

44. Since the energy absorbed by the lake equals the solar power times the time, $\Delta t = \Delta Q/P = mc\Delta T/(200 \text{ W/m}^2)A$, where m/A is the mass per unit area of lake surface. Therefore:

$$\Delta t = (10^3 \text{ kg/m}^3)(10 \text{ m})(4184 \text{ J/kg} \cdot \text{K})(10 \text{ K})/(200 \text{ W/m}^2) = 2.09 \times 10^6 \text{ s} = 24.2 \text{ d}$$

52. $\Delta Q = \Delta K = 2(\frac{1}{2}mv^2) = 2mc \Delta T$ (if there are no energy losses), therefore $\Delta T = v^2/2c_{\text{Iron}} = (90 \text{ m}/3.6 \text{ s})^2/(2 \times 447 \text{ J/kg} \cdot \text{K}) = 0.699 \text{ K}$.

55. **INTERPRET** Our system consists of two materials, water and copper, which are initially at different temperatures. They are brought together and reach a thermal equilibrium. We want to find the mass of the copper.

DEVELOP Let us assume that all the heat lost by the copper is gained by the water, with no heat transfer to the container or its surroundings. Then $-\Delta Q_{\text{Cu}} = \Delta Q_{\text{H}_2\text{O}}$ (as in Example 16.2), or

$$-m_{\text{Cu}}c_{\text{Cu}}(T - T_{\text{Cu}}) = m_{\text{H}_2\text{O}}c_{\text{H}_2\text{O}}(T - T_{\text{H}_2\text{O}})$$

The specific heats of copper and water can be found in Table 16.1.

EVALUATE Expressing all the temperatures in the Kelvin scale and solving for m_{Cu} , one finds

$$m_{\text{Cu}} = \frac{m_{\text{H}_2\text{O}}c_{\text{H}_2\text{O}}(T - T_{\text{H}_2\text{O}})}{c_{\text{Cu}}(T_{\text{Cu}} - T)} = \frac{(1 \text{ kg})(4184 \text{ J/kg} \cdot \text{K})(298 \text{ K} - 293 \text{ K})}{(386 \text{ J/kg} \cdot \text{K})(573 \text{ K} - 298 \text{ K})} = 0.197 \text{ kg}$$

ASSESS Since the water has much greater mass and higher specific heat, its temperature change is less compared to copper.

66. The average power supplied to the water is $P = \Delta Q/\Delta t = mc \Delta T/\Delta t = (430 \text{ g})(1 \text{ cal/g} \cdot \text{C}^\circ)(100^\circ\text{C} - 20^\circ\text{C}) \times (4.184 \text{ J/cal})/(5 \times 60 \text{ s}) = 480 \text{ W}$. This is also the output of the microwave, if we neglect the power absorbed by the container and any leakage in the unit.