

Phys 3344:

Office Hours: Wed 3:30-4:30???

Homework #1:

Homework #2

Mathematica

Units

Air Resistance

Please join us for the

# PHYSICS Department Kick-Off Event

**Gifts for participants!**

6:00 – 7:00 pm  
Wed Sept 2<sup>nd</sup> by Zoom

Look for  
Canvas Announcement  
to register

**Meet the current Physics faculty and students**  
**Learn about opportunities for undergraduate research**  
**Get advice about careers and majoring or minoring in Physics**  
**Find out about the Society of Physics Students (SPS)**

<b>2020 FALL      PHYS 3344</b>					
#	DAY	LECTURE:	NOTES:	Chpt	TOPIC
1	TUE	08/25/20	First Class	1	Newtons Laws
2	THUR	08/27/20		2	Projectiles
3	TUE	09/01/20		3	Momentum & Angular Momentum
4	THUR	09/03/20		4	Energy
5	TUE	09/08/20		5	Oscillations
6	THUR	09/10/20			
7	TUE	09/15/20			
8	THUR	09/17/20			<b>EXAM 1</b>
9	TUE	09/22/20		6	Calculus of Variations
10	THUR	09/24/20		7	Lagrange's Equation
11	TUE	09/29/20			
12	THUR	10/01/20		8	Two Body Problems
13	TUE	10/06/20			
14	THUR	10/08/20		9	Non-Inertial Frames
	TUE	10/13/20	<b>Fall Break</b>		
15	THUR	10/15/20		10	Rotational Motion
16	TUE	10/20/20			<b>EXAM 2</b>
17	THUR	10/22/20			
18	TUE	10/27/20		10	Rotational Motion
19	THUR	10/29/20			
20	TUE	11/03/20		11	Coupled Oscillations
21	THUR	11/05/20			
22	TUE	11/10/20		13	Hamiltonian Mechanics
23	THUR	11/12/20			
24	TUE	11/17/20			
25	THUR	11/19/20		14	Collision Theory
26	TUE	11/24/20			
27	THUR	11/26/20	<b>Thanksgiving</b>		
28	TUE	12/01/20		15	Special relativity
29	THUR	12/03/20	Last Class		Review
	WED	<b>Dec 16</b>	<b>FINAL EXAM</b>	<b>Wednesday Dec. 16, 2020, 11:30am - 2:30</b>	

# Homework #1

Phys 3344 Prof. Olness

Due: 26 Wednesday August 2020 on Canvas

## Problem 1:

For the unit vectors  $\{\hat{x}, \hat{y}, \hat{z}\}$  compute all possible

a) dot and b) cross products. (There are  $3 \times 3 = 9$  of each.)

## Problem 2:

For both  $F_1 = x \hat{x} + y \hat{y}$  and  $F_2 = -y \hat{x} + x \hat{y}$ ,

a) compute (grad)  $\nabla \cdot F$ ,

b) compute (curl)  $\nabla \times F$ , and

c) sketch  $F_1$  and  $F_2$  in the  $\{x, y\}$  plane.

## Problem 3:

For both  $F_1 = r \hat{r}$  and  $F_2 = \hat{r}/r^2$ ,

a) sketch  $F_1$  and  $F_2$  in the  $\{r, \phi\}$  plane,

b) compute  $\nabla \cdot F$  and  $\nabla \times F$  in cylindrical coordinates,

c) compute  $\nabla \cdot F$  and  $\nabla \times F$  in spherical coordinates.

## Problem 4:

a) For  $F_1 = r \hat{\theta}$  compute  $\nabla \cdot F$  and  $\nabla \times F$  in cylindrical coordinates.

b) For  $F_2 = r \sin \theta \hat{\phi}$  compute  $\nabla \cdot F$  and  $\nabla \times F$  in spherical coordinates.

(Hint: Take a look at the back cover page of the text book.)

## Problem 5:

a) A projectile of mass  $m$  is launched from a cliff of height  $h$  with velocity  $v$  at an angle  $\theta$  above the horizon. Find the a) range of the projectile, b) the time it is in the air, and c) the maximum height above the valley floor.

(Hint: This to refresh some of your skills from intro physics.)

