

Drell-Yan process and heavy boson production at hadron colliders

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June 4, 2007

Some references

- My slides are available from the CTEQ webpage or <http://hep.pa.msu.edu/nadolsky/tmp/cteqX.pdf>
- Feynman rules for tree helicity amplitudes involving massive quarks and bosons
Schwinn, Weinzierl, hep-th/0503015
- Gluon PDF in a pion (depends on theory assumptions)
Sutton, Martin, Roberts, Stirling, PRD 45, 2349 (1992); Gluck, Reya, Stratmann, hep-ph/9711369
- Multiple parton interactions in Pythia
Sjostrand, Mrenna, Skands, hep-ph/0603175, chapters 11.2-11.4

Outline

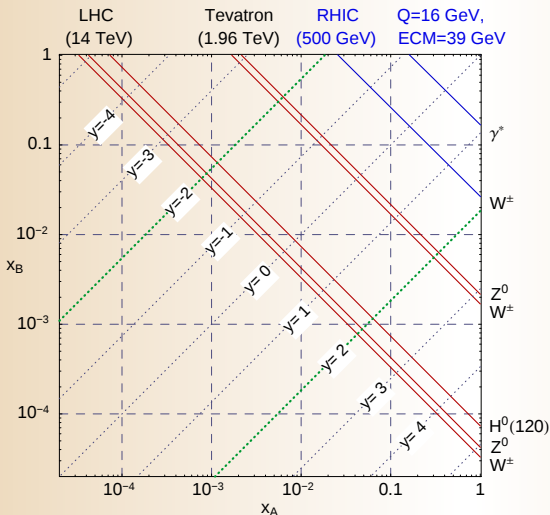
■ Saturday

- ▶ low- Q lepton pair production
- ▶ heavy electroweak bosons
- ▶ kinematics
- ▶ leading-order (LO) cross sections
- ▶ NLO/NNLO results

■ Monday

- ▶ modern applications
- ▶ QCD factorization and resummation of large logarithms
- ▶ new physics searches

Typical parton momentum fractions



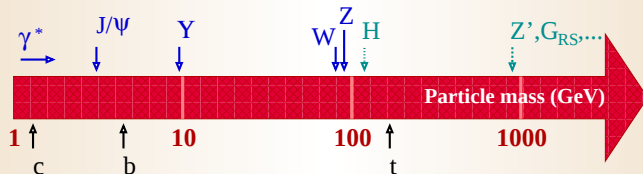
$$x_{A,B} \equiv \frac{Q}{\sqrt{s}} e^{\pm y}$$

Born level: $p_a^\mu = x_A p_A^\mu$,
 $p_b^\mu = x_B p_B^\mu$

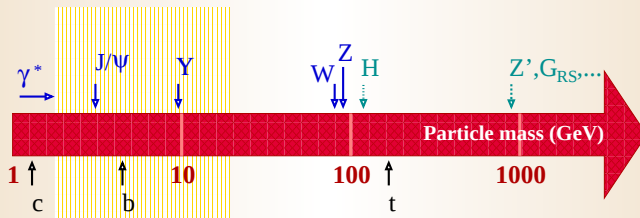
Typical rapidities in the experiment: $|y| \lesssim 2$

- experiments at higher energies are sensitive to PDF's at smaller x

Particle states probed by Drell-Yan-like processes

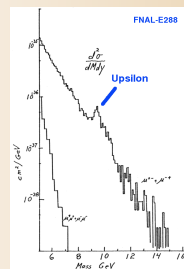
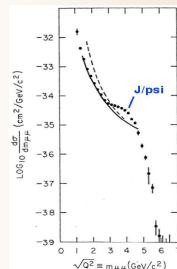


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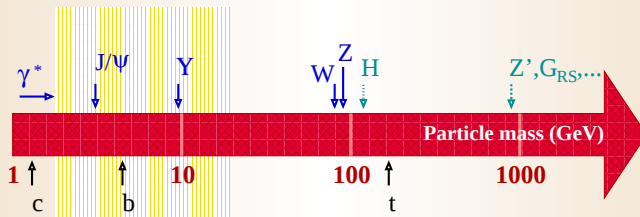


$$pN \xrightarrow{\gamma^*} \ell^+ \ell^- X \text{ at } Q < 20 \text{ GeV}$$

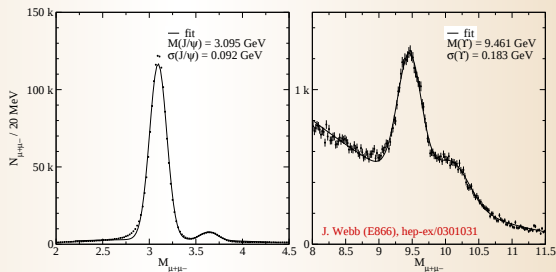
- Continuous γ^* cross section
- Multiple quarkonium resonances (neglected in the PDF fit)
- ▲ J/ψ ($c\bar{c}$)– found in e^+e^- scattering (1974)
- ▲ Υ ($b\bar{b}$)– found in $pN \rightarrow \mu^+ \mu^- X$ (FNAL-E288, 1977)



Particle states probed by Drell-Yan-like processes



$J/\psi, \Upsilon$
resonances
shown with
better
resolution
(FNAL-E866)



Constraints on quark sea from $pN \rightarrow \ell^+ \ell^- X$

($N = p, d, Fe, Cu, \dots$)

$$\frac{d\sigma_{pp}}{dQ^2 dy} \sim \left(\frac{2}{3}\right)^2 [u_A \bar{u}_B + \bar{u}_A u_B] + \left(-\frac{1}{3}\right)^2 [d_A \bar{d}_B + \bar{d}_A d_B] + \text{smaller terms}$$

$\Rightarrow$ sensitivity to $\bar{q}(x, Q)$

Assuming charge symmetry between protons and neutrons

($u_p = d_n, u_n = d_p$):

$$\frac{d\sigma_{pn}}{dQ^2 dy} \sim \left(\frac{2}{3}\right)^2 [u_A \bar{d}_B + \bar{u}_A d_B] + \left(-\frac{1}{3}\right)^2 [d_A \bar{u}_B + \bar{d}_A u_B] + \text{smaller terms}$$

If deuterium binding corrections are neglected:

$$q_d(x) \approx q_p(x) + q_n(x)$$

At $x_A \gg x_B$ (large y): $\bar{q}(x_A) \sim 0$ and $4u(x_A) \gg d(x_A)$

$$\frac{\sigma_{pd}}{2\sigma_{pp}} \approx \frac{\frac{1}{2} \left(1 + \frac{d_A}{4u_A}\right) [1 + r]}{\left(1 + \frac{d_A}{4u_A} r\right)} \approx \frac{1}{2} (1 + r), \text{ where } r \equiv \bar{d}(x_B)/\bar{u}(x_B)$$

