



## A search for baryon and lepton number violation in *B* decays using the BaBar dataset <u>SMU HEP Seminar</u> Southern Methodist University

#### M. Bellis

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March 7<sup>th</sup>, 2011





## OUTLINE

#### MOTIVATION

#### 2 BABAR

- **3** Analysis overview
  - Blind analysis
  - Candidate selection
  - Fitting procedure
  - Results
  - Summary

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• Our universe is matter...not anti-matter.



Image: A mathematical states of the state

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- t = early universe:
  - matter = anti-matter



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- Our universe is matter...not anti-matter.
- t = early universe:
  - matter = anti-matter
- t = now:
  - matter  $\neq$  anti-matter
- How do we know?
  - Cosmic ray's are mostly matter.
  - γ-ray spectrum.
- Universe is compartmentalized?
  - Very difficult theoretically.



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- "Violation of CP Invariance, c Asymmetry, and Baryon Asymmetry of the Universe."
- Three conditions required for matter (baryon) asymmetry. [1]

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    - Decay rates are different for *matter* and *anti-matter*.

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  - 2 C and CP-violation
    - Decay rates are different for matter and anti-matter.
  - 8 Baryon number violation
    - Implies sum of baryons + anti-baryons is a non-conserved quantity.
- Let's look at these last two...

# DIRECT CP-VIOLATION

• Direct CP-violation •  $B^0 \rightarrow K^+\pi^-$ •  $\bar{B}^0 \rightarrow K^-\pi^+$ 



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# DIRECT CP-VIOLATION

- Direct CP-violation
  - $B^0 \rightarrow K^+ \pi^-$ •  $\bar{B}^0 \rightarrow K^- \pi^+$
- Decay rates are different!
- $A_{CP} \approx -0.1$
- Sakharov condition # 2!



- Baryon number violation actually *does* exist in the Standard Model.
  - Sphaleron, a non-perturbative process.
  - Occurs at very high temperatures. T = 100GeV.  $(10^{15}$ K)
  - Only found immediately after the big bang.
- Sakharov condition # 3!

- Does this predict our asymmetric universe?
  - B for baryon
  - $B + \overline{B}$  annihilations in the early universe produced photons.
  - Asymmetry parameter  $(\eta)$ .

$$\eta = rac{N_B - N_{ar{B}}}{N_{\gamma}} \ pprox 10^{-9}$$

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 Combination of observed CP-violation and and theoretical BNV in Standard Model is insufficient by 10 orders of magnitude!!!

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- Combination of observed *CP*-violation and and theoretical BNV in Standard Model is insufficient by 10 orders of magnitude!!!
- Additional CP violation? Much work out there...no smoking gun.
- Additional BNV?
- 1974, "Unity of All Elementary Particle Forces.", Georgi and Glashow
  - Proton decay mediated by heavy bosons (X & Y) which couple to *quarks* and *leptons*.
- Many Grand Unified Theories ⇒ BNV
- How would proton decay work?

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#### PROTON DECAY

- X is  $q = \frac{1}{3}$ • X  $\rightarrow q + q$ • X  $\rightarrow q + \ell$
- B-L is conserved quantity.



#### PROTON DECAY

- X is  $q = \frac{1}{3}$ • X  $\rightarrow q + q$ • X  $\rightarrow q + \ell$
- B-L is conserved quantity.
- Hypothesize a flavour/generation dependance to this interaction...
  - $B^0 \rightarrow \Lambda_c^+ \ell^-$ •  $B^+ \rightarrow \Lambda^0 \ell^+$

• 
$$\ell = \mu$$
 or  $\epsilon$ 

$$\begin{pmatrix} \mathsf{X}_{u\bar{d}} & \mathsf{X}_{c\bar{d}} & \mathsf{X}_{t\bar{d}} \\ \mathsf{X}_{u\bar{s}} & \mathsf{X}_{c\bar{s}} & \mathsf{X}_{t\bar{s}} \\ \mathsf{X}_{u\bar{b}} & \mathsf{X}_{c\bar{b}} & \mathsf{X}_{t\bar{b}} \end{pmatrix}$$
$$\begin{pmatrix} \mathsf{X}_{\bar{u}e^-} & \mathsf{X}_{c\bar{e}^-} & \mathsf{X}_{\bar{t}e^-} \\ \mathsf{X}_{\bar{u}\mu^-} & \mathsf{X}_{\bar{c}\mu^-} & \mathsf{X}_{\bar{t}\mu^-} \\ \mathsf{X}_{\bar{u}\tau^-} & \mathsf{X}_{\bar{c}\tau^-} & \mathsf{X}_{\bar{t}\tau^-} \end{pmatrix}$$





