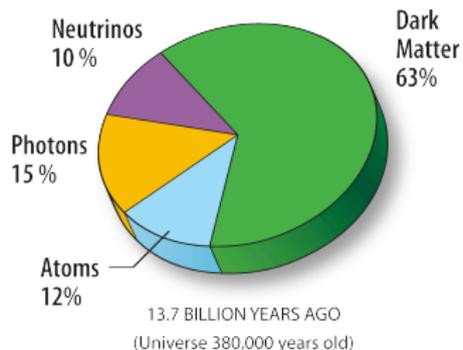
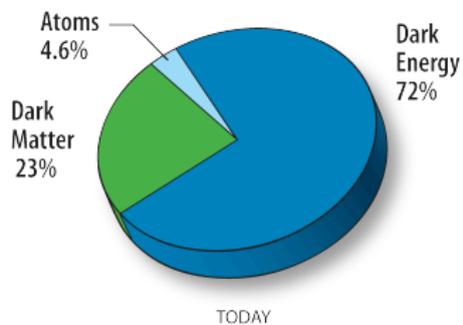


Decaying Dark Matter, Bulk Viscosity, and Dark Energy

Nguyen Quynh Lan, HNUE

Dallas, SMU; April 5, 2010

Outline



Outline

- Standard Views Dark Matter
- Standard Views of Dark Energy
- Alternative Views of Dark Energy/Dark Matter

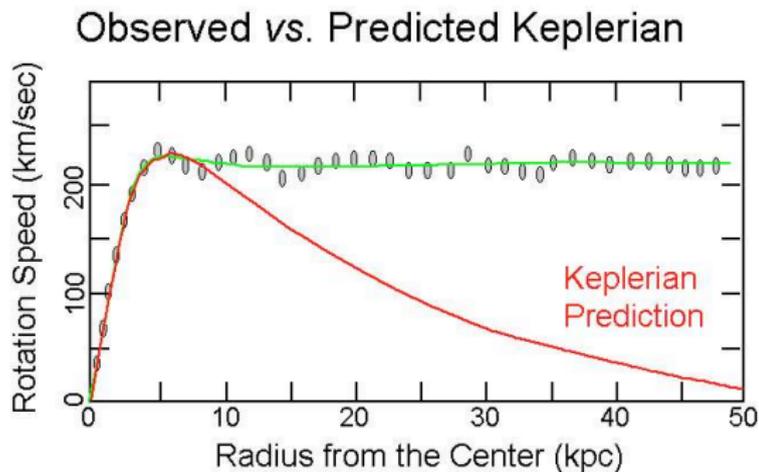
Dark Matter

The evidence for dark matter very strong:

- Galactic rotation curves cannot be explained by the disk alone.
- Cosmic microwave background radiation.
- Gravitational lensing of background galaxies by clusters is so strong that it requires a significant dark matter component.
- Clusters are filled with hot X-ray emitting intergalactic gas (without dark matter, this gas would dissipate quickly).

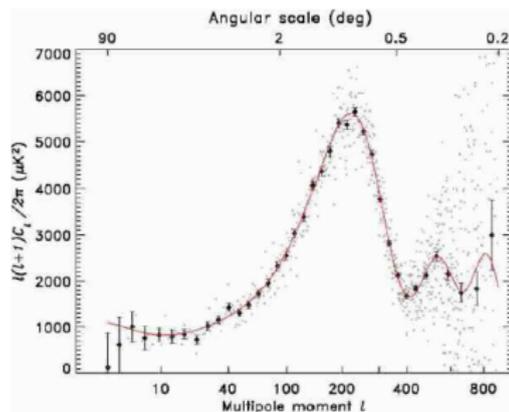
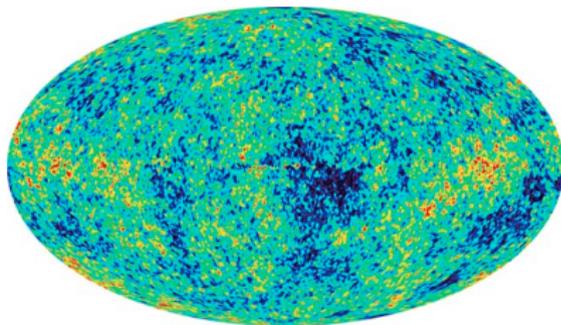
Evidence for Dark Matter