$\therefore \sigma_{pd}/(2\sigma_{pp})$ constrains $\bar{d}(x, Q)/\bar{u}(x, Q)$ at moderate x

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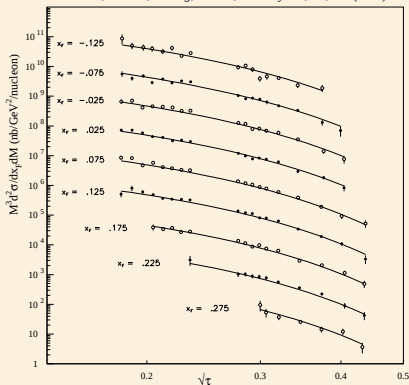
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Theory vs. experiment

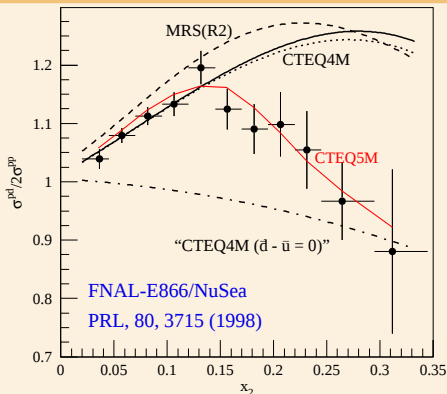
Cross section at $Q = 4 - 17 \text{ GeV}$

E605 (p Cu $\rightarrow \mu^+ \mu^- X$) $P_{\text{LAB}} = 800 \text{ GeV}$

Martin, Roberts, Stirling, Thorne, Eur. Phys. J., C4, 463 (1998)



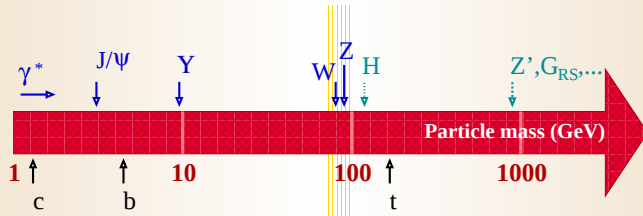
$\sigma_{pd}/(2\sigma_{pp})$ at large $x_F = x_A - x_B$



Theory curves reflect different assumptions about $\bar{d}/\bar{u}$

The recent PDF fits (e.g., CTEQ5M) quantitatively account for the violation of $SU(2)$ symmetry in the quark sea

Particle states probed by Drell-Yan-like processes



W and Z boson production

- good convergence of the α_s series
- small backgrounds
- separation of PDF flavors (via the CKM matrix)
- sensitivity to new physics

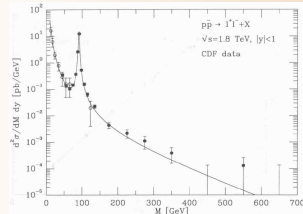


Fig. 9.5. The lepton pair cross section in $p\bar{p}$ collisions at $\sqrt{s} = 1.8$ TeV, with CDF data from ref. [12] (open circles) and ref. [13] (solid circles). The curve is the next-to-leading-order QCD prediction using the parton distributions from ref. [9].

Z pole and γ^* continuum in $\ell^+ \ell^-$ production

Leptonic vs. hadronic decay modes

The W and Z branching ratios $\text{Br}_i \equiv \Gamma_i/\Gamma$ are

- $\text{Br}[W \rightarrow \ell \nu_\ell] \approx 3 \times 11\%$, $\text{Br}[W \rightarrow \text{jets}] \approx 68\%$
- $\text{Br}[Z \rightarrow \ell^+ \ell^-] = 3 \times 3.36\%$, $\text{Br}[Z \rightarrow \nu_\ell \bar{\nu}_\ell] = 3 \times 6.67\%$,
 $\text{Br}[Z \rightarrow \text{jets}] \approx 70\%$

At $\sqrt{s}$ of a few TeV, hadronic W , Z decays cannot be observed because of the large background (mostly $q\bar{q}, g\bar{g} \rightarrow \text{jets}$)

Despite small branching ratios, the only viable decay modes are

- $Z \rightarrow e^+ e^-, Z \rightarrow \mu^+ \mu^-$
- $W \rightarrow e + \nu_e, W \rightarrow \mu + \nu_\mu$, with neutrinos identified by missing transverse energy E_T

A quiz on W boson kinematics

Consider $AB \rightarrow (W^+ \rightarrow e^+ \nu_e) X$ decay in the lab frame.

The most probable **transverse momentum Q_T of the W boson** is

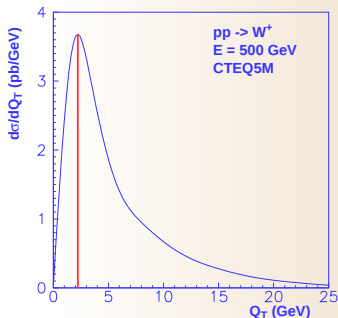
- a) $Q_T = \sqrt{s}/2$
- b) $Q_T = |\vec{p}_T^e| + E_T$
- c) $Q_T = 0$
- d) $Q_T = 2 - 5 \text{ GeV}$,
depending on $\sqrt{s}$

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- c) $Q_T = 0$
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depending on $\sqrt{s}$



The LO condition $Q_T = 0$ (corresponding to no QCD radiation) is never realized because of self-suppression of very soft QCD contributions (Sudakov suppression). To predict $d\sigma/dQ_T$ at $Q_T \ll Q \sim M_W$, one needs to resum such soft contributions to all orders in α_S .

A quiz on W boson kinematics

Consider $AB \rightarrow (W^+ \rightarrow e^+ \nu_e) X$ decay in the lab frame.

The most probable **transverse momentum** p_T^e of the positron is

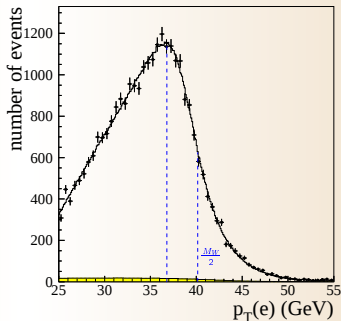
- a) $p_T^e = 0 - 5 \text{ GeV}$
- b) $p_T^e \approx 40 \text{ GeV}$
- c) $p_T^e \approx 80 \text{ GeV}$
- d) $p_T^e = Q_T/2$

A quiz on W boson kinematics

Consider $AB \rightarrow (W^+ \rightarrow e^+ \nu_e) X$ decay in the lab frame.