#### HISTORY

- Experimental work
  - Proton lifetime  $> 10^{32}$  years!
  - Tevatron and HERA searches for "true" leptoquarks [2].
    - *M* Mass of the mediating leptoquark (X-boson)
    - $\lambda$  Yukawa coupling



#### HISTORY

- Experimental work
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    - *M* Mass of the mediating leptoquark (X-boson)
    - $\lambda$  Yukawa coupling
- Theoretical work
  - "Baryon number violation involving higher generations.", Hou, et.al.[3]
    - Uses proton decay to constrain upper limits.
    - $\mathcal{B}(B^0) \rightarrow \Lambda_c^+ \ell^- < 4 imes 10^{-29}$
    - "Despite our findings, we believe it is still worth to look for BNV processes in τ, charm, B, and maybe in the future in top decays."
- This analysis is the first search for  $B \to \Lambda_{(c)} \ell$  decays.



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$$\ell = \mu \text{ or } e$$

 $\rightarrow$ 

$$B^0 \rightarrow \Lambda_c^+ \ell^-$$

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 $\ell = \mu \text{ or } e$   $B^0 \rightarrow \Lambda_c^+ \ell^ \rightarrow \qquad e^- e^+$ 

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 $\ell = \mu \text{ or } e$ 

 $\rightarrow$ 

 $\rightarrow \Lambda_c^+ \ell^-$ 

 $B^0$ 

 $e^ B^0$   $e^+$ 

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 $\ell = \mu \text{ or } e$   $B^{0} \rightarrow \Lambda_{c}^{+} \ell^{-}$   $\rightarrow \qquad e^{-} \qquad e^{+}$   $\overline{B^{0}} \qquad e^{+}$ 

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 $\ell = \mu \text{ or } e$   $B^{0} \rightarrow \Lambda_{c}^{+} \ell^{-}$   $\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}$ e



#### BNV IN B DECAYS

 $\ell = \mu \text{ or } e$  $\begin{array}{rcl} B^0 & \to & \Lambda_c^+ \ell^- \\ & & \Lambda_c^+ \to p K^- \pi^+ \end{array}$  $e^{-}$  $B^ \begin{array}{ccc} B^{-} & \rightarrow & \Lambda^{0}\ell^{-} \\ & & \Lambda^{0} \rightarrow p\pi^{-} \end{array}$  $B^- \rightarrow \overline{\Lambda^0 \ell^-}$ 

$$ar{\Lambda^0} o ar{m{
ho}} \pi^-$$

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- Experimental requirements:
  - Cleanly identify 4 charged particles.
  - Demonstrate they came from a *B* meson.



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# SLAC AND BABAR



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Image: A matrix and a matrix

## BABAR



- BaBar at SLAC
- 1999-2008

### BABAR



- BaBar at SLAC
- 1999-2008
- PEP-II asymmetric  $e^+e^-$  collider

  - Ran on  $\Upsilon(4S)$  Instantaneous  $\mathcal{L} = 10^{-34} \text{ cm}^{-2} \text{ s}^{-1}$

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• 1 billion *B* mesons

### BABAR



- BaBar at SLAC
- 1999-2008
- PEP-II asymmetric  $e^+e^-$  collider
  - Ran on  $\Upsilon(4S)$
  - Instantaneous  $\mathcal{L} = 10^{-34} \text{ cm}^{-2} \text{ s}^{-1}$
- 1 billion B mesons
- Backgrounds (or other physics!)
  - $e^+e^- \rightarrow u\bar{u}/d\bar{d}/s\bar{s}/c\bar{c}$ •  $e^+e^- \rightarrow e^+e^-/\mu^+\mu^-/\tau^+\tau^-$
- 400+ papers and counting.
- Excellent momentum and spatial resolution.

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#### PAIR PRODUCTION



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### BABAR



- Sophisticated particle ID.
- Inner silicon vertex detector.
  - Energy, spatial position (momentum)
- Drift chambers.
  - Energy, momentum
- Cerenkov detector (DIRC)
  - Velocity  $(\pi/K \text{ ID})$
- Muon detection in outer region
  - Timing, spatial position
- All fed into a neural net algorithm.
- Gives analysts 6 levels.
  - For each particle type (e, μ, p, π, K)
  - Vary purity/efficiency.
  - Function of kinematics.