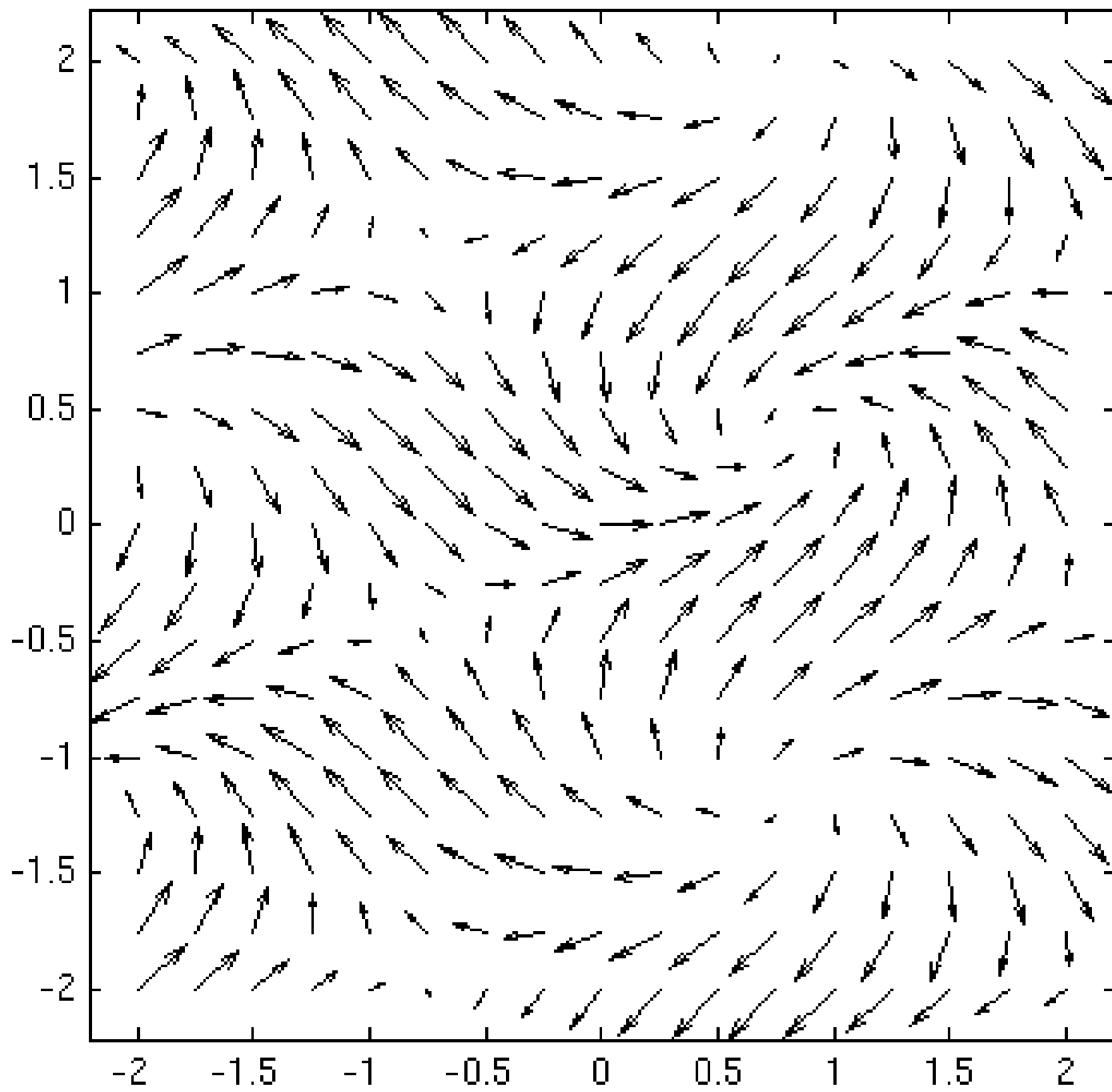
## Problem 6:

A proton of mass  $m$  and charge  $q$  circulates in a magnetic field of strength  $B$  with velocity  $v \simeq c$  (where  $c$  is the speed of light).

a) Find the radius of the orbit.

b) At the LHC  $B = 7.7$  Tesla. Compute  $r$  in meters. (Look up the values for  $m$ ,  $c$  and  $q$ .)

