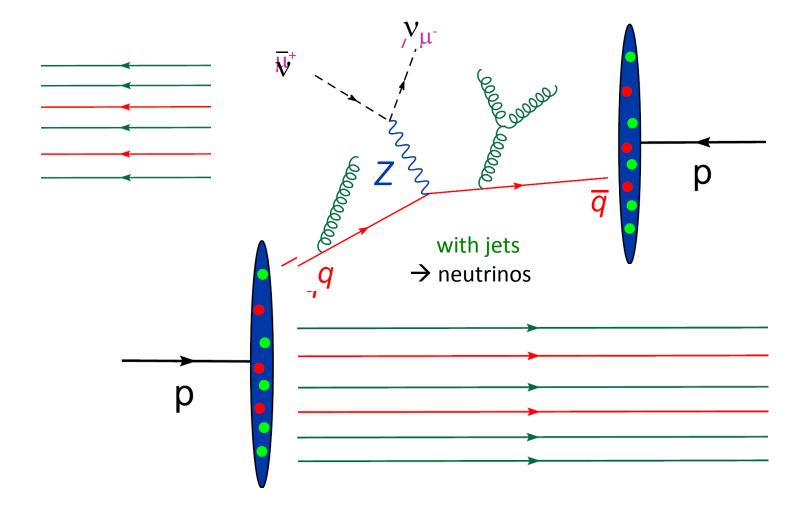


Non perturbative effects in the spectrum...

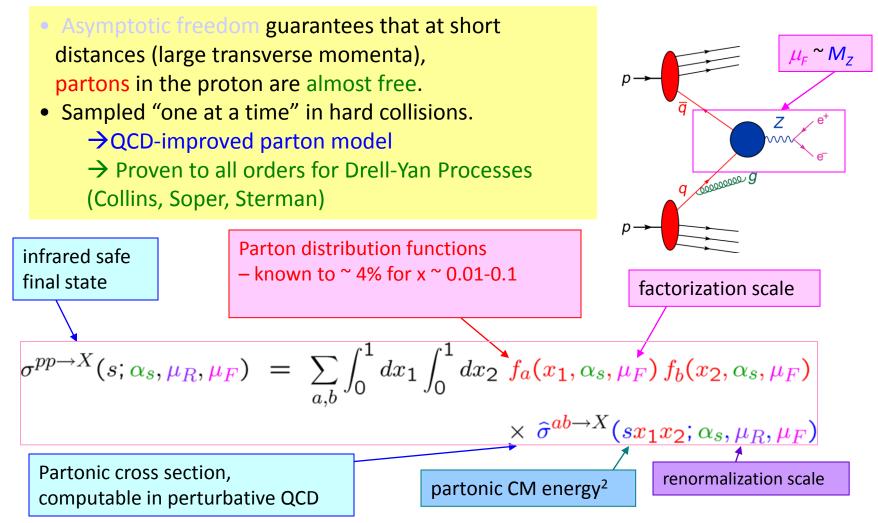
Scattering processes at hadron colliders: **A multi-layered problem**



A Closer Look to the Hard Scattering



QCD Factorization & Parton Model



Partonic Cross Section
in Perturbation Theory

$$\hat{\sigma}(\alpha_s,\mu_F,\mu_R) = [\alpha_s(\mu_R)]^{n_{\alpha}} \left[\hat{\sigma}^{(0)} + \frac{\alpha_s}{2\pi} \hat{\sigma}^{(1)}(\mu_F,\mu_R) + \left(\frac{\alpha_s}{2\pi}\right)^2 \hat{\sigma}^{(2)}(\mu_F,\mu_R) + \cdots \right]$$

LO NLO NNLO

Problem: Leading-order, tree-level predictions only qualitative DØ, 0.4 fb⁻¹ due to **poor convergence** Z/γ* Rapidity of expansion in $\alpha_s(\mu)$ **NNLO** DØ Run II Data -NNLO, MRST '04 i²σ/dM/dY [pb/GeV] (setting $\mu_R = \mu_F = \mu$) 15 NLO (2007)0.2 Example: *Z* production at Tevatron Distribution in rapidity Y 10 $Y = rac{1}{2} \ln \left(rac{E+p_z}{E-p_z}
ight)$ $rac{d\sigma}{dY}$ has $n_lpha = 0$ LO 0.1 ۵ 1.5 0.5 2 2.5 -2 still ~50% corrections, LO \rightarrow NLO [Anastasiou, Dixon, Melnikov, Petriello hep-ph/0312266]

Drell-Yan Precision

 \rightarrow Inclusive NNLO QCD corrections

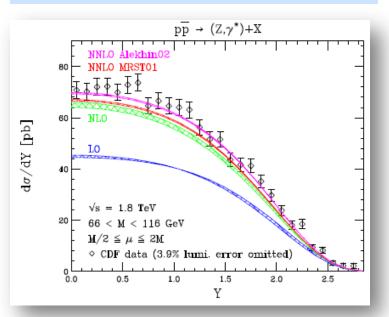
know for some time

- → Fully exclusive NNLO QCD results available
- → NLO Electroweak and QED corrections
- → Many efforts toward exact mixed EW-QCD and QED-QCD corrections...