The most probable **transverse momentum** p_T^e of the positron is

- a) $p_T^e = 0 - 5 \text{ GeV}$
- b) $p_T^e \approx 40 \text{ GeV} = M_W/2$
- c) $p_T^e \approx 80 \text{ GeV}$
- d) $p_T^e = Q_T/2$



$d\sigma/dp_T^e$ has a kinematical (Jacobian) peak,

■ ...located exactly at $p_T^e = M_W/2$ if $Q_T = 0$ and $Q = M_W$

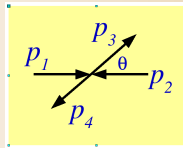
■ ...smeared by higher-order EW and soft QCD corrections

The origin of the Jacobian peak

In the
Collins-Soper
 W rest frame,
for $Q = M_W$:

$$p_T^e = |\vec{p}_1| \sin \theta_* = \frac{M_W}{2} \sin \theta_*$$

$$\frac{d\sigma}{d \cos \theta_*} = \sum_j F_j(Q, Q_T, y) a_j(\theta_*, \varphi_*)$$



$a_1 = 1 + \cos^2 \theta_*$, $a_2 = 2 \cos \theta_*$, etc. (smooth functions)

$$\frac{d\sigma}{dp_T^e} = \underbrace{\left| \frac{d \cos \theta_*}{dp_T^e} \right|}_{\text{Jacobian}} \frac{d\sigma}{d \cos \theta_*} = \frac{1}{\sqrt{1 - \left(\frac{2p_T^e}{M_W} \right)^2}} \frac{4p_T^e}{M_W^2} \frac{d\sigma}{d \cos \theta_*}$$

$$\frac{d\sigma}{dp_T^e} \rightarrow \infty \text{ if } p_T^e \rightarrow M_W/2 (!)$$

The origin of the Jacobian peak

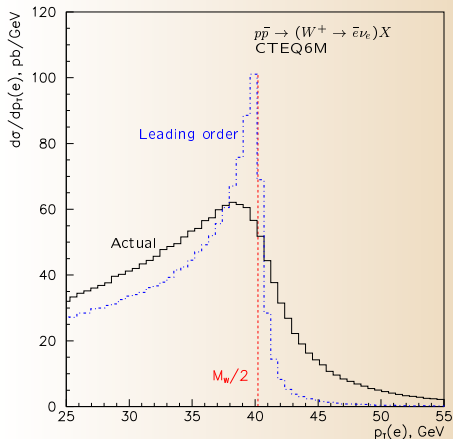
If $Q_T = 0$: $(p_T^e)_{\text{lab frame}} = (p_T^e)_{\text{CS frame}}$

(the boost from the CS frame to the lab frame is along the z -axis)

Corrections to $d\sigma/dp_T^e$ are of order

■ $\mathcal{O}(\Gamma_W^2/M_W^2)$ due to the non-zero W width Γ_W ($Q \neq M_W$)

■ $\mathcal{O}(Q_T/Q)$ due to the boost $\Rightarrow$ sensitivity to the shape of $d\sigma/dQ_T$ (soft radiation) at $Q_T \ll Q$



A similar Jacobian peak is present in $d\sigma/dp_T^\nu$

Lepton transverse mass

Definition

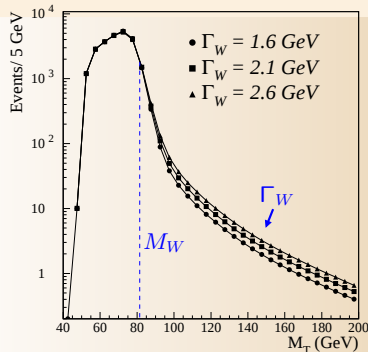
$M_T^{e\nu} \equiv 2(p_T^e p_T^\nu - \vec{p}_T^e \cdot \vec{p}_T^\nu)$ in the lab frame (Smith, van Neerven, Vermaseren, 1983)

Exercise

Assuming $Q_T = 0$, verify that there is a Jacobian peak in $d\sigma/dM_T^{e\nu}$ at $M_T^{e\nu} = M_W$

■ Corrections to $d\sigma/dM_T^{e\nu}$ are of order $\mathcal{O}(Q_T^2/Q^2) \Rightarrow$ reduced sensitivity to small- Q_T soft contributions

■ $d\sigma/dM_T^{e\nu}$, $d\sigma/dp_T^e$, and $d\sigma/dp_T^\nu$ are important observables. They are commonly used to measure M_W . Γ_W is found from $d\sigma/dM_T^{e\nu}$ at large $M_T^{e\nu}$



W and Z production as a “luminosity monitor”

(Dittmar, Pauss, Zuercher; Khoze, Martin, Orava, Ryskin; Giele, Keller';...)

- Cross sections for $pp \rightarrow W^\pm X$, $pp \rightarrow Z^0 X$ at the LHC can be measured with accuracy $\delta\sigma/\sigma \sim 1\%$ (tens of millions of events even at low luminosity)
- These measurements can be employed to
 - ▶ measure all other LHC cross sections in units of $\sigma_{W,Z}^{LHC}$
 - ▶ measure magnitudes of $\sigma_{W,Z}^{LHC}$; use them to monitor the LHC luminosity in real time
 - ▶ precisely measure PDF's (parton luminosities); reduce theory uncertainties for tiny new physics signals and huge SM backgrounds

The accuracy of luminosity monitoring in $p\bar{p}$ elastic scattering at the Tevatron is of order 5%

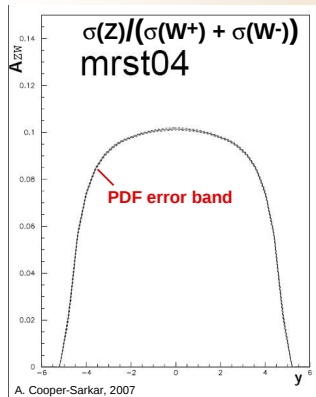
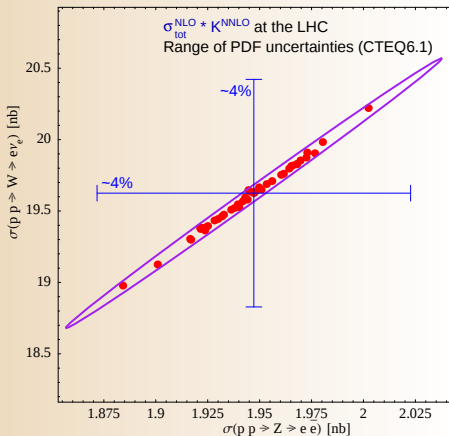
Theoretical aspects of luminosity monitoring

Several factors contribute to W & Z cross sections at a percent level, including

- $\mathcal{O}(\alpha_s^2)$, or NNLO, QCD corrections
- $\mathcal{O}(\alpha)$, or NLO, EW corrections
- PDF uncertainties
- Experimental acceptance
- QCD and EW showering (all-orders resummations)