- Galactic rotation curves



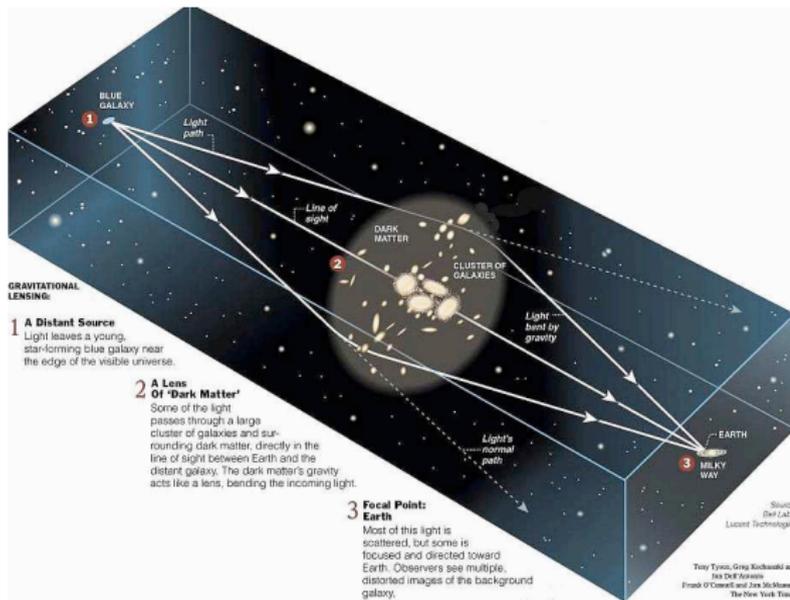
Evidence of Dark Matter

- Cosmic Microwave Background



Evidence of Dark Matter

- Gravitation lensing: seeing the invisible



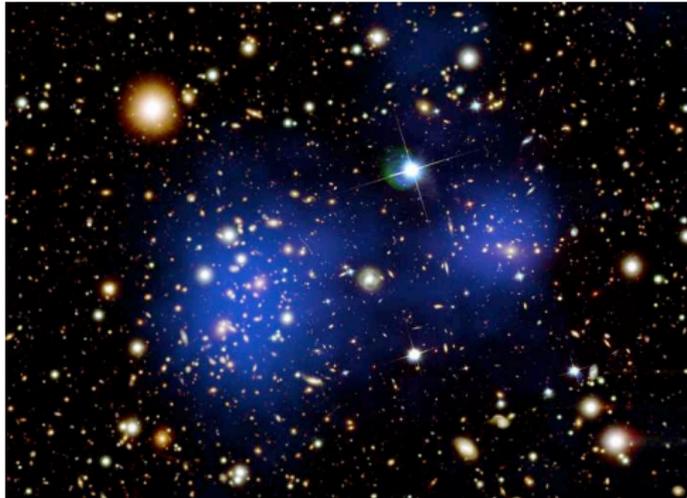
Evidence of Dark Matter

- Clusters are filled with hot X-ray emitting intergalactic gas
Merging cluster: optical image



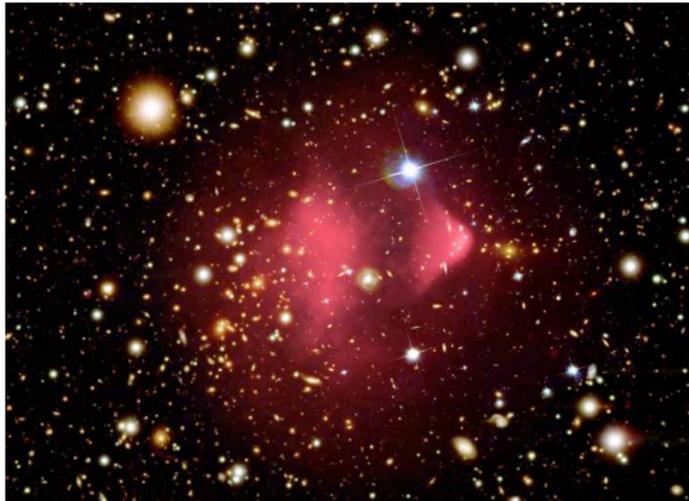
Evidence of Dark Matter

- Clusters are filled with hot X-ray emitting intergalactic gas
Merging cluster: gravitation lensing