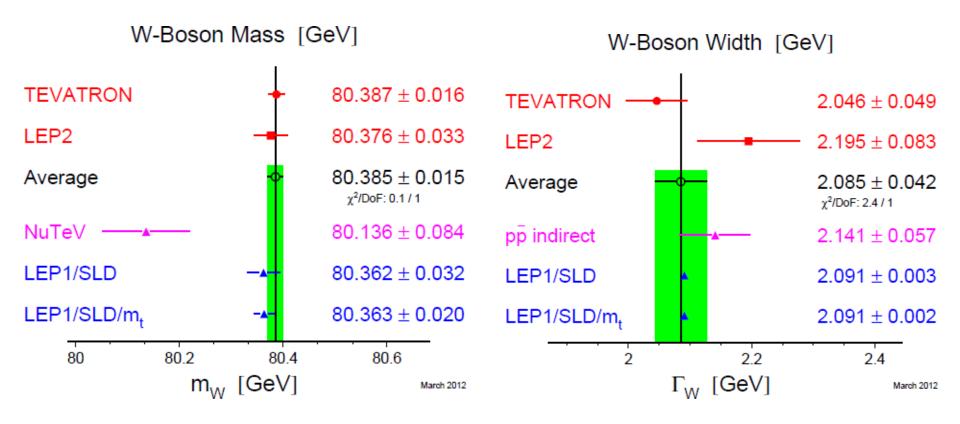
All this leaves the theory uncertainty for Drell-Yan observables at the few percent level! Hamberg, van Neerven, Matsuura (1991)

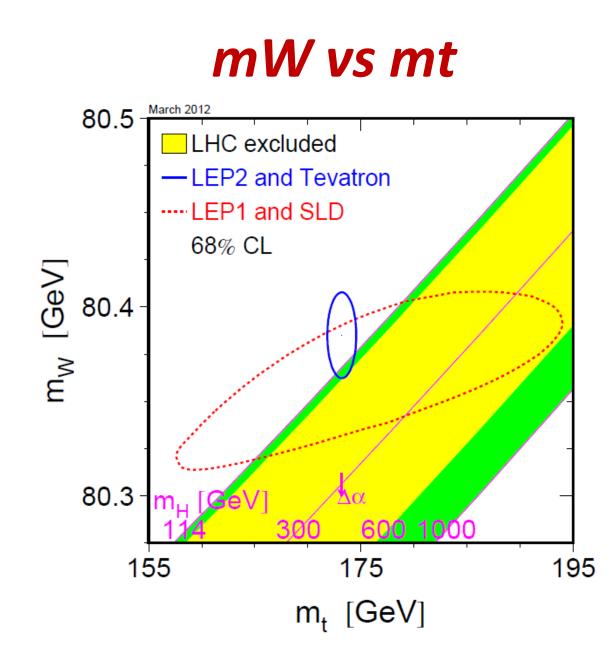
See for example: Gavin, Li, Petriello, Quackenbush (2012) ; Catani, Cieri, Ferrera, de Florian, Grazzini (2009)

See for example: Baur, Keller, Wackeroth (1999) ; Dittmaier, Kramer (2002) ; Calame, Montagna, Nicrosini (2006)



Some Observables





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Vector Bosons

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TESTING GAUGE STRUCTURE IN THE SM

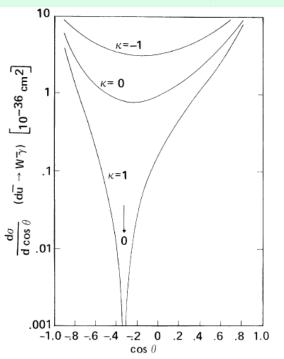
$$q_{i}(k_{1})\overline{q}_{j}(k_{2}) \rightarrow W^{\pm}(p)\gamma(k)$$
This process allows to measure the trilinear WWy coupling
$$q_{i}(k_{1}) \xrightarrow{W^{\pm}(p)}_{q_{j}(k_{2})} = \bigoplus_{(a)} + \bigoplus_{(a)} + \bigoplus_{(b)} + \bigoplus_{(c)} +$$

24

 $\cos \theta$

A CURIOUS RADIATION ZERO

Mikaelian, Samuel, Sahdev; PRL 1979



 Θ is the angle between W^{-} and d

Bern, Carrasco, Johansson ; arXiv:0805.3993

For $cos \theta = -1/3$; the diff cross section vanishes!