 $\pi$  efficiency



Selector : SuperLooseKMPionMicroSelection

Dataset : run6-r24c

Tables created on 4/2/2009 (Data) , 4/2/2009 (MC)

 $\pi$  efficiency



#### K contamination



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- B mass

Signal process (Monte Carlo)



All background processes (Monte Carlo)



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$$m_{ES} = \sqrt{\frac{1}{4}s - (p_B^*)^2}$$

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$$m_{ES} = \sqrt{\frac{1}{4}s - (p_B^*)^2}$$

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$$\Delta E = E_B^* - \frac{1}{2}\sqrt{s}$$

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- Unbinned extended likelihood fit.
- Fit using appropriate kinematic variables.
- B mass
- $m_{ES} = \sqrt{\frac{1}{4}s (p_B^*)^2}$
- $\Delta E = E_B^* \frac{1}{2}\sqrt{s}$
- Discriminating power in 2D plane.
- Signal region is blinded in data analysis!



All background processes (Monte Carlo)



### Our blind data



- Blind searches
  - Taken from Roodman, "Blind analysis in particle physics" [4]



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- Blind searches
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- Experimenter's bias.



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- Medical field: double blind trials.
- Electron *e*/*m*, Dunnington (1933)



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- History of measurements?



Figure 2: A historical perspective of values of a few particle properties tabulated in this *Review* as a function of date of publication of the *Review*. A full error bar indicates the quoted error; a thick-lined pertion indicates the same but without the "scale factor."

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- Experimenter's bias.
- Medical field: double blind trials.
- Electron e/m, Dunnington (1933)
- History of measurements?
- How do you guard against this?
- Don't look!



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- Hidden signal box.

  - $K_L^0 \rightarrow \mu^{\pm} e^{\mp}$  Ariska, **PRL 70**, 1993



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- Kinematics dictates region of interest.



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- Hidden signal box.

  - $K_L^0 \rightarrow \mu^{\pm} e^{\mp}$  Ariska, **PRL 70**, 1993
- Kinematics dictates region of interest.
- Other approaches: hidden answer, ۰ random noise.



#### CDMS (2009), dark matter search





Image: A matrix and a matrix

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### ANALYSIS OVERVIEW

- Full dataset (435 fb<sup>-1</sup>)
  - Constrain vertex of B candidate.
  - Mass/vertex constrain  $\Lambda_c/\Lambda^0$  candidate.
- Optimize PID selectors.
- Multivariate discriminator.
  - TMVA.
  - Input variables.
  - Choice of background sample.
  - Check for correlations with  $\Delta E$  and  $m_{ES}$ .
- Check for fit bias.
- Fit the unblinded data.

- Punzi figure of merit.
  - Strike a balance between setting upper limit for null results and observation of a small signal.

f.o.m. = 
$$\frac{\epsilon_S}{\sqrt{B} + a/2}$$

- a is the significance (sigma) at which you want to make a final claim.
  - For this analysis, a = 5.
- $\epsilon_S$  is the efficiency of the signal.
- Don't need to know S (cross section), but we do need an idea of B (background).

- During optimization, make extensive use of MC samples.
- GEANT4 simulation of the detector.
- Simulated signal events (assume no polarization of (Λ<sub>(c)</sub>)
- Background samples.
- qā
  - $u\bar{u}/d\bar{d}/s\bar{s}/c\bar{c}$
- *BB* 
  - B<sup>+</sup>B<sup>-</sup>
  - *B*<sup>0</sup>*B*<sup>¯0</sup>
- All generics
  - $q\bar{q} + B\bar{B}$  (weighted by relative cross sections)

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#### BHABBA LEAKAGE

- Leakage from Bhabba events.
- Eliminated by requiring # charged tracks > 4.



FIGURE: |p| vs.  $\cos(\theta)$  for the  $\pi^-$  coming from the  $\Lambda^0$  candidate.

## PID

- Optimize PID for kinematics.
- e.g.  $\Lambda_c^+ \to p K^- \pi^+$
- Loosest PID



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- Optimize PID for kinematics.
- e.g.  $\Lambda_c^+ \to p K^- \pi^+$
- Loosest PID
- Some set of PID criteria.
- Use Λ<sup>+</sup><sub>c</sub> efficiency and background rejection to optimize selection.



• PID selectors optimized for this signal.



(a) Signal significance for the 216 PID selector combinations.

FIGURE: Optimization criteria for the PID selectors for the  $B \rightarrow \Lambda_c^+ \mu$  mode.

### PARTICLE ID

- Λ: cτ = 7.89 cm
- Pristine  $\Lambda^0$  candidates after transverse flight length > 0.2cm.