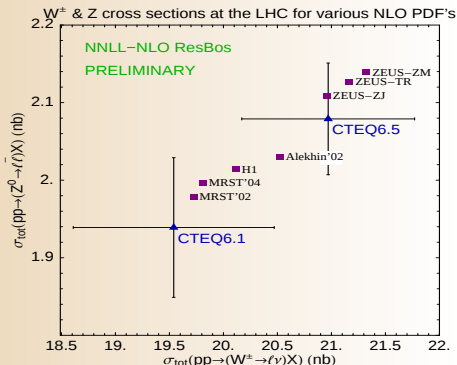
Sometimes, these effects (e.g., PDF dependence or constant K -factors) may cancel in ratios, but in many cases they do not

Ratios of W and Z cross sections



Radiative contributions, PDF dependence have similar structure in W , Z , and alike cross sections; cancel well in Xsection ratios

σ_Z vs. σ_W at NLO for various PDF sets



However, the PDF errors for cross sections themselves are still very appreciable

$$\text{CTEQ6.5/CTEQ6.1} \sim 1.07$$

- reflects a 7% increase in parton luminosities

$\mathcal{L}_{q_i \bar{q}_j}(x_1, x_2, Q) = q_i(x_1, Q) \bar{q}_j(x_2, Q)$ in the relevant x and Q ranges for u, d, s quarks (consequence of improved treatment of heavy-flavor masses in DIS at HERA)

Charged lepton asymmetry at the Tevatron

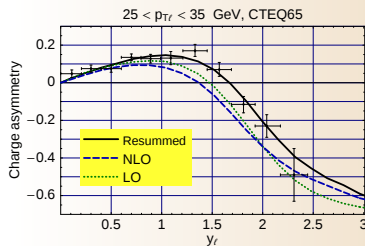
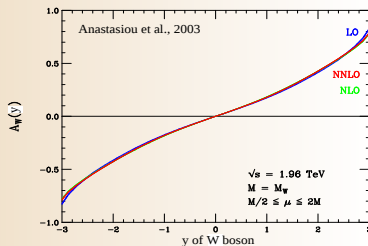
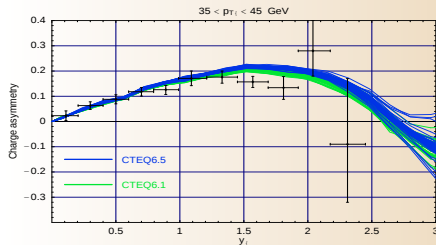
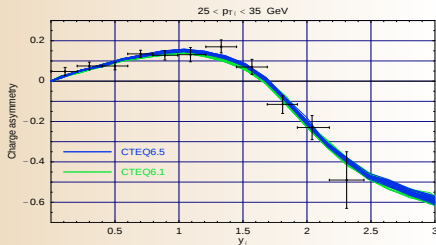
$$A_{ch}(y_e) \equiv \frac{\frac{d\sigma^{W^+}}{dy_e} - \frac{d\sigma^{W^-}}{dy_e}}{\frac{d\sigma^{W^+}}{dy_e} + \frac{d\sigma^{W^-}}{dy_e}}$$

- related to the boson Born-level asymmetry when y_e is large

$$A_{ch}(y) \xrightarrow{y \rightarrow y_{max}} \frac{r(x_B) - r(x_A)}{r(x_B) + r(x_A)}, \quad r(x) \equiv \frac{d(x, M_W)}{u(x, M_W)}$$

- constrains the PDF ratio $d(x, M_W)/u(x, M_W)$ at $x \rightarrow 1$
- In experimental analyses, a selection cut $p_{Te} > p_{Te}^{min}$ is imposed

Charge asymmetry in p_T^e bins (CDF Run-2)



■ With p_{Te} cuts imposed, $A_{ch}(y_e)$ is sensitive to small- Q_T resummation

Factorization for inclusive cross sections

Scale dependence of the renormalized QCD charge $g(\mu)$ and fermion masses $m_f(\mu)$:

$$\mu \frac{dg(\mu)}{d\mu} = \beta(g(\mu)), \quad \mu \frac{dm_f(\mu)}{d\mu} = -\gamma_m(g(\mu))m_f(\mu)$$

The RG equations predict that $\alpha_s(\mu) \rightarrow 0$ and $m_f(\mu) \rightarrow 0$ as $\mu \rightarrow \infty$

These features are employed to prove factorization for inclusive Drell-Yan cross sections (*Bodwin, PRD 31, 2616 (1985); Collins, Soper, Sterman, NPB 261, 104 (1985); B308, 833 (1988)*):

$$\begin{aligned} \frac{d\sigma(Q, \{m_f\})}{d\tau} &= \sum_{a,b} \int_{x_A}^1 d\xi_A \int_{x_B}^1 d\xi_B \frac{d\hat{\sigma}\left(\frac{Q}{\mu}, \frac{\tau}{\xi_A \xi_B}, \{m_f = 0\}\right)}{d\tau} f_{a/A}(\xi_A, \mu) f_{b/B}(\xi_B, \mu) \\ &+ \mathcal{O}\left(\{m_f^2/\mu^2\}\right) \end{aligned}$$

assuming $\mu \sim Q \sim \sqrt{s} \gg \{m_f\}, \Lambda_{QCD}$

Factorization for inclusive cross sections

$$\frac{d\sigma(Q, \{m_f\})}{d\tau} = \sum_{a,b} \int_{x_A}^1 d\xi_A \int_{x_B}^1 d\xi_B \frac{d\hat{\sigma}\left(\frac{Q}{\mu}, \frac{\tau}{\xi_A \xi_B}, \{m_f = 0\}\right)}{d\tau} f_{a/A}(\xi_A, \mu) f_{b/B}(\xi_B, \mu) + \mathcal{O}\left(\left\{m_f^2/\mu^2\right\}\right)$$

- The hard cross section $\hat{\sigma}$ is infrared-safe: $\lim_{\{m_f \rightarrow 0\}} \hat{\sigma}(\{m_f\})$ is finite and can be computed as a series in $\alpha_s(\mu)$
- Collinear logarithms are subtracted from $\hat{\sigma}$ and resummed in $f(\xi, \mu)$ using DGLAP equations
- Soft-gluon singularities in $\hat{\sigma}$ vanish when the sum of all Feynman diagrams is integrated over all phase space (Kinoshita-Lee-Nauenberg theorem)

Factorization for Q_T distributions

- Differential distributions may still contain integrable soft singularities of the type $\alpha_s^k \ln^m(Q^2/p_i \cdot p_j)$, e.g., $L \equiv \ln(Q^2/Q_T^2) \gg 1$:

$$\left. \frac{d\sigma}{dQ_T^2} \right|_{Q_T \rightarrow 0} \approx \frac{1}{Q_T^2} \left\{ \begin{aligned} &\alpha_S (L+1) \\ &+ \alpha_S^2 (L^3 + L^2 + L + 1) \\ &+ \alpha_S^3 (L^5 + L^4 + L^3 + L^2 + L + 1) \\ &+ \dots \end{aligned} \right\}.$$