Goebel, Halzen, Levielle; PRD 1981

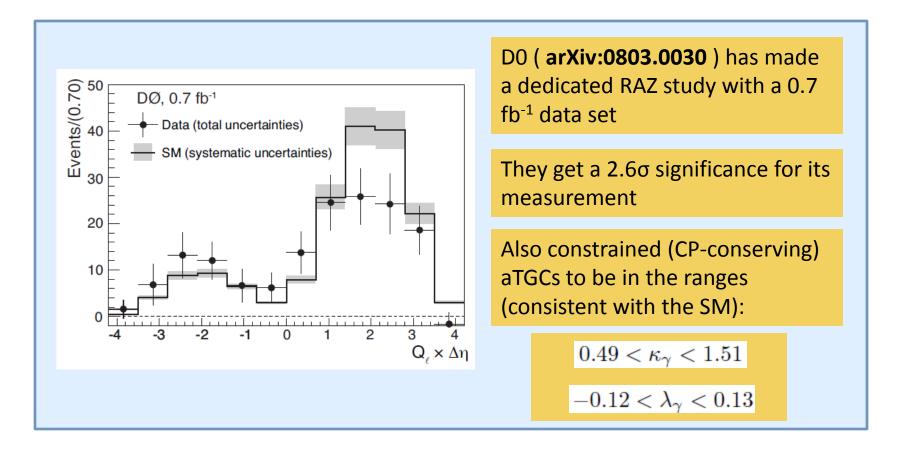
Actually the amplitude vanishes, due to factorization properties!

Indeed they prove that by general properties (mom conservation, on-shellness, charge conservation) 4-point gauge amplitudes can be arranged in forms like:

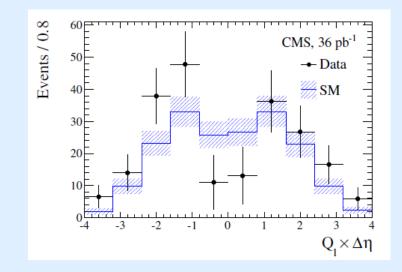
Almost 3 decades later, the "spatial generalized Jacobi identity" used by GHL in their study, would be generalized to higher point amplitudes within the so called BCJ identities: Useful tool for gauge and gravity amplitudes!

RADIATION AMPLITUDE ZERO MEASURED!

At the hadron level the RAZ shows as a dip in the ($\eta_e - \eta_{\gamma}$) distribution. QCD corrections reduce slightly its size. Possible aTGCs basically wash it out.



OTHER RECENT WY AND ZY MEASUREMENTS



CMS (arXiv:1105.2758) has made Wy and Zy measurement with a 36 $pb^{\text{-1}}$ data set

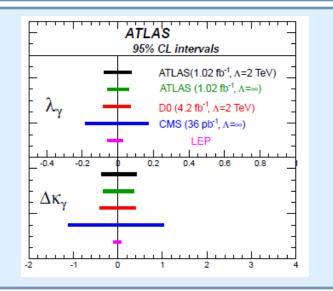
They see agreement with the SM prediction of a RAZ

Constrained (CP-conserving) aTGCs (WWγ, ZZγ and Zγγ)

ATLAS (arXiv:1106.1592, arXiv:1205.2531) has made Wγ and Zγ measurement with a 1.02 fb⁻¹ data set

Made a dedicated study of total and diff cross sections

Discusses Wy / Zy ratios. Don't show RAZ study.



QUANTUM CORRECTIONS TO Wy and Zy PRODUCTION

Original work on the impact of QCD corrections in Wγ production was performed by Smith, Thomas and van Neerven in the late 80's

Ohnemus also studied Wy and added QCD corrections to Zy production

Studies of QCD corrections for general TGCs

Fully differential studies at NLO

Fully differential (partial) Electroweak corrections

Smith, Thomas, van Neerven; Z.phys.C 1989

Ohnemus; PRD 1991

Baur, Han, Ohnemus; PRD 1993

de Florian, Signer ; hep-ph/0002138

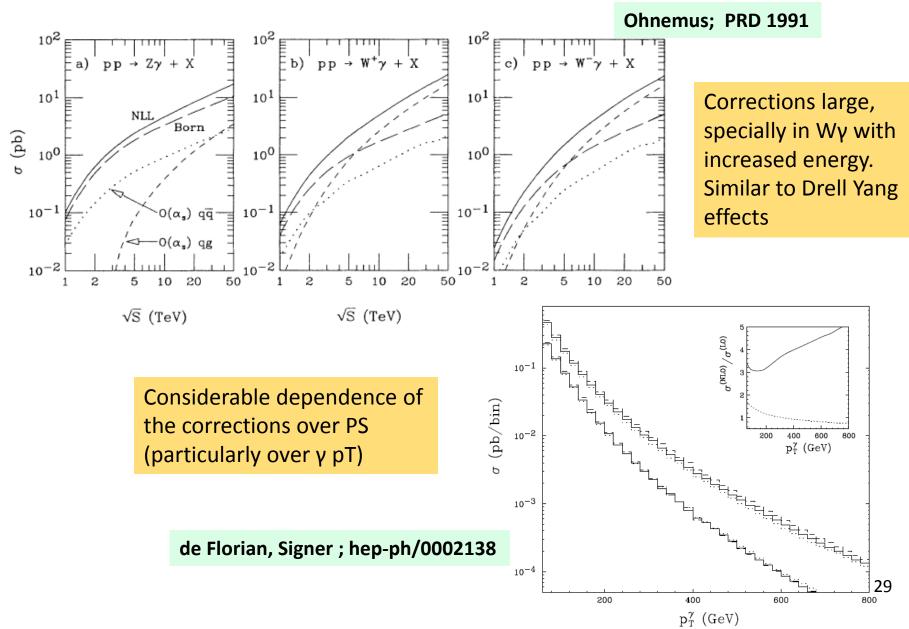
Hollik, Meier ; hep-ph/0402281 Accomando, Denner, Meier ; hep-ph/0509234