FIGURE: Invariant mass of the  $\Lambda^0$  candidate vs. the transverse flight length

#### TRAINING VARIABLES

- Explored multivariate discriminators.
- TMVA implementaion.
  - Toolkit for Multivariate Data Analysis with ROOT.
  - http://tmva.sourceforge.net/
- Pruned discriminating variables to most sensitive that did not have high correlations with  $\Delta E/m_{ES}$ .
- Six variables.
  - B cos(θ) CM
  - $B \cos(\theta)$  sphericity wrt ROE sphericity
  - $B \cos(\theta)$  thrust wrt ROE thrust
  - Legendre P2 (historical name)
    - Moments
    - Use ROE tracks, and B-thrust axis
  - Thrust all
  - R2 all
    - Ratio of Fox-Wolfram moments (0 and 2)

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### TRAINING VARIABLES (DATA AND MC)

Comparison between signal MC and  $q\bar{q}$  MC.



 $\Lambda_c \mu^-$ 

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Image: Image:

- Checked correlations with  $\Delta E$  and  $m_{ES}$ .
  - Bootstrap method used to estimate significance of correlation coefficient.
  - Numerical procedure to estimate some estimator.
  - When you only have one data sample.
  - Originally applied to calculating the error of a correlation coefficent!
- Wound up using only 4 of the variables for  $\Lambda^0$  modes.
- Orthogonally, checked discrimination power using  $q\bar{q}$  MC or  $q\bar{q} + B\bar{B}$  MC as background training sample.
#### Bootstrap method

- Efron (1982)
- Numerical procedure to estimate some *estimator*.
- When you only have *one* data sample.
- Originally applied to calculating the error of a correlation coefficent!
- How does it work?

- Given some dataset,  $\vec{x}$ , of size *n*.
- Need error of some characteristic of that dataset:  $\hat{\rho}$

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- Sample from original dataset to create multiple (1000) datasets of *n* entries.
  - $\vec{x} = (0, 1, 2, 3, 4)$

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• 
$$\vec{x} = (0, 1, 2, 3, 4)$$

•  $\vec{x}_0 = (4, 4, 0, 2, 3)$ 

- $\vec{x}_1 = (1, 4, 3, 4, 0)$
- $\vec{x}_2 = (3, 4, 2, 1, 4)$
- :

3) ( 3)

- Given some dataset,  $\vec{x}$ , of size *n*.
- Need error of some characteristic of that dataset:  $\hat{\rho}$
- Sample from original dataset to create multiple (1000) datasets of *n* entries.

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$$\vec{x} = (0, 1, 2, 3, 4)$$
  
•  $\vec{x}_0 = (4, 4, 0, 2, 3)$   
•  $\vec{x}_1 = (1, 4, 3, 4, 0)$   
•  $\vec{x}_2 = (3, 4, 2, 1, 4)$   
•  $\vdots$ 

- For each dataset, calculate it's own  $\hat{\rho}^*$ .
- Use this distribution to quote a confidence interval (95% in upcoming examples)

#### CORRELATION COEFFICIENTS

#### Look in regions of $\Delta E/m_{ES}$ plane.



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Image: A matrix and a matrix

## CORRELATION COEFFICIENTS

#### Look in regions of $\Delta E/m_{ES}$ plane.



- Red region of histogram shows 95% confidence interval.
- Black solid line shows value of correlation coefficient for original dataset.
- Blue dashed line is at 0.

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## SUMMARY OF CORRELATION COEFFICIENTS

Decay Mode	Training sample	# vars.	Region 1	Region 2	Region 3
$\Lambda_c^+ \mu^-$	qq	6	(-0.09, 0.02)	(-0.11, 0.01)	( 0.07, 0.18)
$\Lambda_c^+ e^-$	$q\bar{q}$	6	(-0.11, 0.03)	(-0.19,-0.07)	(-0.02, 0.11)
$\Lambda^0 \mu^-$	qq	4	(-0.18,-0.02)	(-0.28,-0.12)	( 0.07, 0.23)
$\Lambda^0 e^-$	qq	4	(-0.09, 0.08)	(-0.00, 0.15)	(-0.03, 0.16)
$\bar{\Lambda^0}\mu^-$	qq	4	( 0.02, 0.15)	(-0.07, 0.07)	(-0.24,-0.11)
$\overline{\Lambda^0}e^-$	qq	4	(-0.12, 0.11)	(-0.25,-0.02)	(-0.26,-0.04)

TABLE: Confidence intervals of correlation coefficients for different modes/regions. Red intervals are inconsistent with 0

Doesn't appear to be able to create a peak!

- Summary of MVA studies.
  - Used MLP neural net implementation in TMVA
  - Used  $q\bar{q}$  MC as background training sample.
  - Optimized cut on neural net output for  $\Lambda^0\ell$  modes.
  - Loose cut (90% signal efficiency) for  $\Lambda_c^+ \ell$  modes.
    - Will include in fit as third variable in fit for  $\Lambda_c^+ \ell$  modes.