(Hint: Recall the Lorentz force  $\mathbf{F} = q\mathbf{v} \times \mathbf{B}$ .)



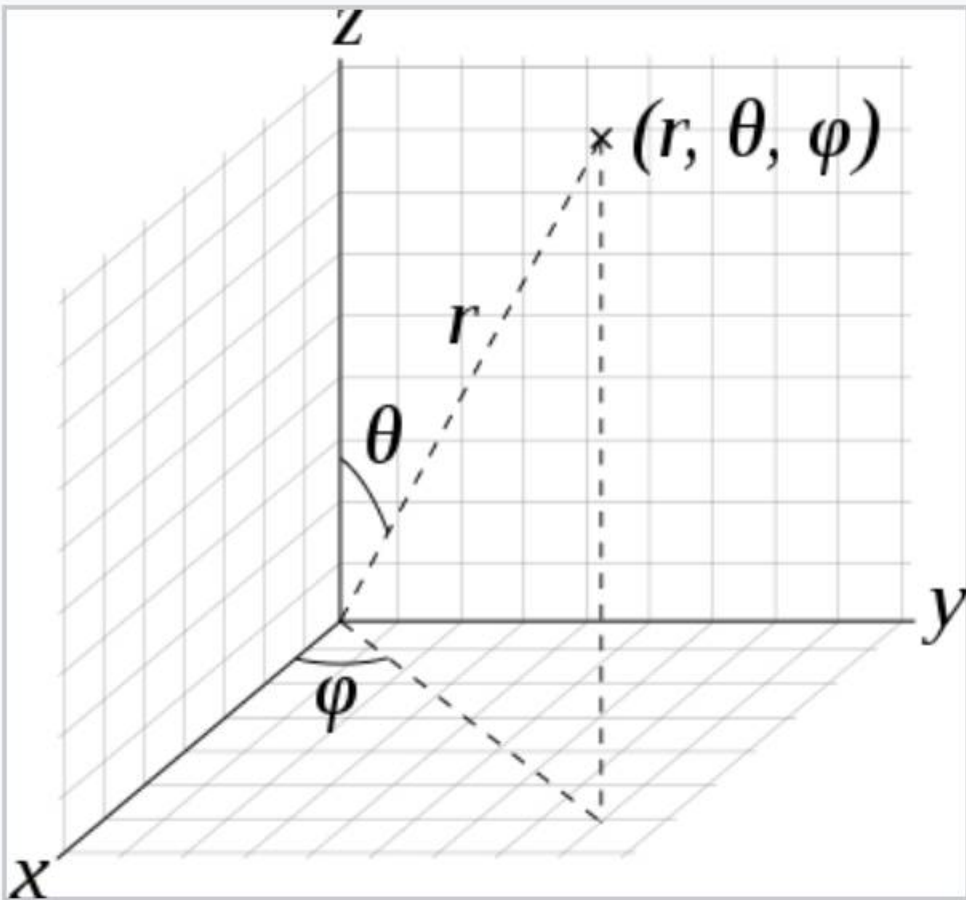
## Vector Calculus

$$\begin{aligned}\nabla f &= \hat{x} \frac{\partial f}{\partial x} + \hat{y} \frac{\partial f}{\partial y} + \hat{z} \frac{\partial f}{\partial z} && \text{[Cartesian]} \\ &= \hat{r} \frac{\partial f}{\partial r} + \hat{\theta} \frac{1}{r} \frac{\partial f}{\partial \theta} + \hat{\phi} \frac{1}{r \sin \theta} \frac{\partial f}{\partial \phi} && \text{[spherical polars]} \\ &= \hat{\rho} \frac{\partial f}{\partial \rho} + \hat{\phi} \frac{1}{\rho} \frac{\partial f}{\partial \phi} + \hat{z} \frac{\partial f}{\partial z} && \text{[cylindrical polars]}\end{aligned}$$

