

Due: 11 November

1. Suppose that a spring of force constant k has unstretched and uncompressed length ℓ . The spring is suspended vertically and loaded with a mass m .
 - (a) Find the equilibrium length of the loaded spring (the length of the spring when the mass is not oscillating).
 - (b) Find the natural angular frequency of undamped vertical oscillations.
 - (c) Compare with the natural angular frequency of undamped horizontal oscillations of the same spring with the same mass attached, sliding on a frictionless horizontal surface.
2. Show that the solutions $x(t) = A \cos(\omega t) + B \sin(\omega t)$ and $x(t) = D \cos(\omega t + \phi)$ are equivalent by finding equations relating $(A$ and $B)$ to $(D$ and $\delta)$ and vice versa.
3. Find, analytically and numerically, the natural angular frequency for a uniform rod of mass 5 kg and length 1 meter pivoted about
 - (a) one end
 - (b) a point 20 cm from one end
 - (c) the middle
4. Marion & Thornton 3-14.
5. Derive Marion & Thornton equations (3.63) and (3.72) by carrying out the differentiations yourself.
6.
 - (a) Marion & Thornton 3-11.
 - (b) Plot (not sketch) the curves yourself. Pick reasonable values for A , m , β , k , etc.