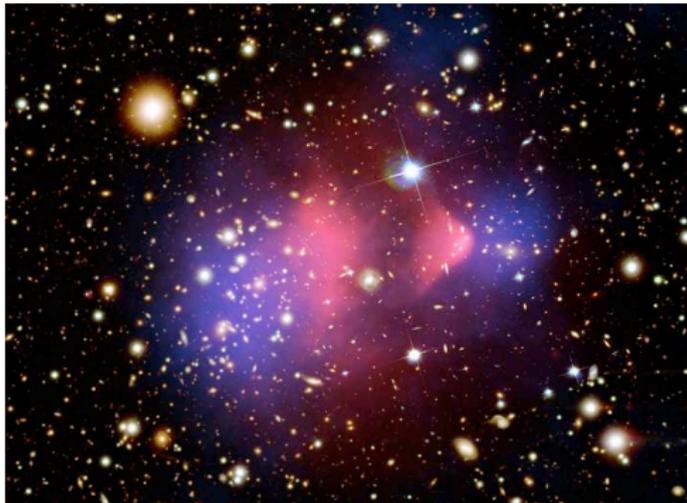
Evidence of Dark Matter

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Merging cluster: x-ray



Evidence of Dark Matter

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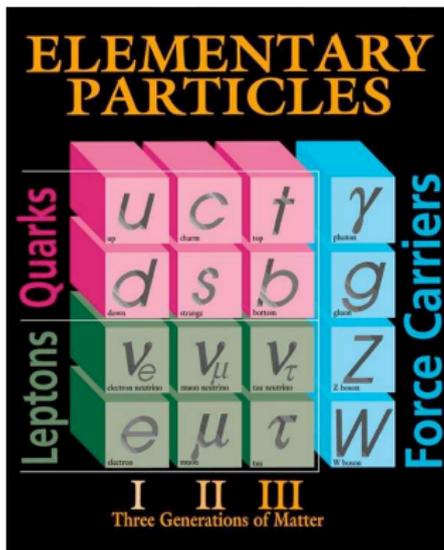


Properties of the Dark Matter

- Nonrelativistic \Rightarrow slow moving \Rightarrow cold/pressureless
- Weakly-interacting \Rightarrow only gravity, no electromagnetic or strong interactions
- Cold Dark Matter and Warm Dark Matter.

Candidates for dark matter

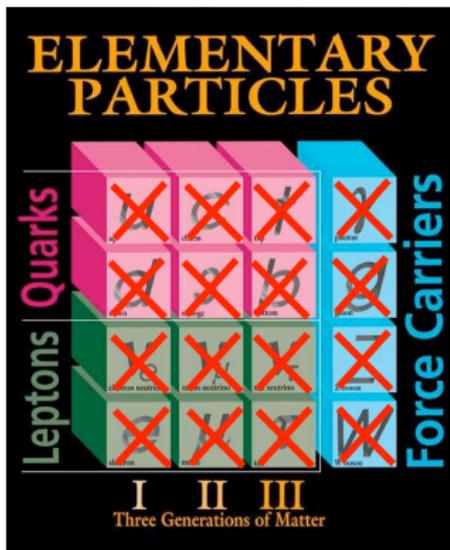
- None of the known particles can be dark matter



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Candidates for dark matter

- None of the known particles can be dark matter



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Could the dark matter of galaxies be normal matter?