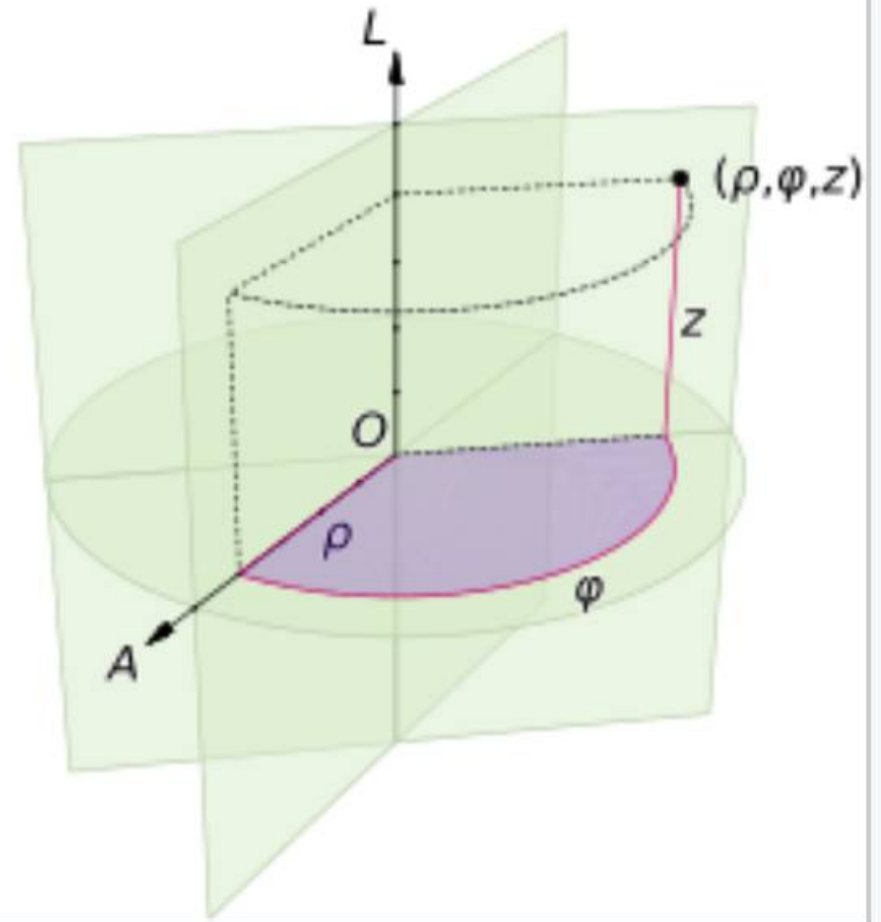
$$\begin{aligned}\nabla \times \mathbf{A} &= \hat{x} \left( \frac{\partial}{\partial y} A_z - \frac{\partial}{\partial z} A_y \right) + \hat{y} \left( \frac{\partial}{\partial z} A_x - \frac{\partial}{\partial x} A_z \right) \\ &\quad + \hat{z} \left( \frac{\partial}{\partial x} A_y - \frac{\partial}{\partial y} A_x \right) && \text{[Cartesian]} \\ &= \hat{r} \frac{1}{r \sin \theta} \left[ \frac{\partial}{\partial \theta} (\sin \theta A_\phi) - \frac{\partial}{\partial \phi} A_\theta \right] + \hat{\theta} \left[ \frac{1}{r \sin \theta} \frac{\partial}{\partial \phi} A_r - \frac{1}{r} \frac{\partial}{\partial r} (r A_\phi) \right] \\ &\quad + \hat{\phi} \frac{1}{r} \left[ \frac{\partial}{\partial r} (r A_\theta) - \frac{\partial}{\partial \theta} A_r \right] && \text{[spherical polar]} \\ &= \hat{\rho} \left[ \frac{1}{\rho} \frac{\partial}{\partial \phi} A_z - \frac{\partial}{\partial z} A_\phi \right] + \hat{\phi} \left[ \frac{\partial}{\partial z} A_\rho - \frac{\partial}{\partial \rho} A_z \right] \\ &\quad + \hat{z} \frac{1}{\rho} \left[ \frac{\partial}{\partial \rho} (\rho A_\phi) - \frac{\partial}{\partial \phi} A_\rho \right] && \text{[cylindrical polar]}\end{aligned}$$

