

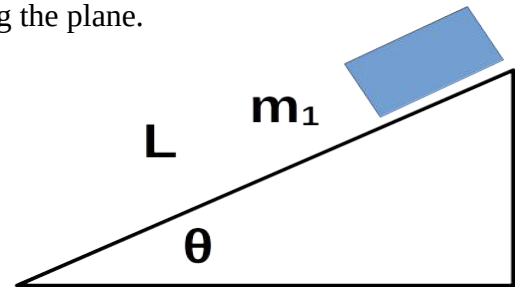
1) Consider a mass m_1 on a friction-less incline plane of length “L” along the plane.

a) Using Newtons laws, compute the

- acceleration
- the time to slide down the distance “L”
- the velocity at the bottom.

b) Repeat to find the acceleration using energy considerations.

c) Repeat to find the acceleration using Lagrange equations.



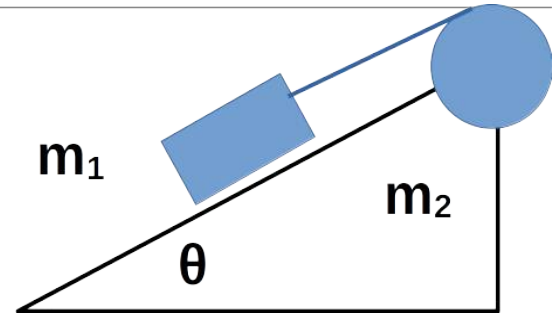
2) Consider a mass m_1 on a friction-less incline plane of length “L.”

There is a pulley of mass m_2 with $I_2 = (\gamma) m_2 R^2$.

a) Using Newtons laws, compute the acceleration.

b) Repeat to find the acceleration using energy considerations.

c) Repeat to find the acceleration using Lagrange equations with a Lagrange multiplier.



3) You launch a projectile of mass m at initial velocity v_0 an angle θ from a cliff of height $h = x_0$.

Find the horizontal distance covered. Find the maximum height above the valley floor.

4) A $M_1 = 40\text{kg}$ railway car stands on a hill with its brakes set. The brakes are released and the car rolls down to the bottom of the hill $h_1 = 100\text{m}$ below its original position. It collides with a $M_2 = 12\text{kg}$ car resting (with its brakes off) at the bottom of the track. The two cars couple together and roll up the track to a height h_2 .

a) Whose fault is the collision? b) Find the final height, h_2 , of the cars.

5) A man pulls his children on a sled with a rope with angle $\theta = 20$ degrees with the horizontal.

The total mass of the children plus the sled is $m = 50\text{kg}$. The coefficient of friction is $\mu = 0.4$.

a) What tension T is necessary in the rope so that the sled moves at a constant velocity?

b) If the man wants the sled to accelerate at $a = 3\text{m/s}^2$, what is the new tension T_2 .

6) A race car rounds a curve of radius $r = 100\text{m}$ at a speed $v = 120\text{km/hr}$.

a) At what angle should the curve be banked so that the car does not need any friction to make the turn?.

b) If the curve is un-banked, what is the minimum coefficient of friction necessary so that the car does not slip?

7) The roller-coaster at Six Flags amusement park has a loop-the-loop track with a radius of $r = 10\text{m}$.

a) Find the minimum velocity the roller-coaster must have at the top so that it stays on the track.

b) Use energy conservation to find the velocity of the above roller-coaster when it reaches the bottom.

8) Assume the earth is a homogeneous sphere of mass $M_E = 6 \times 10^{24}\text{kg}$ and radius $R_E = 6.4 \times 10^6\text{m}$.

($I = \frac{2}{5} m r^2$ for a sphere.) a) Find the kinetic energy and angular momentum due to its rotation of 1

revolution per day. b) If I apply a force $F = 10^{10}\text{N}$ at the equator to slow the rotation of the earth, find the resulting angular deceleration α . c) Using α from part (b), how long will it take to stop the rotation of the earth?

9) A bullet of mass $m_1 = 50\text{g}$ strikes a wood block of mass $m_2 = 1\text{kg}$ at rest hanging vertically on a string of length $L = 50\text{cm}$. After the bullet is embedded in the wood block, the system swings to an angle of $\theta = 30$ degrees. Find the initial velocity of the bullet.

10) A turntable of $m = 20\text{kg}$ $r = 0.5\text{m}$ ($I = \frac{1}{2} m r^2$) is spinning at $\omega_0 = 20\text{ rad/sec}$. A torque of $\tau = 2\text{ N}\cdot\text{m}^2$ is applied to slow the turntable. i) Find the angular deceleration α .

ii) Find the number of revolutions necessary to stop the turntable.