- MAssive Compact Halo Objects (MACHOs)
- Black Holes
- White Dwarfs
- Planets

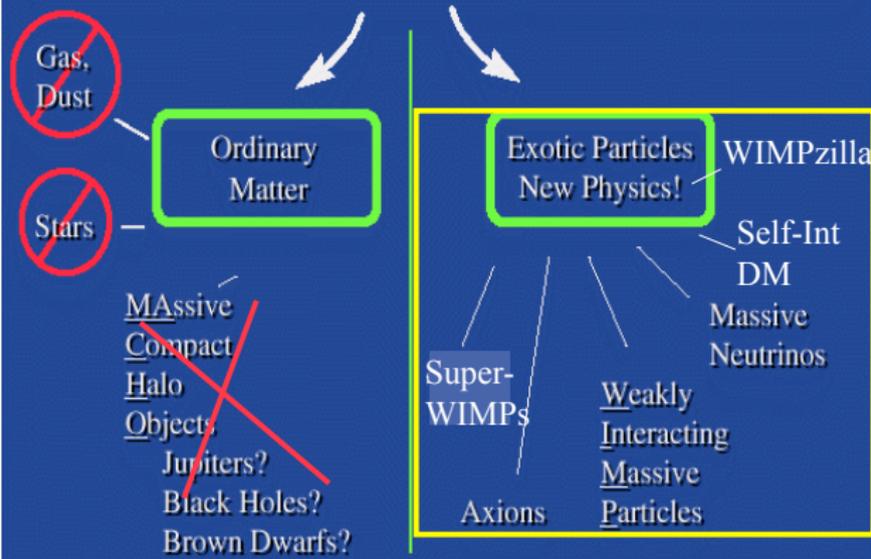
Candidates for Dark Matter

The SM offers no options for dark matter → Beyond standard model

There are two Higgs bosons: one is scalar and one is pseudoscalar particle having properties of candidates for Self Interacting dark matter (Warm Dark matter). (Lan and Long 2006).

- Supersymmetric Dark Matter?
- Extra-Dimensional Particles

What is the Galactic Dark Matter?



Evidence for Dark Energy

- Cosmic Acceleration
- Supernovae are great distance indicators
- Supernovae determine expansion rate in the past
The expansion rate depends on the content:
 - Mass slows the expansion
 - Dark energy accelerates the expansion

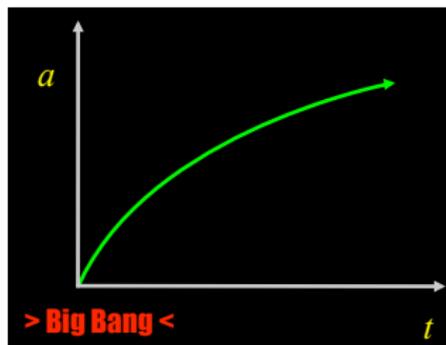
Evidence for Dark Energy

The Friedman equation with matter and radiation:

$$H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3} \left(\frac{\rho_{M0}}{a^3} + \frac{\rho_{R0}}{a^4}\right) - \frac{k}{a^2} \quad (1)$$

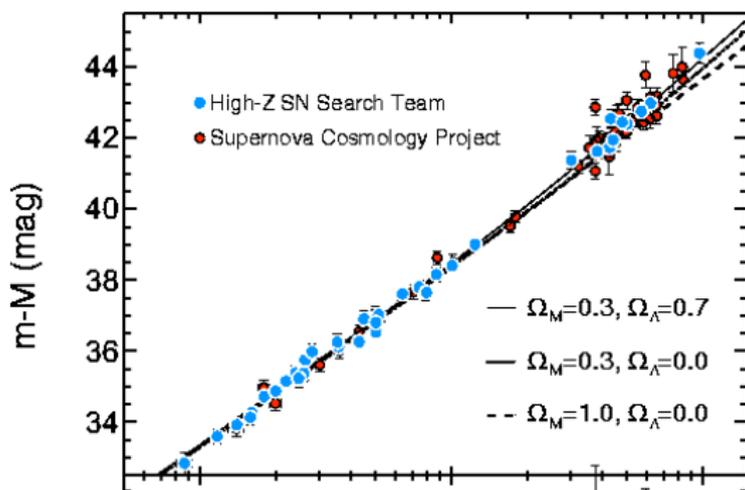
Multiply by a^2 to get: $\dot{a}^2 \propto \frac{\rho_{M0}}{a} + \frac{\rho_{R0}}{a^2} + const$