$$\begin{aligned}\nabla \cdot \mathbf{A} &= \frac{\partial}{\partial x} A_x + \frac{\partial}{\partial y} A_y + \frac{\partial}{\partial z} A_z && \text{[Cartesian]} \\ &= \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 A_r) + \frac{1}{r \sin \theta} \frac{\partial}{\partial \theta} (\sin \theta A_\theta) + \frac{1}{r \sin \theta} \frac{\partial}{\partial \phi} A_\phi && \text{[spherical polars]} \\ &= \frac{1}{\rho} \frac{\partial}{\partial \rho} (\rho A_\rho) + \frac{1}{\rho} \frac{\partial}{\partial \phi} A_\phi + \frac{\partial}{\partial z} A_z && \text{[cylindrical polars]}\end{aligned}$$

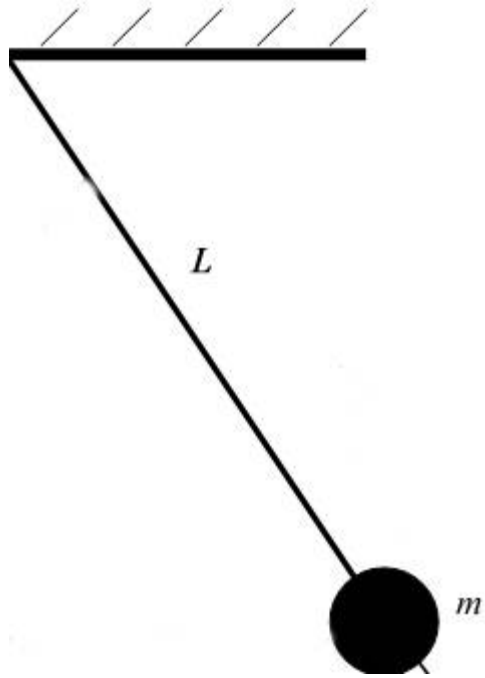
$$\begin{aligned}\nabla^2 f &= \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2} + \frac{\partial^2 f}{\partial z^2} && \text{[Cartesian]} \\ &= \frac{1}{r} \frac{\partial^2}{\partial r^2} (r f) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left( \sin \theta \frac{\partial f}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2 f}{\partial \phi^2} && \text{[spherical polars]} \\ &= \frac{1}{\rho} \frac{\partial}{\partial \rho} \left( \rho \frac{\partial f}{\partial \rho} \right) + \frac{1}{\rho^2} \frac{\partial^2 f}{\partial \phi^2} + \frac{\partial^2 f}{\partial z^2} && \text{[cylindrical polars]}\end{aligned}$$



Spherical coordinates  $(r, \theta, \varphi)$  as commonly used in **physics** (ISO 80000-2:2019 convention): radial distance  $r$ , polar angle  $\theta$  (theta), and azimuthal angle  $\varphi$  (phi). The symbol  $\rho$  (rho) is often used instead of  $r$ .

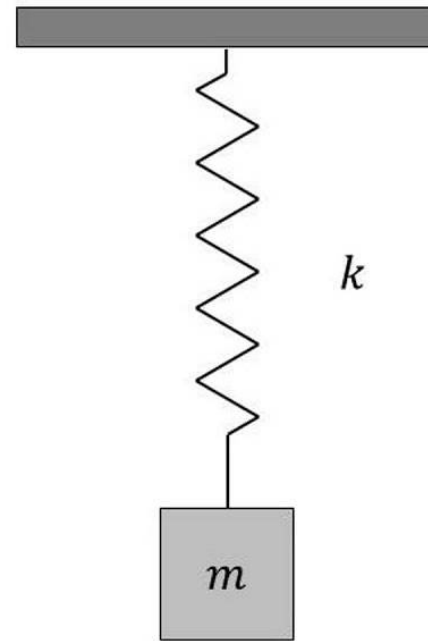


A cylindrical coordinate system with origin  $O$ , polar axis  $A$ , and longitudinal axis  $L$ . The dot is the point with radial distance  $\rho = 4$ , angular coordinate  $\varphi = 130^\circ$ , and height  $z = 4$ .



$L, m, g$

$T = 2\pi \sqrt{\frac{L}{g}}$



$K, m, A,$

$F = -Kx$

$F = ma$

$T = 2\pi \sqrt{\frac{m}{K}}$