TABLE: Remaining events after all cuts for each decay mode for both fitting region (still blinded) and estimated signal region.

Decay Mode	Fitting region	Signal region		
$\Lambda_c^+\mu^-$	900	18-25		
$\Lambda_c^+ e^-$	700	14-20		
$\Lambda^0 \mu^-$	350	7-10		
$\Lambda^0 e^-$	220	5-8		
$\bar{\Lambda^0}\mu^-$	220	5-8		
$\overline{\Lambda^0}e^-$	80	1-3		

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#### FITS

Unbinned extended maximum likelihood method.

$$\mathcal{L} = \frac{e^{-\nu}\nu^n}{n!} \times \prod_i^n \mathcal{P}(\vec{x}, \vec{k})$$

• PDF  $\mathcal{P}(\vec{x}, \vec{k})$  provided for signal and background.

- Conversion factor (F) turns number of signal events into branching fraction (B).
  - $\mathcal{B}(B \to \Lambda \ell) = n_{\mathrm{sig}}/\mathcal{F}$

• We include a Gaussian constraint on conversion factor than incorporates systematic errors.

- Takes into account asymmetric errors.
- Incorporates systematics into the upper limit calculation.

$$LH = \frac{(\mathcal{F} - \mathcal{F}_{fit})^2}{2\sigma_{\mathcal{F}}^2} - \sum_i^n \ln \mathcal{L}$$

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#### m<sub>ES</sub>

- Signal PDF: Crystal Ball function.
- Background PDF: Argus function.
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  - Signal PDF: Double Crystal Ball function. Constrained to have the same mean.
  - Background PDF: Linear function.
- *NN* output (only in  $\Lambda_c$  fits)
  - Signal PDF: RooKeysPdf. Adaptive kernel estimation.
  - Background PDF: Crystal Ball function.

#### PDF DESCRIPTIONS



FIGURE:  $\Lambda_c \mu$  decay mode. Fits to the signal and generic MC.

$$\mathcal{B}(\mathcal{B} 
ightarrow \mathrm{baryon} + \mathrm{lepton}) = rac{N_{\mathrm{sig}}}{\epsilon_{\mathrm{sig}} imes \mathcal{B}_{\mathrm{baryon}} imes N_{Bar{B}} imes 2.0 imes \mathcal{B}_{\mathrm{neut./chgE}}}$$

- N<sub>sig</sub>: The number of signal events.
- $\epsilon_{sig}$ : Signal reconstruction efficiency.
- $\mathcal{B}_{baryon}$ : Baryon branching fraction.
- N<sub>BB</sub>: The number of BB pairs.
- $\mathcal{B}_{neut./chgB}$ : The branching fraction of the  $\Upsilon(4S)$  to either a charged or neutral  $B\overline{B}$  pair.

#### $\operatorname{TABLE:}$ Contributions to the systematic uncertainty on the branching fraction.

			Decay i	mode		
Contribution	$\Lambda_c^+ \mu$	$\Lambda_c^+ e$	$\Lambda^{0}\mu$	$\Lambda^0 e$	$  \bar{\Lambda}^0 \mu$	$  \overline{\Lambda}^0 e$
B counting (%)	0.28	0.28	0.28	0.28	0.28	0.28
Charged/neutral B's (%)	1.24	1.24	1.24	1.24	1.24	1.24
Efficiency (MC stat.) (%)	0.33	0.33	0.30	0.30	0.30	0.30
$\Lambda_{(c)}$ Branching fraction (%)	26.00	26.00	0.78	0.78	0.78	0.78
Tracking eff. (%)	0.50	0.50	0.38	0.38	0.38	0.38
PID eff. (%)	2.70	2.10	2.50	1.70	2.50	1.70
Total (%)	26.21	26.16	3.05	2.54	3.02	2.49

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#### UPPER LIMIT CALCULATION

- Perform likelihood scan as function of  $\mathcal{B}$ .
- Integrate under the curve *above*  $\mathcal{B} = 0$ .
- Interpret  $\mathcal{B}$  at 90% of the area above 0 as upper limit.
- Define  $\mathcal{B}_{best}$  be the best solution for the branching fraction.

$$\begin{aligned} \Delta \mathcal{L} &= \ln \mathcal{L}(\mathcal{B}_{\text{best}}) - \ln \mathcal{L}(\mathcal{B}) \\ y &= e^{\Delta \mathcal{L}} \end{aligned}$$





## SIGNIFICANCE OF SIGNAL

- Use ratio of likelihoods.
- Best  $\mathcal{B}$  and  $\mathcal{B} = 0$ .

$$\sigma = \sqrt{2 \cdot (\ln \mathcal{L}(\mathcal{B}_{\text{best}}) - \ln \mathcal{L}(\mathcal{B}_{0}))}$$



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#### TOY STUDIES

- Ran 100k's of toy studies to determine *bias* and *sensitivity*.
- Can run 1000 toy studies at a given branching fraction.
- Count what % show a  $3\sigma$ ,  $4\sigma$  or  $5\sigma$  observation.