The purpose of Q_T resummation is to reorganize this series as

$$\left. \frac{d\sigma}{dQ_T^2} \right|_{Q_T \rightarrow 0} \approx \frac{1}{Q_T^2} \left\{ \alpha_S Z_1 + \alpha_S^2 Z_2 + \dots \right\},$$

where $\alpha_S^{n+1} Z_{n+1} \ll \alpha_S^n Z_n$:

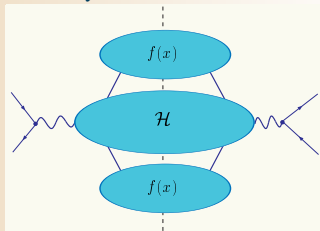
$$\begin{aligned} \alpha_S Z_1 &\sim \alpha_S (L+1) + \alpha_S^2 (L^3 + L^2) + \alpha_S^3 (L^5 + L^4) + \dots & | A_1, B_1, C_0 ; \\ \alpha_S^2 Z_2 &\sim \alpha_S^2 (L+1) + \alpha_S^3 (L^3 + L^2) + \dots & | A_2, B_2, C_1 ; \\ \alpha_S^3 Z_3 &\sim \alpha_S^3 (L+1) + \dots & | A_3, B_3, C_2 . \\ &\dots \end{aligned}$$

QCD factorization at large and small Q_T

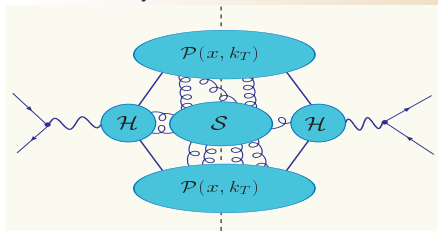
Finite-order (FO) factorization

Small- q_T factorization

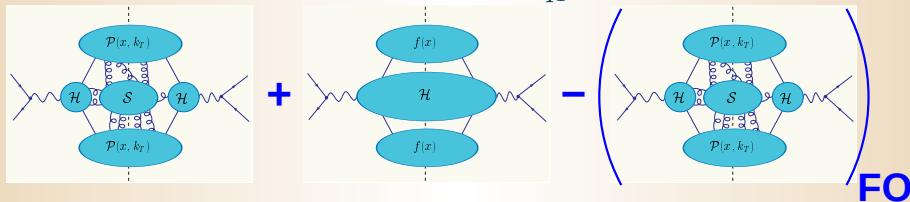
$$\Lambda_{QCD}^2 \ll q_T^2 \sim Q^2$$



$$\Lambda_{QCD}^2 \ll q_T^2 \ll Q^2$$



Solution for all q_T :



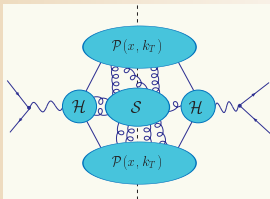
Factorization at $Q_T \ll Q$ (Collins, Soper, Sterman, 1985)

Realized in space of the impact parameter b

$$\left. \frac{d\sigma_{AB \rightarrow VX}}{dQ^2 dy dq_T^2} \right|_{q_T^2 \ll Q^2} = \sum_{\text{flavors}} \int \frac{d^2b}{(2\pi)^2} e^{-i\vec{q}_T \cdot \vec{b}} \widetilde{W}_{ab}(b, Q, x_A, x_B)$$

$$\widetilde{W}_{ab}(b, Q, x_A, x_B) = |\mathcal{H}_{ab}|^2 e^{-\mathcal{S}(b, Q)} \overline{\mathcal{P}}_a(x_A, b) \overline{\mathcal{P}}_b(x_B, b)$$

$\mathcal{H}_{ab}$ is the hard vertex, $\mathcal{S}$ is the soft (Sudakov) factor, $\overline{\mathcal{P}}_a(x, b)$ is the unintegrated PDF



For $b \ll 1 \text{ GeV}^{-1}$, $\widetilde{W}_{ab}(b, Q, x_A, x_B)$ is calculable in perturbative QCD; at $Q \sim M_Z$, this region dominates the resummed cross section

Nonperturbative contributions at large b

At $b \gtrsim 1 \text{ GeV}^{-1}$, the leading nonperturbative contribution is approximated as $\exp(-a(Q)b^2)$, where $a(Q)$ is an effective “nonperturbative parton $\langle k_T^2 \rangle / 4$ ” inside the proton

The RG invariance suggests that

$$a(Q) \approx a_1 + a_2 \ln Q,$$

where $a_{1,2} \sim \Lambda_{QCD}^2$, and a_2 is process-independent

The $\ln Q$ growth of $a(Q)$ is indeed observed in the Drell-Yan and Z p_T data

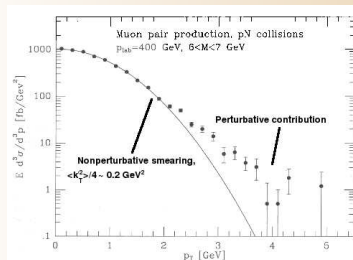
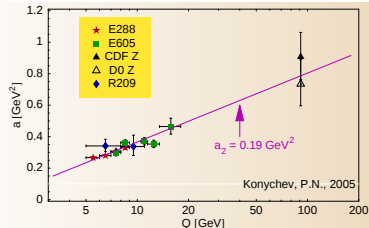
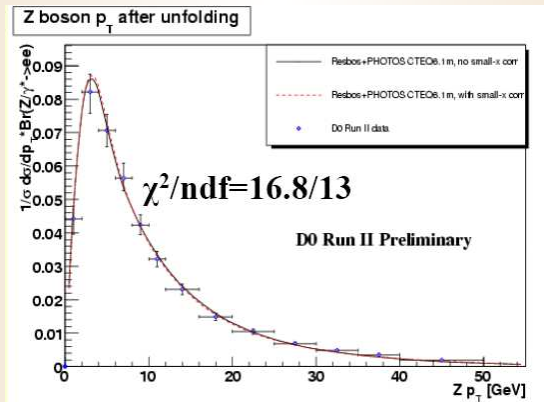


Fig. 9.2. The lepton pair transverse momentum from the CFS collaboration [4]. The curve corresponds to a Gaussian intrinsic k_T distribution for the annihilating



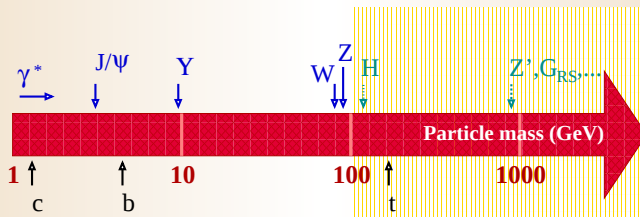
An example of the resummed cross section

Z production at the Tevatron vs. resummed NLO (*Balazs, Ladinsky, PN, Yuan*)