Recent update on general Vector Boson Pair production (including γ radiation from leptons)

Campbell, Ellis, Williams; arXiv:1105.0020

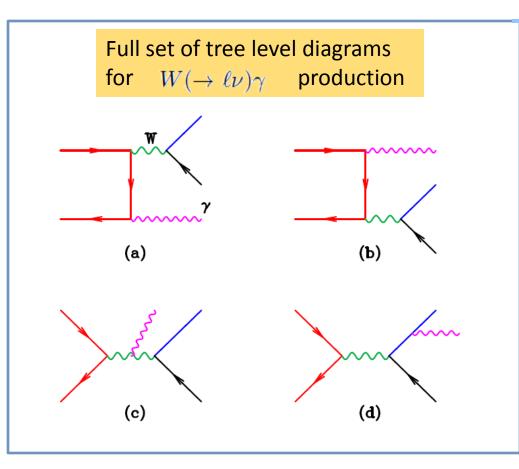
INCLUDED INTO MCFM (v6.0): A PARTON LEVEL NLO MONTECARLO PROGRAM

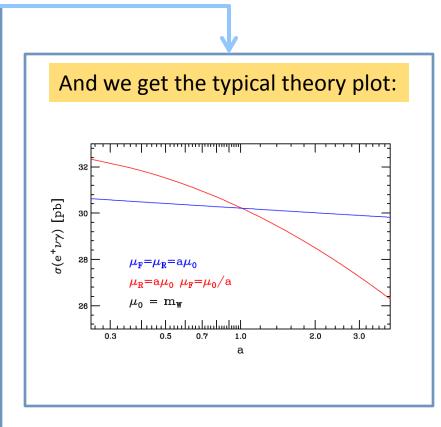
QCD CORRECTIONS: BRIEF RECOUNT



TOOLS: Wy Production At The LHC

Campbell, Ellis, Williams; arXiv:1105.0020

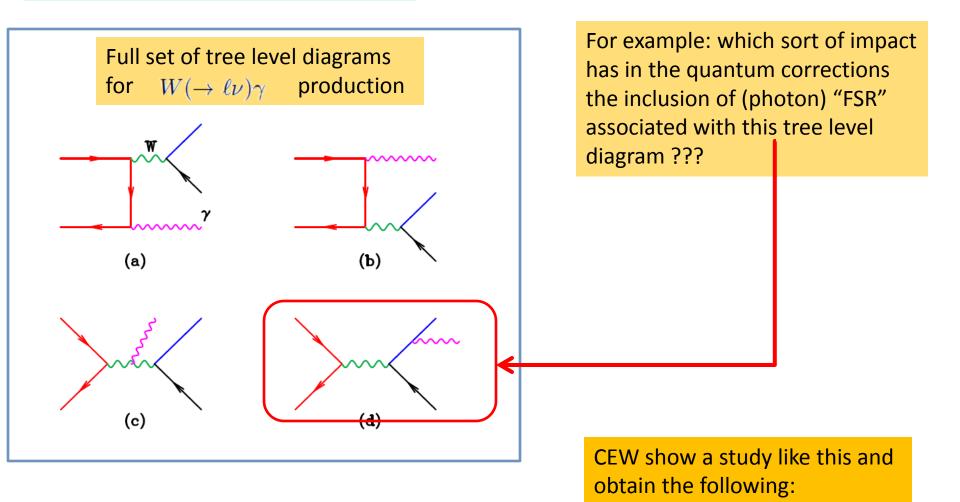




But we might be interested into learn much more than just scale dependence!!!

TOOLS: Wy Production At The LHC

Campbell, Ellis, Williams; arXiv:1105.0020



TOOLS: Wy Production At The LHC

Campbell, Ellis, Williams; arXiv:1105.0020

APPLY THESE DIFFERENT SET OF CUTS

 $\begin{array}{l} \text{Basic Photon}: \, p_T^{\gamma} > 10 \,\, \text{GeV}, \,\, |\eta_{\gamma}| < 5, \,\, R_{\ell\gamma} > 0.7, \,\, R_0 = 0.4, \,\, E_T^{max} = 3 \,\, \text{GeV}. \\ M_T \,\, \text{cut} : \, \text{Basic Photon} + M_T > 90 \,\, \text{GeV}. \end{array}$

Lepton cuts : M_T cut + $E_T^{\text{miss}} > 25$ GeV, $p_T^{\ell} > 20$ GeV, $|\eta_{\ell}| < 2.5$.