- Summary of toy studies.
  - Possible bias?
    - Negligible, less than errors on yield.
  - Sensitivity to a  $5\sigma$  discovery

$$egin{array}{lll} \mathcal{B}(B o \Lambda_c \ell) &pprox & 400 imes 10^{-8} \ \mathcal{B}(B o \Lambda^0 \ell) &pprox & 25 imes 10^{-8} \end{array}$$

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### FITTING PROCEDURE

Simulated data

 $\ensuremath{\operatorname{Figure:}}$  Figure: Fit to simulated data

 $B \to \Lambda_c^+ \mu^-$ 



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 $B 
ightarrow \Lambda_c^+ e^-$ 



 $B 
ightarrow \Lambda^0 \mu^-$ 



 $B\to \Lambda^0 e^-$ 



 $B 
ightarrow ar{\Lambda}^0 \mu^-$ 



 $B 
ightarrow ar{\Lambda}^0 e^-$ 



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TABLE: Upper limits on branching fractions at 90% confidence level for the six decay modes.

Decay mode	Upper limit		
$B^0  ightarrow \Lambda_c^+ \mu$	$170  imes 10^{-8}$		
$B^0  o \Lambda_c^+ e$	$500  imes 10^{-8}$		
$B^-  o \Lambda^0 \mu$	$6.0 imes10^{-8}$		
$B^-  ightarrow \Lambda^0 e$	$8.2 imes10^{-8}$		
$B^-  ightarrow ar{\Lambda}^0 \mu$	$6.3 imes10^{-8}$		
$B^-  ightarrow ar{\Lambda}^0 e$	$3.1 imes10^{-8}$		

Most signifcant branching fraction:

$$\mathcal{B}(B^0 \to \Lambda_c^+ e^-) = (190^{+130}_{-94}) \times 10^{-8} \text{ at } 2.4\sigma$$

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Image: A matrix and a matrix

- Interesting physics analysis.
- Submitted to PRD-RC.

- Interesting physics analysis.
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- Similar analysis still left to be done.
- Much more physics left in BaBar dataset!

-

- Interesting physics analysis.
- Submitted to PRD-RC.
- Similar analysis still left to be done.
- Much more physics left in BaBar dataset!
- Thanks for your time!

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- A. D. Sakharov, Pisma Zh. Eksp. Teor. Fiz. **5**, 32 (1967) [JETP Lett. **5**, 24 (1967 SOPUA,34,392-393.1991 UFNAA,161,61-64.1991)].
- K. Nakamura [Particle Data Group], J. Phys. G 37, 075021 (2010).
- W. S. Hou, M. Nagashima and A. Soddu, Phys. Rev. D 72, 095001 (2005).



A. Roodman, [physics/0312102]. HEP :: Search :: Help Powered by Invenio v1.0.0-rc0+ Problems/Questions to feedback@inspirebeta.net

# Backup slides

M. Bellis Mar. 2011

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• Pruned discriminating variables to most sensitive that did not have high correlations with  $\Delta E/m_{ES}$ .

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- Six variables.
  - *B* cos(*θ*) CM
  - $B \cos(\theta)$  sphericity wrt ROE sphericity
  - $B \cos(\theta)$  thrust wrt ROE thrust
  - Legendre P2
    - Legendre moments
    - Use ROE tracks, and B-thrust axis
  - Thrust all
  - R2 all
    - Ratio of Fox-Wolfram moments (0 and 2)
    - Whole event variables.
    - Both charged and neutral tracks.

#### OVERTRAINING TEST

- For one mode  $(\overline{\Lambda^0}e^-)$ , some correlation with both  $\Delta E/m_{ES}$  in generic MC background.
- But none in *signal MC*.
- Previous studies showed MLP classifier was not sensitive to overtraining.
- Questions remain:
  - For the  $\Lambda_c$  modes, which training sample gives us better sensitivity?
  - Is there a danger of creating an artificial peak?