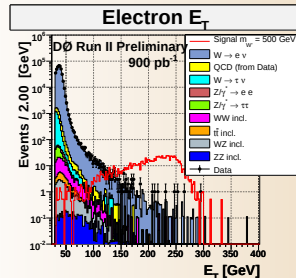
In this case, precise predictions for $d\sigma/dQ_T$ are needed to measure M_W with accuracy better than 0.03%

Particle states probed by Drell-Yan-like processes

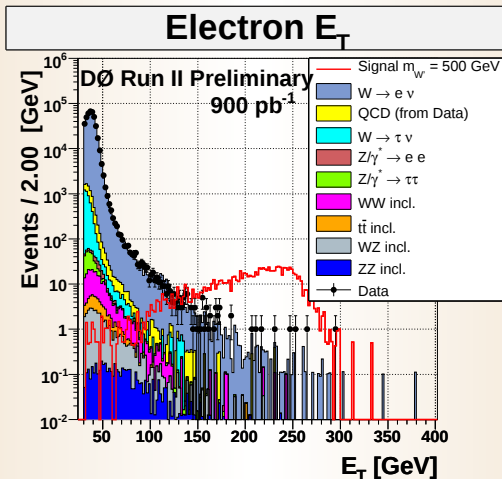


New physics at $Q > 100$ GeV

- Indirect constraints from electroweak precision measurements
- direct new physics searches

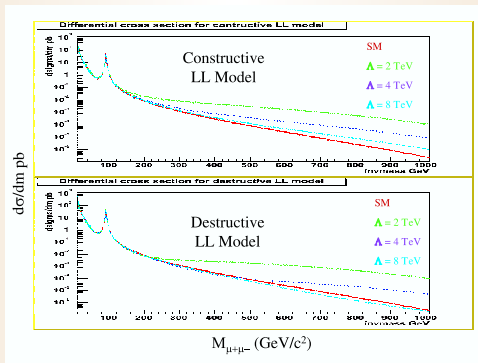


Search for heavy states at DO



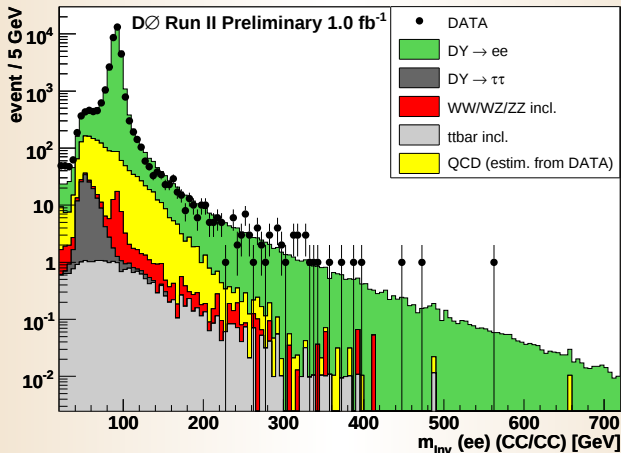
$$W' \rightarrow \ell \nu$$

Search for heavy states at DO



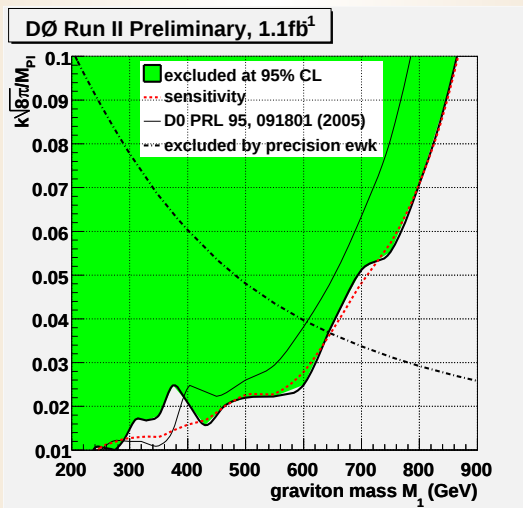
Leptoquark $\rightarrow \mu\mu$

Search for heavy states at DØ



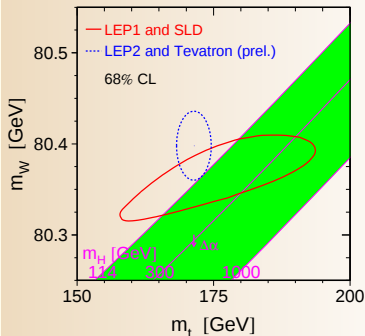
Contact interactions: $p\bar{p} \rightarrow e(e^* \rightarrow e\gamma)X$

Search for heavy states at DØ



Randall-Sundrum graviton $\rightarrow ee, \gamma\gamma$

Higgs sector in Standard Model & supersymmetry



SM: 1 Higgs doublet, one boson H

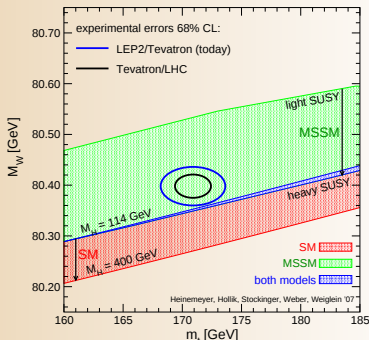
- Direct search:
 $m_H > 114$ GeV at 95% c.l.
- indirect: $M_H = 80^{+39}_{-28}$ GeV at 68% c.l.

MSSM: 2 Higgs doublets; $h^0, H^0, A^0, H^\pm$

$$m_h \leq m_Z |\cos 2\beta| + \text{rad. corr.} \lesssim 135 \text{ GeV}$$

- In these models, expect one or more Higgs bosons with mass below 140 GeV
- Many other possibilities for EW symmetry breaking exist!

Higgs sector in Standard Model & supersymmetry



SM band: $114 \leq M_H \leq 400$ GeV

SUSY band: random scan

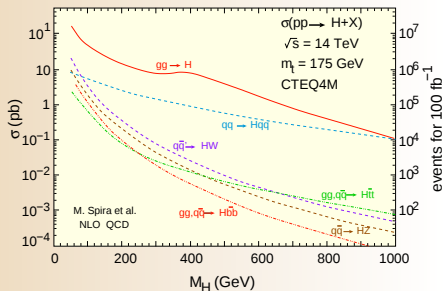
- the goal of direct and indirect measurements is to over-constrain SM, greatly constrain SUSY
- indirect constraints strongly depend on M_W , m_t values, hence require accurate QCD predictions for W and t production

