

$$P_1^\mu = (E_1, +P)$$

$$P_2^\mu = (E_2, -P)$$

$$P_{12}^\mu = (E_1 + E_2, 0)$$

$$\mathcal{B} P_2^\mu = (m_2, 0)$$

$$\begin{pmatrix} \gamma & \gamma\beta \\ \gamma\beta & \gamma \end{pmatrix} \begin{pmatrix} E_2 \\ -P \end{pmatrix} = \begin{pmatrix} m_2 \\ 0 \end{pmatrix}$$

$$\begin{cases} \gamma E_2 - \gamma\beta P = m_2 \\ \gamma\beta E_2 - \gamma P = 0 \end{cases}$$

$$\cancel{\gamma}\beta E_2 = \cancel{\gamma}P$$

$$\beta E_2 = P$$

$$\beta = \frac{P}{E_2}$$

$$\gamma E_2 - \gamma P \frac{P}{E_2} = m_2$$

$$\gamma \left(\frac{E_2^2 - P^2}{E_2} \right) = m_2$$

$$\gamma \left(\frac{m_2^2}{E_2} \right) = m_2$$

$$\gamma = \frac{E_2}{m_2}$$

$$\gamma = \frac{1}{\sqrt{1-\beta^2}} = \frac{1}{\sqrt{1-\frac{P^2}{E_2^2}}}$$

$$= \frac{1}{\sqrt{\frac{E_2^2 - P^2}{E_2^2}}} = \frac{1}{\sqrt{\frac{m_2^2}{E_2^2}}}$$

$$= \frac{E_2}{m_2}$$

$$\mathcal{B} = \begin{pmatrix} \cosh & +\sinh \\ +\sinh & \cosh \end{pmatrix}$$

$$\mathcal{R} = \begin{pmatrix} \cos & -\sin \\ +\sin & \cos \end{pmatrix}$$

$$\mathcal{B} P_2^\mu = (m_2, 0)$$

$$\mathcal{B} P_1^\mu = (E', P')$$

$$P_1 \rightarrow P_2$$

$$P_1^\mu = (E + P) \quad P_1^2 = E^2 - P^2 = m^2$$

$$P_2^\mu = (E - P) \quad P_2^2 = E^2 - P^2 = m^2$$

$$P_{12}^\mu = (2E, 0) \quad P_{12}^2 = S = 4E^2$$

$$PP \rightarrow PPPP$$

$$P_{3456}^\mu = (m, 0, 0, 0)$$

$$P_{3456}^\mu = (4m, 0)$$

$$P_{3456}^2 = S = 16m^2$$

$$S_{\text{before}} = S_{\text{After}}$$

$$4E^2 = 16m^2$$

$$E = 2m$$

$$S_{\text{before}} = 4E^2$$

$$PP \rightarrow PPH$$

$$P_3^\mu = (m, 0)$$

$$P_4^\mu = (m, 0)$$

$$P_5^\mu = (M, 0)$$

$$P_{345}^\mu = (2m + M, 0)$$

$$S = P_{345}^2 = (2m + M)^2 = 4E^2$$

$$2m + M = 2E$$

$$P_1 \rightarrow P_2$$

$$P_1^\mu = (E, P)$$

$$P_2^\mu = (m, 0)$$

$$P_{12}^\mu = (E + m, P)$$

$$S = P_{12}^2 = (E + m)^2 - P^2$$

$$= E^2 + 2Em + m^2 - P^2$$

$$S_{\text{before}} = 2m^2 + 2Em = S_{\text{after}} = (2m + M)^2$$

$$U = \begin{pmatrix} t \\ x \end{pmatrix}$$

$$\mathcal{B} = \gamma \begin{pmatrix} 1 & \beta \\ \beta & 1 \end{pmatrix}$$

$$\mathcal{B} U = \gamma \begin{pmatrix} 1 & \beta \\ \beta & 1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = U'$$

$$= \gamma \begin{pmatrix} t + \beta x \\ \beta t + x \end{pmatrix} = U'$$

$$\|U'\|^2 = U' \cdot g \cdot U'$$

$$\begin{pmatrix} t \\ x \end{pmatrix} \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix}$$

$$(t \ x) \begin{pmatrix} t \\ -x \end{pmatrix} = t^2 - x^2$$

$$[\gamma(t + \beta x)]^2 - [\gamma(\beta t + x)]^2$$

$$\gamma^2 = \frac{1}{1 - \beta^2} \quad \hookrightarrow t^2 - x^2$$

$$U = (x, y) \quad g = \begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix}$$

$$\|U\|^2 = U \cdot g \cdot U$$

$$= (x \ y) \begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

$$(x \ y) \begin{pmatrix} x+y \\ x+y \end{pmatrix} \quad g = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

$$\|U\|^2 = (x+y)^2 \quad g = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

$$\|U\| = x + y$$

$$\mathcal{B} U = \gamma \begin{pmatrix} 1 & \beta \\ \beta & 1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} t' \\ x' \end{pmatrix}$$

$$F_{\mu\nu} = \begin{pmatrix} 0 & E & E & E \\ E & 0 & B & B \\ E & B & 0 & B \\ E & B & B & 0 \end{pmatrix}$$

$$\mathcal{B} F_{\mu\nu} \mathcal{B}^T$$