	Decay	Cuts	$\sigma^{LO}(e^+\nu\gamma)$	$\sigma^{NLO}(e^+\nu\gamma)$	- L
	No FSR	Basic γ	4.88	8.74	-
AND LOOK AT THE		M_T cut	1.99	3.78	
TOTAL RATES:		Lepton cuts	1.49	2.73	L
	Full	Basic γ	23.0	30.1	
		M_T cut	2.12	3.94	
		Lepton cuts	1.58	2.85	_

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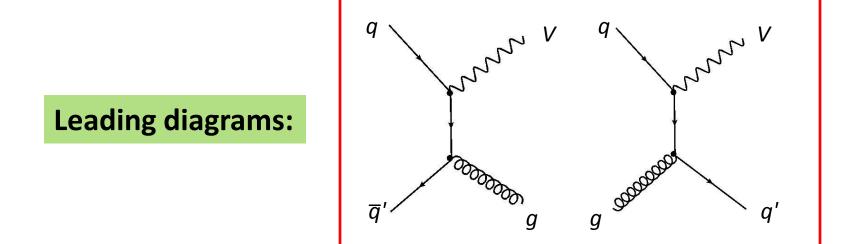
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Vector Bosons

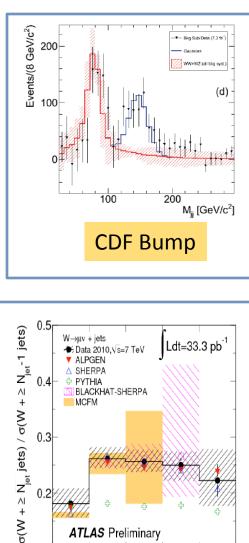
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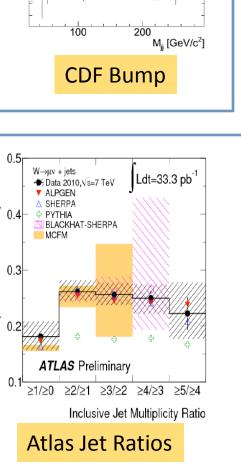
V Production in Association with Jets

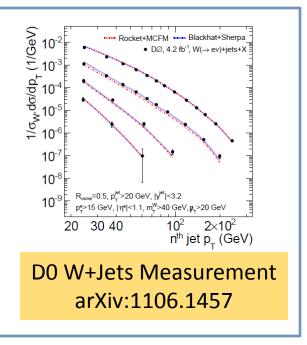
- → More exclusive processes involving Weak Vector Bosons
- \rightarrow Of key importance for testing both the SM and collider detectors
- \rightarrow Associated to many signals of BSM
- → Important progress in tools for precise studies in W+1 jet at NNLO QCD and for NLO QCD correction with large jet multiplicity