If a is increasing, each term on the right is decreasing; we therefore predict the universe should be decelerating

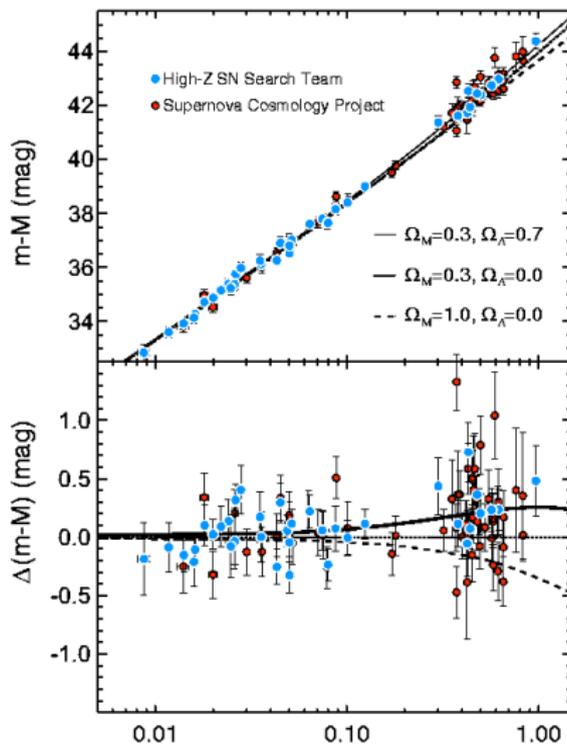


Evidence for Dark Energy

Two groups went out to look for the deceleration of the universe, using type Ia supernovae as standardizable candles. Result: supernovae are dimmer than expected. The universe is not decelerating at all, it's accelerating. Can't be explained by matter and radiation.



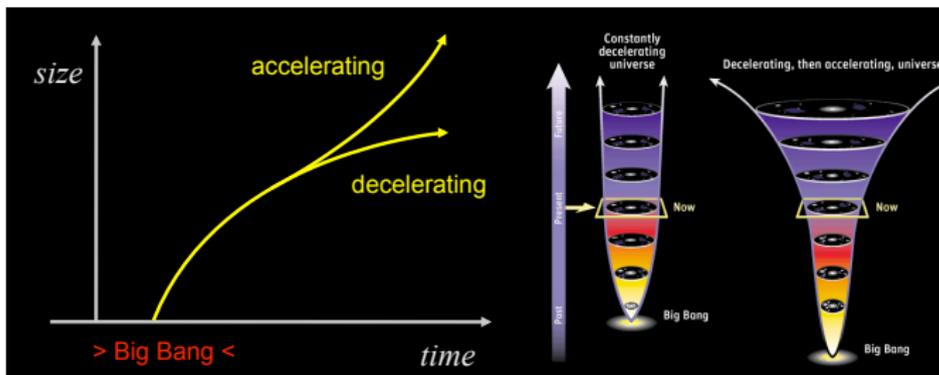
Evidence for Dark Energy



Evidence for Dark Energy

What could make the universe accelerate? From the Friedmann equation, we need something that doesn't dilute away as the universe expands. Call it Dark Energy.

$$\dot{a}^2 \propto \frac{\rho_{M0}}{a} + \frac{\rho_{R0}}{a^2} + a^2 \rho_{DE} + const$$