#### OVERTRAINING TEST

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- But none in *signal MC*.
- Previous studies showed MLP classifier was not sensitive to overtraining.
- Questions remain:
  - For the  $\Lambda_c$  modes, which training sample gives us better sensitivity?
  - Is there a danger of creating an artificial peak?
- These are somewhat correlated.
- There may be some concern about two of the training variables: R2 (all), Thrust (all)
- Our approach:
  - For each mode run 4 TMVA training sessions.
    - Train using qq and 4 variables.
    - Train using  $q\bar{q}$  and 6 variables.
    - Train using  $q\bar{q} + B\bar{B}$  and 4 variables.
    - Train using  $q\bar{q} + B\bar{B}$  and 6 variables.
  - Generate sig eff. vs. bkg. rej. using signal MC and all the generic MC.
  - Generate sig eff. vs. bkg. rej. using signal MC and sideband data for comparison.

## TRAINING SAMPLE/VARIABLE CHOICE

Curves generated with generic MC and sideband data:  $\Lambda_c \mu^-$  (zoomed in)


Curves generated with generic MC and sideband data:  $\Lambda_c e^-$  (zoomed in)



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Curves generated with generic MC and sideband data:  $\Lambda^0\mu^-$ 



Curves generated with generic MC and sideband data:  $\Lambda^0 e^-$ 



Curves generated with generic MC and sideband data:  $\bar{\Lambda^0}\mu^-$ 



Curves generated with generic MC and sideband data:  $\bar{\Lambda^0}e^-$ 



- At this point it seems like I can use any of the combinations.
- Little difference amongst them all.
- However...are any of these combinations producing an artifical peak?
- Can see if the MLP (neural net) output is correlated with  $m_{ES}/\Delta E$ .
- But how to do that?
- Look at correlation coefficents between neural net output and  $\Delta E/m_{ES}$  plane.
- How to isolate signal region of  $\Delta E/m_{ES}$  plane?

# CORRELATION COEFFICIENTS

#### Look in regions of $\Delta E/m_{ES}$ plane.



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#### CORRELATION COEFFICIENTS

#### Look in regions of $\Delta E/m_{ES}$ plane.



- Danger would be a positive, positive, negative correlation, respectively, for these three regions.
- But how to determine if correlation is significant?

- Return to fitting procedure.
- Questions to answer with toy studies.
  - How the upper limit be calculated? review...
  - How will significance of "signal" be determined? review...
  - What is my sensitivity to a signal? NEW!
  - What is the chance of a false positive? NEW!
  - Are there any inherent bias' in the fitting procedure? NEW!

- Return to fitting procedure.
- Questions to answer with toy studies.
  - How the upper limit be calculated? review...
  - How will significance of "signal" be determined? review...
  - What is my sensitivity to a signal? NEW!
  - What is the chance of a false positive? NEW!
  - Are there any inherent bias' in the fitting procedure? NEW!
- Take a look at some trials...

Signal: Fit



Background: Fit



- 1000 trials
- 1400 background (Poisson fluctuated)
- 0 signal



- 1000 trials
- 1400 background (Poisson fluctuated)
- 20 signal (Toy, Poisson fluctuated and fixed number)



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Image: A matrix and a matrix

- 1000 trials
- 1400 background (Poisson fluctuated)
- 20 signal (Full simulation, Poisson fluctuated and fixed number)



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Image: A matrix and a matrix

- How to summarize this?
- As a function of number of embedded signal events plot:
  - Number of extracted (fit) events for toy signal.
  - Number of extracted (fit) events for fully simulated signal.
- Because of issues that have only recently come up, I will show this for the *full 3D fit* and for a 2D fit to the  $\Delta E/m_{ES}$  plane only.
- Both of these have a loose cut on the NN output ( $\approx$  90% signal efficiency)

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 $\Lambda_c^+\mu^-$  3D fit



 $\Lambda_c^+\mu^-$  2D fit



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 $\Lambda_c^+ e^-$  3D fit



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 $\Lambda_c^+ e^-$  2D fit



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 $\Lambda^0\mu^-$  3D fit



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 $\Lambda^0\mu^-$  2D fit



 $\Lambda^0 e^-$  3D fit



 $\Lambda^0 e^-$  2D fit



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 $\bar{\Lambda^0}\mu^-$  3D fit



 $\bar{\Lambda^0}\mu^-$  2D fit



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 $\bar{\Lambda^0}e^-$  3D fit



 $\bar{\Lambda^0}e^-$  2D fit



#### Λ<sub>c</sub> modes.

- $\Lambda_c^+\mu^-$ : (+5,+10)% on extracted signal events (both 2D and 3D).
- $\Lambda_c^+ e^-$ : (+3,6)% on extracted signal events (2D only).
- $\Lambda^0$  modes are unstable in 3D fits. About 25% fits don't converge.
  - $\Lambda^0 \mu^-$ : (-3,0)% on extracted signal events (2D).
  - $\Lambda^0 e^-$ : (-10,+2)% on extracted signal events (2D).
  - $\overline{\Lambda^0}\mu^-$ : (+1,+4)% on extracted signal events (2D).
  - $\overline{\Lambda^0}e^-$ : (0,+5)% on extracted signal events (2D).
- How does this map onto sensitivity?
- Review UL and significance calculation...