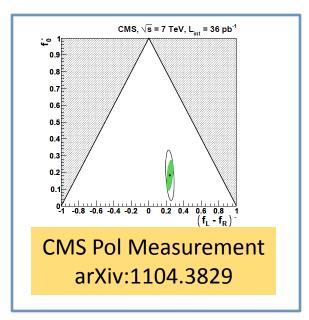


V+JETS: A IMPORTANT SIGNAL

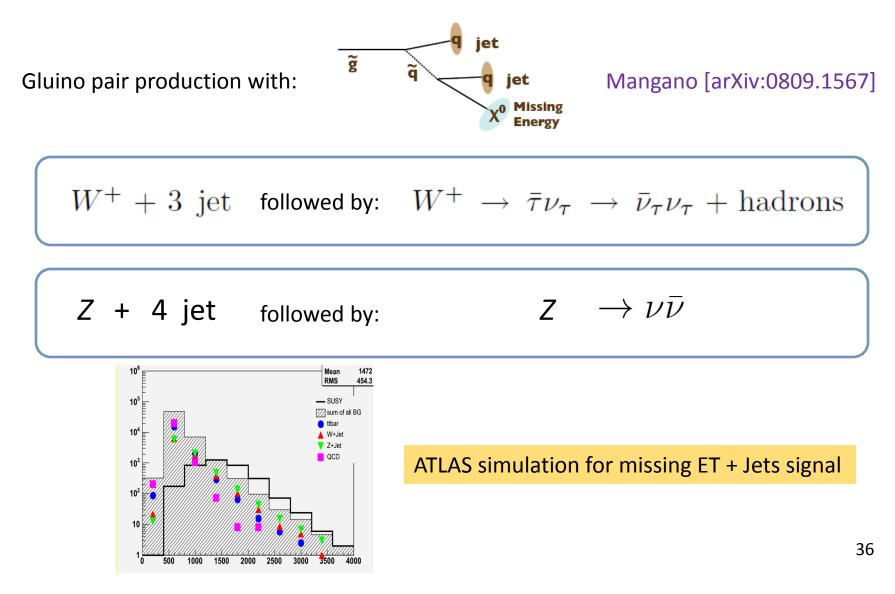






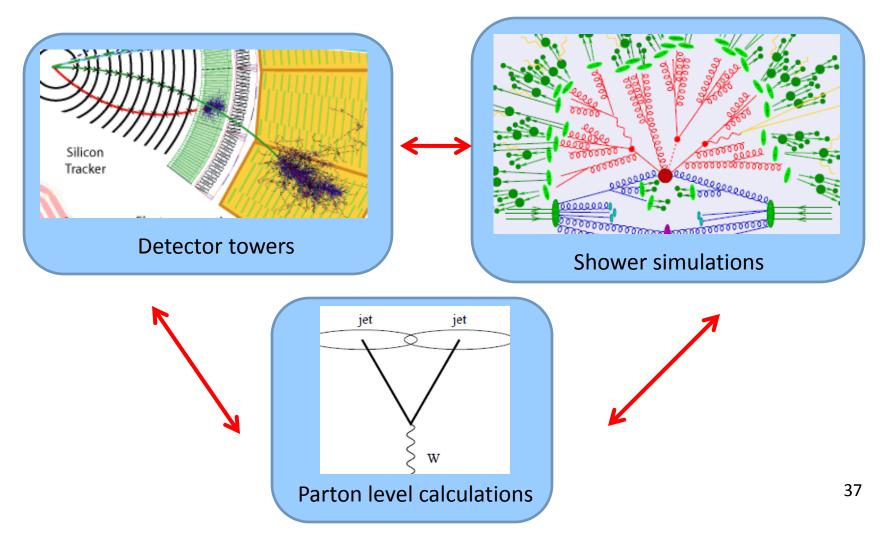


V + Jets at NLO for SUSY Searches



Jets

• Definition of complex objects



Jets: Cones vs. Recombination

✓ Cone algorithms

- ✓ Intutitive, clear jet structure
- Complicated; problems with IR safety
- Solved by SiSCone
- ✓ Recombination algorithms (k_T etc)
 - ✓ Simple, IR safe
 - × Messy jet structure
 - ✓ Solved by anti-k_T

Salam, Soyez [arXiv:0704.0292]

Cacciari, Salam, Soyez [arXiv:0802.1189]

IR Safe Jet Algorithms

In the past, performance of implementations of IR safe jet algorithms, kept them away from practical use at hadron colliders: for example with the "standard" N³ scaling of the kt algorithm, or the naive 2^N of seedless cone algorithms

Great progress in recent years:

- •Sequential recombination algorithms as kt / Cambrige-Aachen / anti-kt [4 have been implemented with h *N ln (N)* scaling
- •A seedless infrared safe cone algorithm, SISCone, has appeared with N² In (N) scaling

[Cacciari, Salam hep-ph/0512210]

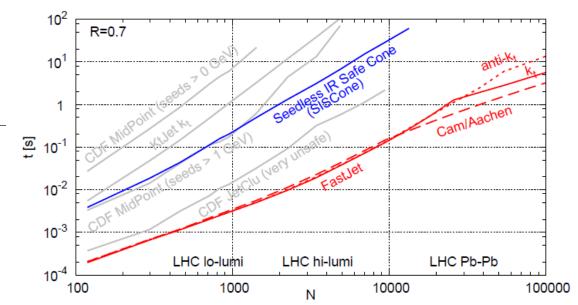
[Salam, Soyez arXiv:0704.0292]

Available within FatJet http://fastjet.fr

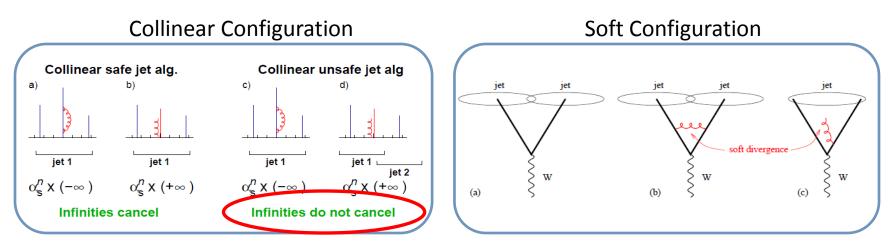
Some typical event multiplicities at colliders:

Type of event	N
e^+e^- event on the Z peak	50
Tevatron ($\sqrt{s} = 1.96 \text{ TeV}$) dijet event	200
LHC ($\sqrt{s} = 14 \text{ TeV}$) dijet event	500
LHC low-luminosity event (5 pileup collisions)	1000
LHC high-luminosity event (20 pileup collisions)	4000
RHIC Au Au event ($\sqrt{s} = 200 \text{ GeV/nucleon}$)	3000
LHC Pb Pb event ($\sqrt{s} = 5.5 \text{ TeV/nucleon}$)	30000

[Salam arXiv:0906.1833]



The need of IR safety

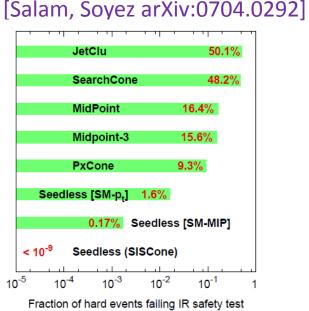


→ IRC unsafety makes data / pertubative calculation comparison hard (if at all meaningful)
 → Indeed, quantum corrections become useless for large enough multiplicity!

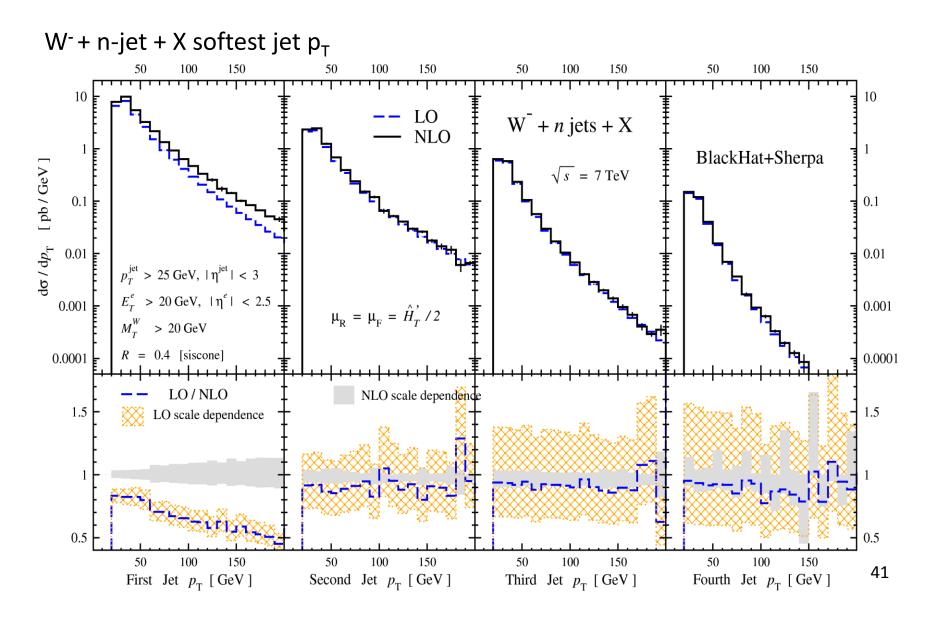
Observable	1st miss cones at	Last meaningful order
Inclusive jet cross section	NNLO	NLO
W/Z/H + 1 jet cross section	NNLO	NLO
3 jet cross section	NLO	LO
W/Z/H + 2 jet cross section	NLO	LO
jet masses in 3 jets, $W/Z/H + 2$ jets	LO	none

Testing IR safety of some commonly used cone algorithms

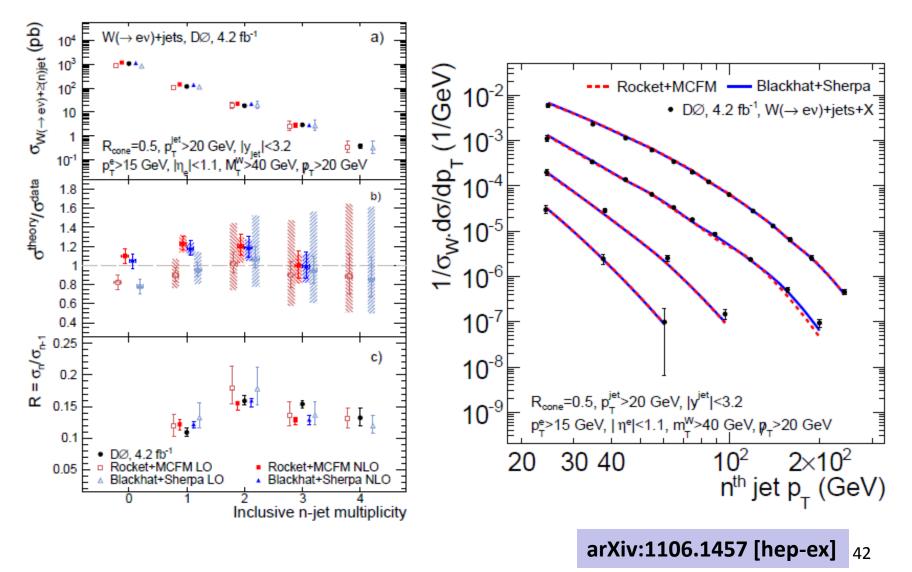
Both ATLAS and CMS use IR safe algorithms in their analyses!