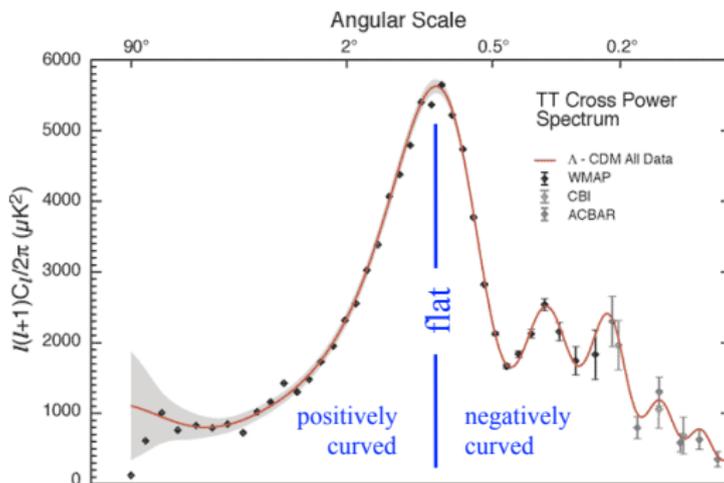


Evidence for Dark Energy

The expansion rate is described by the Hubble constant, H , relating the distance of a galaxy to its velocity. $v = Hd$ (Hubble law)
 $H^2 = (\frac{8\pi G}{3})\rho$ The Hubble constant (squared) is proportional to the energy density ρ . So if ρ is constant, H will be constant. But the distance d to some particular galaxy will be increasing, so from Hubble law its apparent velocity will go up: it will accelerate away from us.

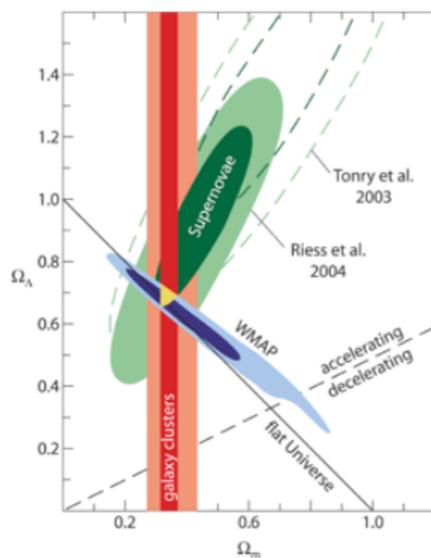
Evidence for Dark Energy

Density parameter, $\Omega = \frac{8\pi G}{3H^2} \rho = 1 + \frac{k}{a^2 H^2}$ The geometry of space depend on Ω and k . From the CMB temperature anisotropies $\Omega_{tot} = [\theta_{(peak)}]^{-2}$ we know that $\Omega_{tot} = 1$, the Universe is flat. Matter (Ordinary+dark) and radiation only accounts for 0.3



Cosmic Concordance

- $\Omega_B = 0.04, \Omega_\gamma = 0.001, \Omega_{DM} = 0.23, \Omega_\Lambda = 0.73$



Constraining the Cosmological Parameters



Evidence for Dark Energy

- Cosmic Acceleration
- Supernovae are great distance indicators
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Evidence for acceleration leads us to the Dark Energy

Unified Models Dark matter produces Dark Energy

- Appearing Dark Matter

Umezu, Ichiki, Kajino, Mathews, Yashiro(2006)

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Yahiro et.al.(2006)
- Viscous Dark Matter
- Decaying Dark Matter
- Relativistic Corrections to Friedmann Cosmology
Kolb, Matarrese, Riotto(2005)

Bulk Viscosity and Decaying Dark Matter

Mathews, Lan, Kolda(2008)

- Decaying dark matter leads to dissipative bulk viscosity in the cosmic fluid
- This viscosity may account for some or all of the apparent cosmic acceleration

Viscous Dark matter

- Bulk Viscosity

$$T^{\mu\nu} = (\rho + p)U^\mu U^\nu + g^{\mu\nu}p + \Delta T^{\mu\nu} \quad (2)$$

$$\Delta T^{\mu\nu} = -\zeta 3 \frac{\dot{a}}{a} \left(g^{\mu\nu} + U^\mu U^\nu \right) \quad (3)$$

$$T^{\mu\nu} = \left(\rho + p - \zeta 3 \frac{\dot{a}}{a} \right) U^\mu U^\nu + g^{\mu\nu} \left(p - \zeta 3 \frac{\dot{a}}{a} \right) \quad (4)$$

- Negative pressure \rightarrow Dark Energy

The effect of bulk viscosity is to replace the fluid pressure with an effective pressure given by,

$$p_{\text{eff}} = p - \zeta 3 \frac{\dot{a}}{a} \quad (5)$$

Cosmological Model

- Flat cosmology $k = 0$, $\Lambda = 0$ in a comoving FRW metric

$$g_{\mu\nu} dx^\mu dx^\nu = -dt^2 + a(t)^2 [dr^2 + r^2 d\theta^2 + r^2 \sin^2\theta d\phi^2] \quad (6)$$