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#### UPPER LIMIT

- Likelihood scan.
  - *n* = Number of signal events.
  - *n*<sub>0</sub> = Number of signal events, best solution.

• 
$$y = -\ln \mathcal{L}(n) - -\ln \mathcal{L}(n_0)$$



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#### UPPER LIMIT

- Likelihood scan.
  - *n* = Number of signal events.
  - n<sub>0</sub> = Number of signal events, best solution.
  - $y = -\ln \mathcal{L}(n) -\ln \mathcal{L}(n_0)$
- Upper limit
  - Area under likelihood curve.
  - $y = e^{-\ln \mathcal{L}(n) -\ln \mathcal{L}(n_0)}$
  - Integrate under curve to find total area *above* 0.
  - Integrate under curve up above 0 up to to 90% of this area.
  - This is the UL at 90% confidence.
  - Plan to publish curve for others to draw their own conclusions.



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#### UPPER LIMIT

- 1000 studies
  - Background from PDF (1400 events, Poisson fluctuated)
  - No signal events.



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# SIGNIFICANCE OF SIGNAL

- Likelihood scan.
  - *n* = Number of signal events.
  - *n*<sub>0</sub> = Number of signal events, best solution.

• 
$$y = -\ln \mathcal{L}(n) - -\ln \mathcal{L}(n_0)$$



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#### SIGNIFICANCE OF SIGNAL

- Likelihood scan.
  - *n* = Number of signal events.
  - n<sub>0</sub> = Number of signal events, best solution.
  - $y = -\ln \mathcal{L}(n) -\ln \mathcal{L}(n_0)$
- Significance
  - If there is no signal in nature, what are the odds that the background fluctuates to give a false peak?
  - How many σ's is the extracted signal yield from 0.
  - Assume  $\mathcal{L}$  is Gaussian in region of best solution.

• 
$$\mathcal{L}(n) = e^{-n^2/2\sigma^2}$$

• 
$$\sigma = \sqrt{2(\ln \mathcal{L}(0) - \ln \mathcal{L}(n_0))}$$



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### SIGNIFICANCE OF SIGNAL

- 1000 studies
  - Background from PDF (800 events, Poisson fluctuated)
  - No signal events.
- Negative yields have 0 significance.
- Number of trials greater than some significance?
  - 3σ: 1
  - 4σ: 0
  - 5σ: 0
- APOLOGIES: In upcoming plots, ignore RED axis at top. Currently a plotting artifact that will eventually be calculated correctly.



 $\Lambda_c^+\mu^-$  Toy signal (3D),



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 $\Lambda_c^+\mu^-$  Toy signal (3D), Full simulation (3D),



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$\Lambda_c^+\mu^-$  Toy signal (3D), Full simulation (3D), Full simulation (2D)



- The 3D and 2D fit, on average, extract same number of events, but the 2D fit has less sensitivity.
- Remind ourselves that the significance depends not just on the number of signal events extracted by the fit, but also the contours of the likelihood function itself.

 $\Lambda_c^+\mu^-$  Full simulation for signal, 12 embedded events (not Poisson fluctuated), 3D fit



 $\Lambda_c^+\mu^-$  Full simulation for signal, 12 embedded events (not Poisson fluctuated), 2D fit



 $\Lambda_c^+\mu^-$  Full simulation for signal, 12 embedded events (not Poisson fluctuated), 3D fit



 $\Lambda_c^+\mu^-$  Full simulation for signal, 12 embedded events (not Poisson fluctuated), 2D fit



- Understand the difference.
- Implication?
- Define sensitivity as number of events (branching fraction) that 90% of the time, gives  $>5\sigma$  observation.
- Fitting with 2D loses only some sensitivity (5-15%).
- Other modes?

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Image: A matrix and a matrix

 $\Lambda_c^+ e^-$  Full simulation (3D),



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 $\Lambda_c^+ e^-$  Full simulation (3D), Full simulation (2D)



• For  $\Lambda^0$  modes, show only 2D fits (full simulation)

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 $\Lambda^0 \mu^-$  Full simulation (2D)



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 $\Lambda^0 e^-$  Full simulation (2D)



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 $\bar{\Lambda^0}\mu^-$  Full simulation (2D)



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 $\bar{\Lambda^0}e^-$  Full simulation (2D)



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