For example, in SM

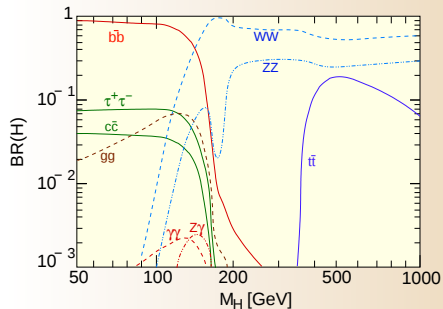
$$\begin{aligned}
 M_W = & 80.3827 - 0.0579 \ln \left(\frac{M_H}{100 \text{ GeV}} \right) - 0.008 \ln^2 \left(\frac{M_H}{100 \text{ GeV}} \right) \\
 & + 0.543 \left(\left(\frac{m_t}{175 \text{ GeV}} \right)^2 - 1 \right) - 0.517 \left(\frac{\Delta\alpha_{had}^{(5)}(M_Z)}{0.0280} - 1 \right) - 0.085 \left(\frac{\alpha_s(M_Z)}{0.118} - 1 \right)
 \end{aligned}$$

SM Higgs boson search at the LHC

Production rate

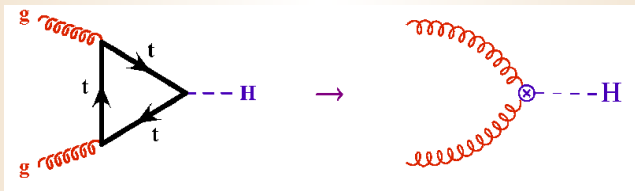


Branching ratios



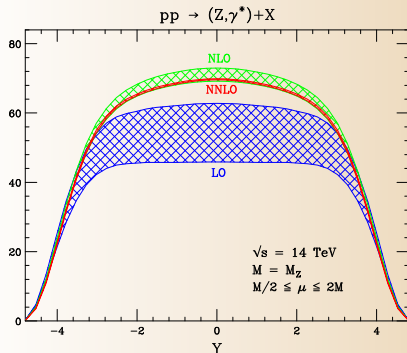
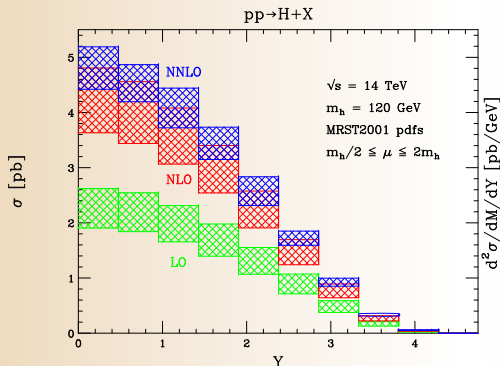
Let's concentrate on $gg \rightarrow H \rightarrow \gamma\gamma$, the leading search mode for $M_H < 140$ GeV (besides vector boson fusion and $t\bar{t}H$ production)

$$gg \rightarrow \text{Higgs} \rightarrow \gamma\gamma$$



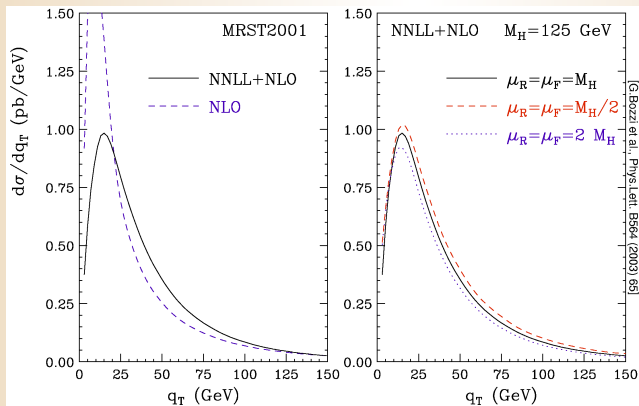
The scattering proceeds via a top quark loop, which can be replaced by an effective point vertex under the assumption $m_t^2 \gg m_H^2$ (works well for $m_H \lesssim 350$ GeV). This trick greatly simplifies calculations, which can be carried out up to two gluon loops (as in the Drell-Yan process). Many techniques developed for the Drell-Yan process also apply to Higgs production

Scale dependence of rapidity distributions



However, $gg \rightarrow H$ is characterized by slower convergence of the series in α_s than $q\bar{q} \rightarrow W, Z$

Q_T Resummation

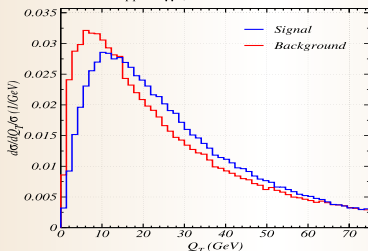


Q_T resummation for Higgs bosons has been carried out by several groups, and they are in a reasonable agreement (*Balazs, Yuan; Berger, Qiu; Bozzi et al.; Kulesza, Stirling; Kulesza, Sterman, Vogelsang*)

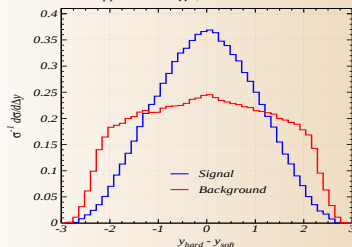
Resummed distributions for Higgs $\rightarrow \gamma\gamma$ signal and background

(ResBos, normalized; $M_H = 130$ GeV, $128 < Q < 132$ GeV)

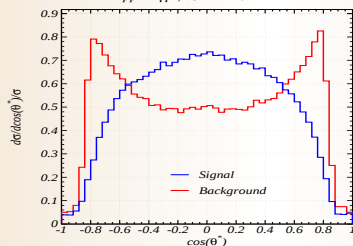
$pp \rightarrow \gamma\gamma X, \sqrt{S} = 14$ TeV



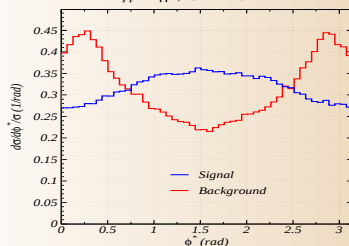
$pp \rightarrow HX \rightarrow \gamma\gamma X, \sqrt{S} = 14$ TeV



$pp \rightarrow \gamma\gamma X, \sqrt{S} = 14$ TeV



$pp \rightarrow \gamma\gamma X, \sqrt{S} = 14$ TeV



Q_T and $y_{\gamma_1} - y_{\gamma_2}$ in the lab frame

Decay angles θ^*, φ^* in the $\gamma\gamma$ rest frame

no singularities, in contrast to the fixed-order rate

Summary

Essential applications of Drell-Yan-like processes

- clean tests of QCD factorization
- studies of the nucleon structure (quark sea, flavor separation,...)
- “standard candle” processes (luminosity monitors....)
- electroweak precision measurements
- searches for new physics