 $pp \rightarrow W + 1,2,3,4$ -jets



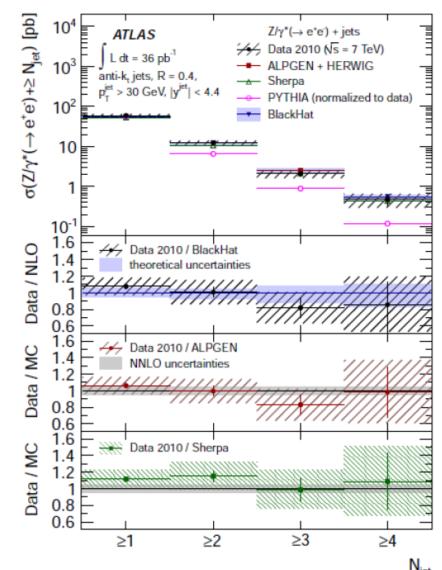
W+Jets at the Tevatron



Z+Jets at the LHC

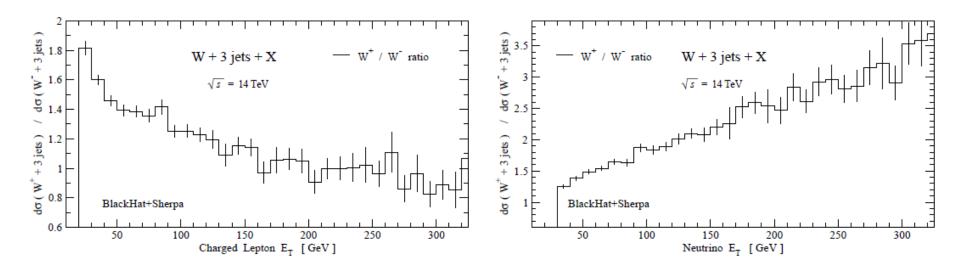
•36 pb-1 Inclusive cross section for each Multiplicity Good agreement of NLO with the data all the way to four jets

ArXiv:1111.2690



Leptonic E_T in W + 3 jets at LHC

[Berger, et al arXiv:0907.1984]

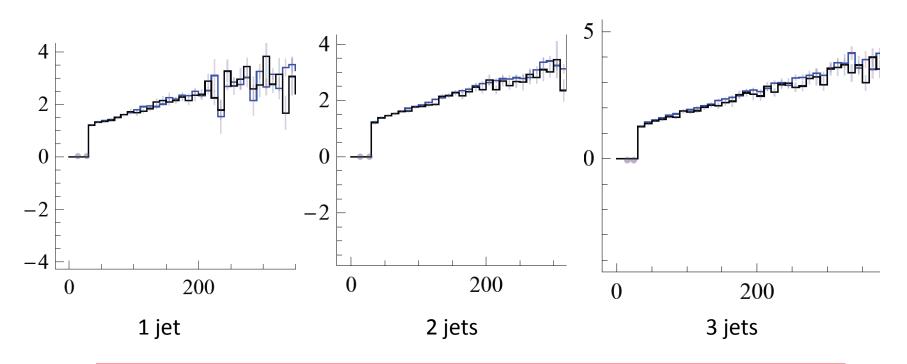


 W^+/W^- transverse lepton ratios trace a remarkably large and stable left-handed W polarization at large $p_T(W)$

- independent of number of jets
- useful to separate W + n jets from top, maybe also from new physics

 $W^{+/-}$ + n jets: Neutrino E_{τ}

NLO LO



Effect independent of multiplicity! Almost no difference from NLO and LO!

Similarly for charged lepton E_{τ}

Top quark pairs very different

Main production channels are CP invariant:

$$gg \to t\overline{t} \qquad q\overline{q} \to t\overline{t}$$

Semi-leptonic decay involves (partially) left-handed W^+

$$t\overline{t} \to bW^+\overline{b}W^- \to b\,e^+\nu\,\overline{b}jj$$

But conjugate decay involves (same degree) right-handed W⁻

$$t\bar{t} \to bW^+\bar{b}W^- \to bjj\,\bar{b}\,e^-\bar{\nu}$$

 \rightarrow electron and positron have almost identical p_T distributions

→ A nice handle on separating W+jets from top



W->µv candidate in 7 TeV collisions

Run Number: 152221, Event Number: 383185 Date: 2010-04-01 00:31:22 CEST $PT(\mu+) = 29 \text{ GeV}, \eta = 0.66$ ETmis = 24 GeV MT = 53 GeV

To be continued...

Few More Topics on Weak Vector boson production will also appear when we review tomorrow recent advancement on Higher Order Tools and Techniques...

Backup Slides...

ELECTROWEAK CORRECTIONS: BRIEF RECOUNT

