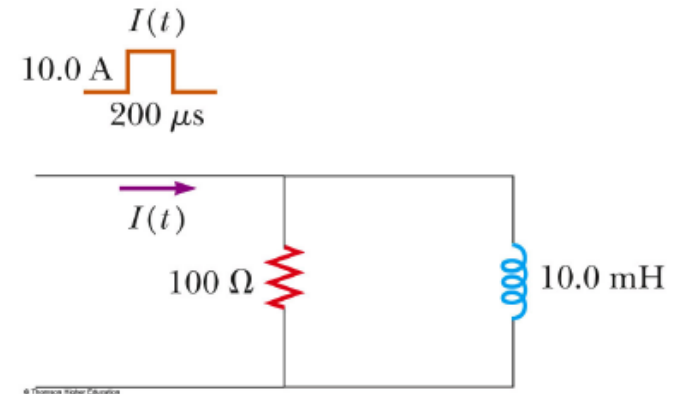


HW9Key

1. A current pulse is fed to the partial circuit shown in the figure. The current pulse is 10.0 A and its duration is from $t = 0$ to $t = 200 \mu\text{s}$. Determine the current in the inductor and the resistor as a function of time.



First, $0 < t < 200 \mu\text{s}$, we have two differential equations: (I_1 is the current go through the inductor and I_2 is the current go through resistor.

$$L \frac{dI_1}{dt} = I_2 R$$

$$I_1 + I_2 = 10$$

Solve these equations(with initial condition: $I_1=0$ when $t = 0$), we will get:

$$I_1 = 10 - 10e^{-\frac{R}{L}t} = \boxed{10 - 10e^{-1 \times 10^4 t}}$$

$$I_2 = 10e^{-\frac{R}{L}t} = \boxed{10e^{-1 \times 10^4 t}}$$

Second, $t > 200 \mu s$ ($200 \mu s = 2 \times 10^{-4} s$)

$$I_1 = I_2 = I_{1@200\mu s} \times e^{-\frac{R}{L}t} = \left(10 - 10e^{-1 \times 10^4 \times 2 \times 10^{-4}}\right) \times e^{-1 \times 10^4 t}$$
$$= \boxed{9e^{-1 \times 10^4 t}}$$

2. A $1.00 \mu\text{F}$ capacitor is fully charged with a 40.0 V power supply. The capacitor is then connected in parallel to a 10.0 mH inductor. Find the maximum current in the circuit.

Energy conserve

$$\frac{1}{2}CV^2 = \frac{1}{2}LI^2 \Rightarrow I = \sqrt{\frac{CV^2}{L}} = \sqrt{\frac{1 \times 10^{-6} \times 40^2}{10 \times 10^{-3}}} = \boxed{0.4(A)}$$