

PHYS 1303

EXEMPLARY SOLUTION

Problem

You are driving into St. Louis and in the distance you see the famous Gateway-to-the-West arch. From your guide book you know that this monument rises to a height of 192m. You estimate your line of sight with the top of the arch to be 3 degrees above the horizontal. Approximately how far in kilometers are you from the base of the arch?

Solution (DIANA)

DEFINITIONS – define symbols for unknowns sought and data given

DIAGRAM – label with your symbols, include a directed coordinate system

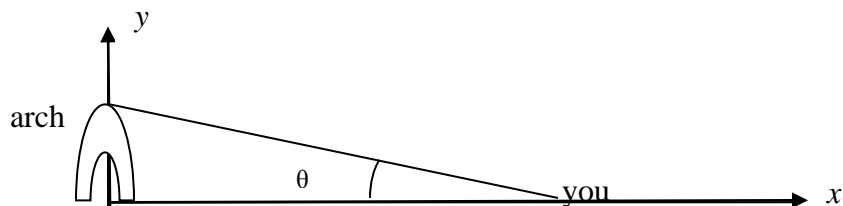
IDEA – what fundamental idea/equation will you use?

ALGEBRA – symbolically derive the unknown you want

NUMBERS – substitute data for the knowns.

ANSWER – round to appropriate precision, put units

D



Knowns: y = height of arch = 192 m, θ = angle of sight = 3°

Unknown: x = horizontal distance from base of arch

I

$$\tan \theta = \text{Opp/Adj} = y / x$$

A

Hint: put one line above the other, do not snake algebra across the page

$$\begin{aligned} x \tan \theta &= y \\ x &= y / \tan \theta \end{aligned}$$

N

$$\begin{aligned} x &= 192 / \tan 3^\circ \\ &= 192 / 0.05 = 3840 \end{aligned}$$

A

Hint: use precision from the least precise data used

$$\underline{x = 4 \text{ km (1 s.f.)}}$$