- Total mass energy density

$$\rho = \rho_{DM} + \rho_b + \rho_h + \rho_r \quad (7)$$

- In the FRW frame, the energy momentum tensor can reduce to $T_{00} = \rho$, $T_{0i} = 0$

$T_{eff} = (\rho - 3\zeta H)g \Rightarrow$ Bulk Viscosity enters as an effective negative pressure in the energy momentum tensor but the Friedmann equation does not depend upon the effective pressure and it is exactly the same as for a non-dissipative cosmology

$$H^2 = \frac{\dot{a}^2}{a^2} = \frac{8}{3}\pi G\rho$$

- Conservation equation \Rightarrow energy density in matter and radiation:

$$\rho_h = \frac{\rho_{m0} e^{-\frac{t}{\tau}}}{a^3}$$

$$\rho_l = \frac{1}{a^4} [\rho_{l0} + \frac{\rho_{h0}}{\tau} + \rho_{BV}]$$

- ρ_{BV} is the dissipated energy in light relativistic species due to the cosmic bulk viscosity \Rightarrow total density includes term from dissipated energy density in bulk viscosity.

Need a Physical model for Bulk Viscosity

- If a gas is out of pressure equilibrium as it expands or contracts a bulk viscosity is generated

$$3\zeta H = \Delta p$$

Δp is the different between the constant volume equilibrium pressure and the actual fluid pressure

Decaying Dark Matter Produces Bulk Viscosity

- Particle decays lead to heating and pressure from the relativistic decay products
- This increase in heating is inevitably associated with an increase in entropy $\Delta S = \frac{\Delta Q}{T}$
- Entropy will be evidenced in a dissipation of energy => Dissipation => Bulk Viscosity

Particle decay

Pressureless DM \Rightarrow relativistic particles $p = \rho/3$

- out of temperature and pressure equilibrium
- dissipation and bulk viscosity

During decay matter and relativistic particles are out of pressure and temperature equilibrium (Weinberg)

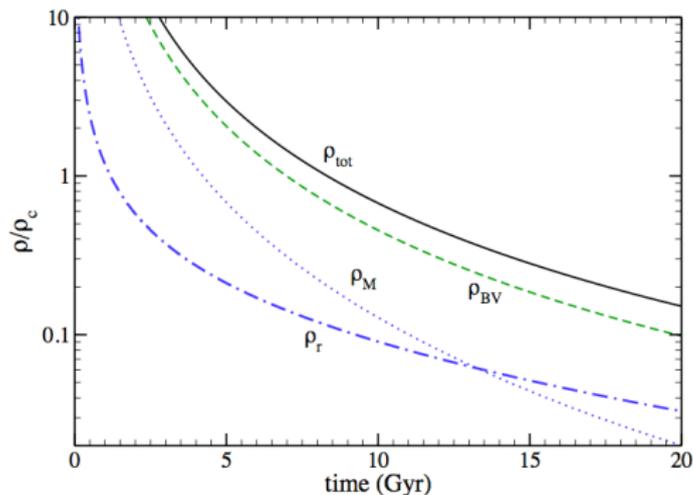
- $\Delta p = \left(\frac{4}{3}\right)\rho_h\tau_{eq}\left[1 - 3\frac{\partial p}{\partial\rho}\right]\left(\frac{\partial U^\alpha}{\partial x^\alpha}\right)$
Equilibration $\tau_{eq} = \frac{\tau}{1-3\tau H}$ Need $\frac{\partial p}{\partial\rho} \sim \frac{p}{\rho} \neq \frac{1}{3}$
 $p = \frac{\rho_l + \rho_\gamma}{3}$
- $\Rightarrow \zeta = \rho_h\tau_{eq}\left[1 - \frac{\rho_l + \rho_\gamma}{3}\right]^2$