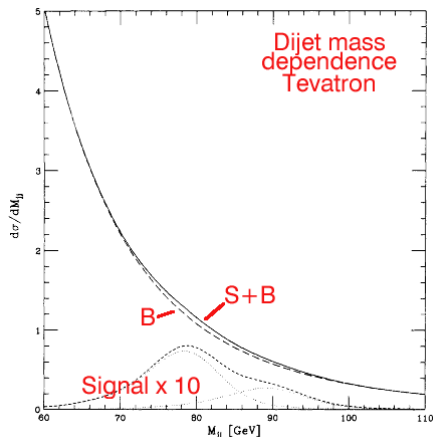
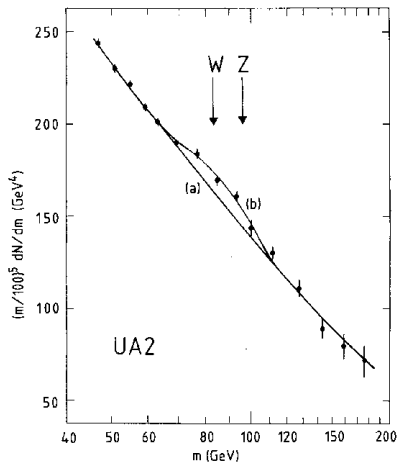
Many interesting topics were not covered

- Polarized Drell-Yan-like processes (measurements of new nucleon structure functions)
- Connections to k_T factorization in semi-inclusive DIS
- Various resummations (small x , threshold, heavy-quark....)
- Higher-twist and nuclear effects in low- Q Drell-Yan and heavy-ion scattering

Many exciting studies still remain to be done!

Backup slides

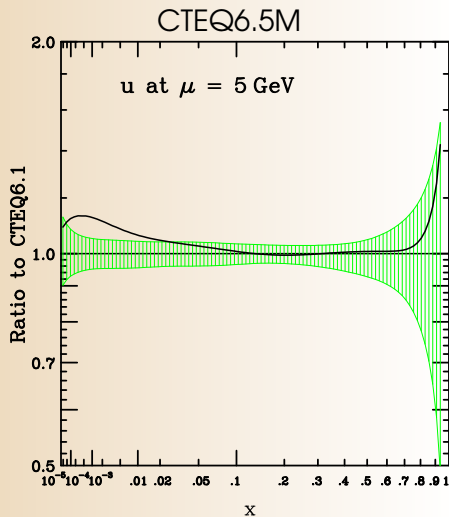
W and Z signal in the hadron decay mode at SPS and Tevatron



$pp \rightarrow \text{jets}$ at $\sqrt{s} = 630 \text{ GeV}$;
background/signal ~ 20

$p\bar{p} \rightarrow \text{jets}$ at $\sqrt{s} = 1.8 \text{ TeV}$;
background/signal ~ 255 (J. Pumplin,
PRD45, 806 (1992))

Impact of charm contributions to DIS at HERA



CTEQ6.5 employs a more accurate calculation of charm mass effects (general-mass factorization scheme) in DIS structure functions $F_i(x, Q^2)$ at HERA

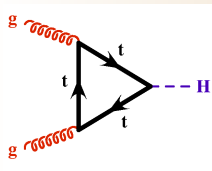
■ W, Z production at the LHC:
 $x \sim 10^{-3} - 10^{-2}$

■ Suppression of charm contribution to $F_2(x, Q^2)$ in CTEQ6.5 results in larger $\bar{u}^{(-)}(x)$, $\bar{d}^{(-)}(x)$ at small $x \Rightarrow$ larger $\sigma_{W,Z}^{LHC}$

$$\delta \bar{q}_{light}(x) / \bar{q}_{light}(x) = 3 - 4\% \quad \Rightarrow \quad \delta \mathcal{L}_{q_i \bar{q}_j} / \mathcal{L}_{q_i \bar{q}_j} = 2(\delta \bar{q}_{light} / \bar{q}_{light}) = 6 - 8\%$$

Heavy Quark Loops

Somewhat surprisingly, gluon fusion via a virtual top-quark loop dominates Higgs production at hadron colliders.



$$\sigma_{\text{LO}}(gg \rightarrow H) = \frac{\pi G_F}{128\sqrt{2}} \left(\frac{\alpha_s(\mu)}{\pi} \right)^2 \tau^2 |1 + (1 - \tau)f(\tau)|^2 \delta\left(1 - \frac{M_H^2}{\hat{s}}\right)$$

$$f(\tau) = \begin{cases} \arcsin^2 \frac{1}{\sqrt{\tau}}, & \tau \geq 1, \\ -\frac{1}{4} \left[\ln \frac{1+\sqrt{1-\tau}}{1-\sqrt{1-\tau}} - i\pi \right]^2, & \tau < 1, \end{cases}$$

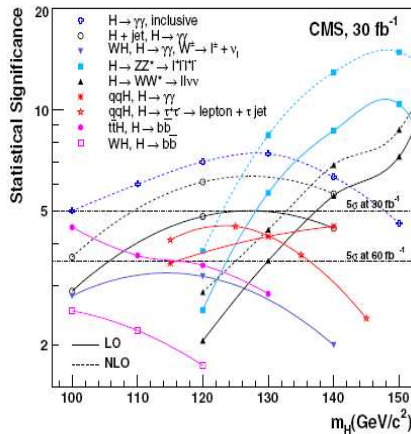
$$\tau = 4M_t^2/M_H^2,$$

Light Higgs boson search at the LHC

■ $gg \rightarrow h \rightarrow \gamma\gamma$ (via a t -quark loop) is the leading search mode for $115 \lesssim M_H \lesssim 140$ GeV

■ A 5σ discovery of SM Higgs boson is possible with $\mathcal{L} = 10 - 30 \text{ fb}^{-1}$

■ $\delta M_H \lesssim 1 \text{ GeV}$, $\delta\sigma(H \rightarrow \gamma\gamma) \sim 20\%$ within the experimental reach at later stages?



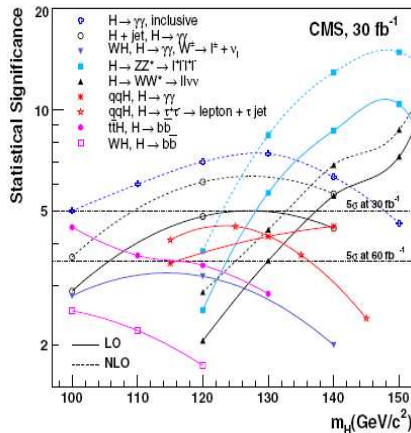
Light Higgs boson search at the LHC

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■ A 5σ discovery of SM Higgs boson is possible with $\mathcal{L} = 10 - 30 \text{ fb}^{-1}$

■ $\delta M_H \lesssim 1 \text{ GeV}$, $\delta\sigma(H \rightarrow \gamma\gamma) \sim 20\%$ within the experimental reach at later stages?

■ Statistical significance depends on the (new) physics model, QCD contributions, etc.



A challenging measurement!