Candidates for Decaying Dark Matter

- Sneutrinos mix in vacuum with active neutrinos
(ν_e, ν_μ, ν_τ) \Rightarrow WDM and CDM
- Parameters: Sterile neutrino mass m_s and mixing angle θ
- For $m_s < 10\text{MeV} \Rightarrow \nu_s \rightarrow \gamma + \nu$

Why this does not work

Acceleration $\Rightarrow H^2 = \frac{8}{3}\pi G\rho = \text{constant} \Rightarrow \rho = \text{constant}$

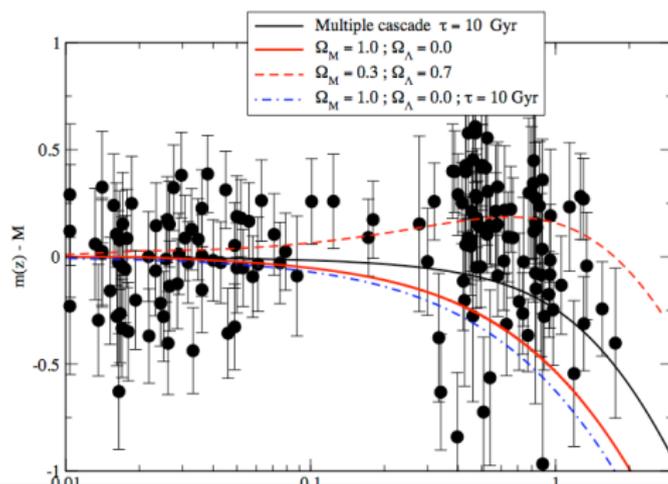


How to fix this

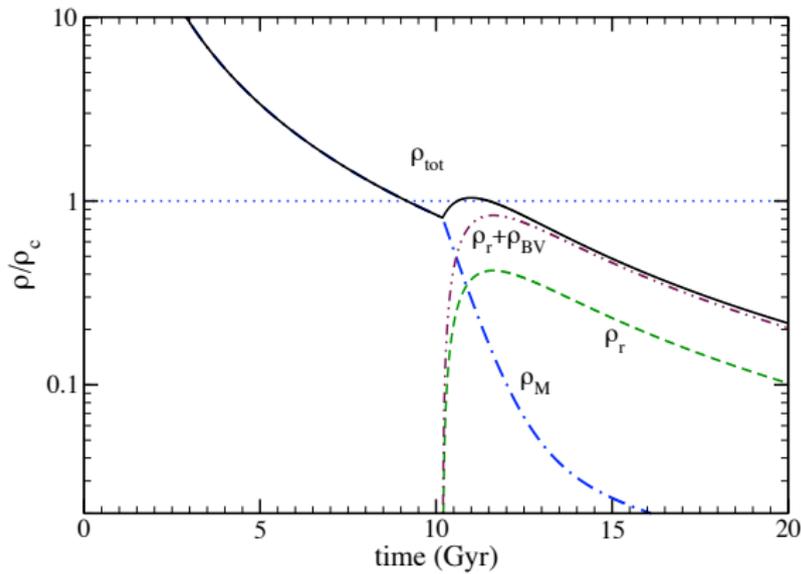
Need much larger BV coefficient

Cascading decays: Sterile neutrinos

$\nu_1 \rightarrow \nu_2 \rightarrow \nu_3 \rightarrow \nu_4 \rightarrow \nu_5 \rightarrow \nu_6 \rightarrow$ regular neutrinos or Late decays
due to time varying mass or a late phase transition



Late decaying DM with bulk viscosity can produce cosmic acceleration without Dark Energy or a Cosmological constant



Conclusion

- Simple DM decay can produce a bulk viscosity but its effect is overwhelmed by the fact that the universe becomes radiation dominated at late times

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Conclusion

- Simple DM decay can produce a bulk viscosity but its effect is overwhelmed by the fact that the universe becomes radiation dominated at late times
- Can account for some dark energy if the appearance of the particle decays is delayed by a cascade
- **Can account for all dark energy if there is a late phase transition possibly caused by a time-dependent mass**

Thank you for your attention!

In collaboration with H. N. Long, G. Mathews, C. Kolda, and M. Giovannini