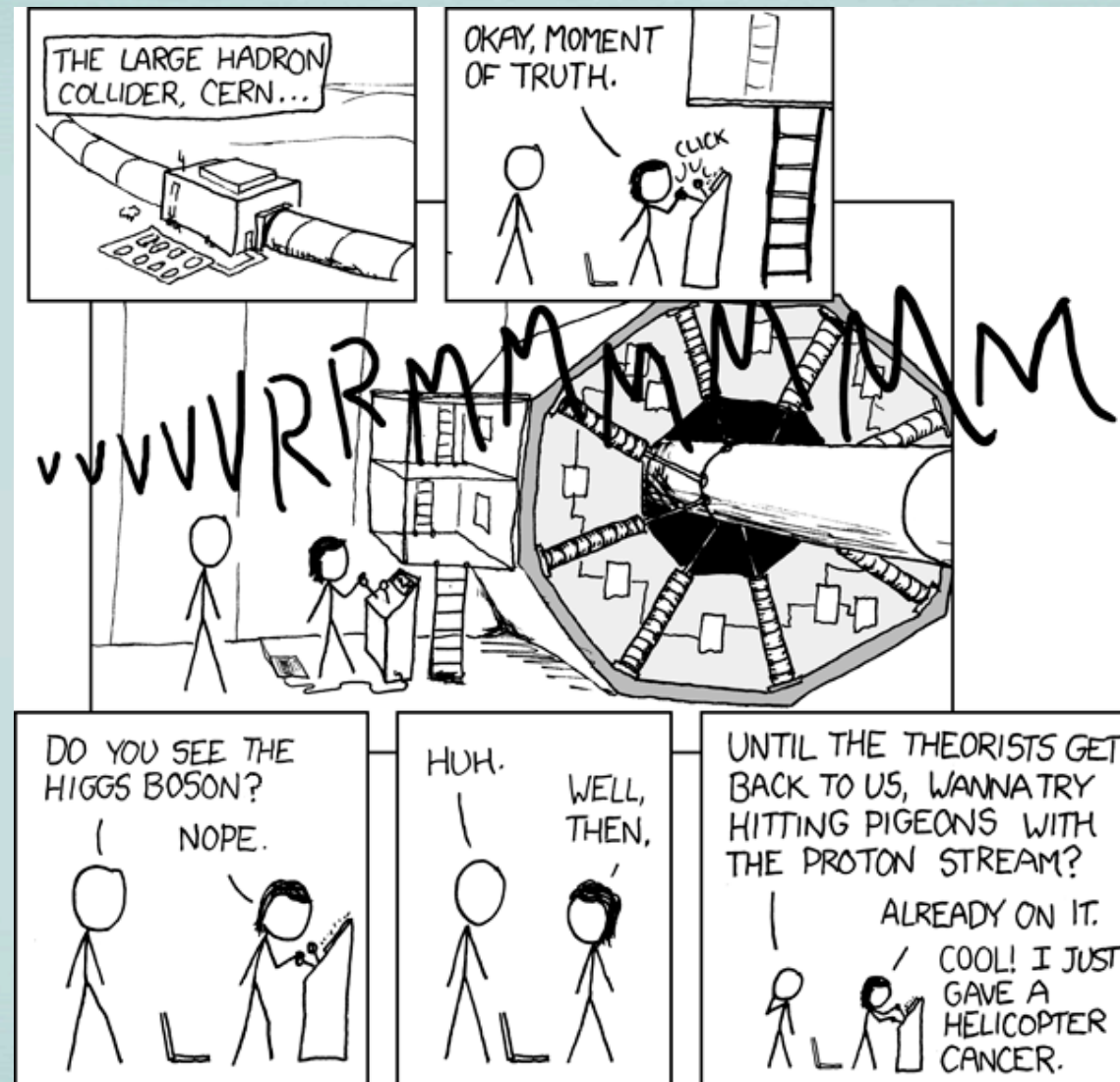


# SEARCHING FOR THE HIGGS BOSON



xkcd.com

2009 CTEQ Summer School  
June 24-July 2, 2009

Frank Petriello  
University of Wisconsin, Madison



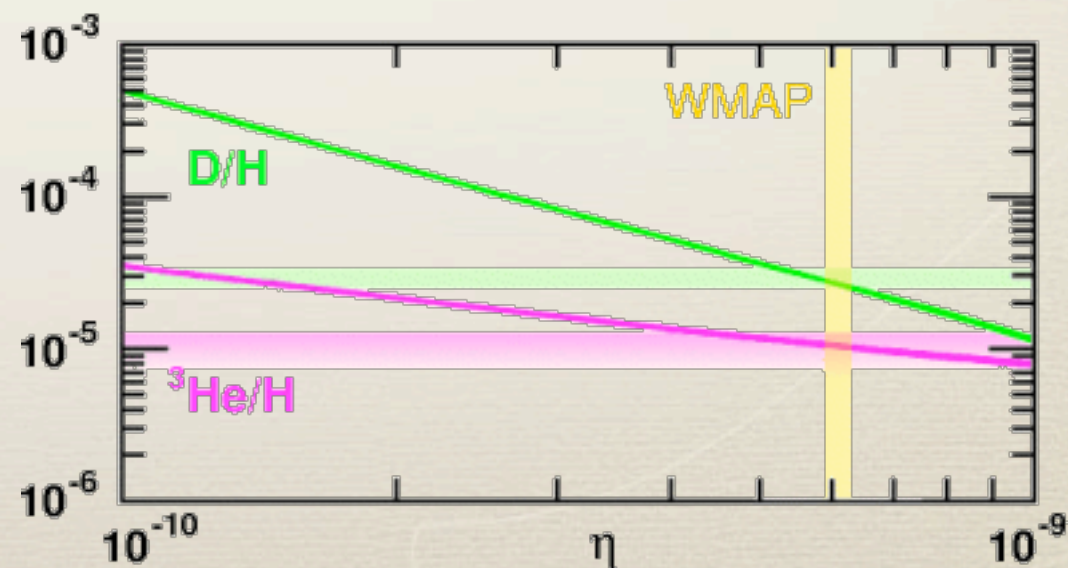
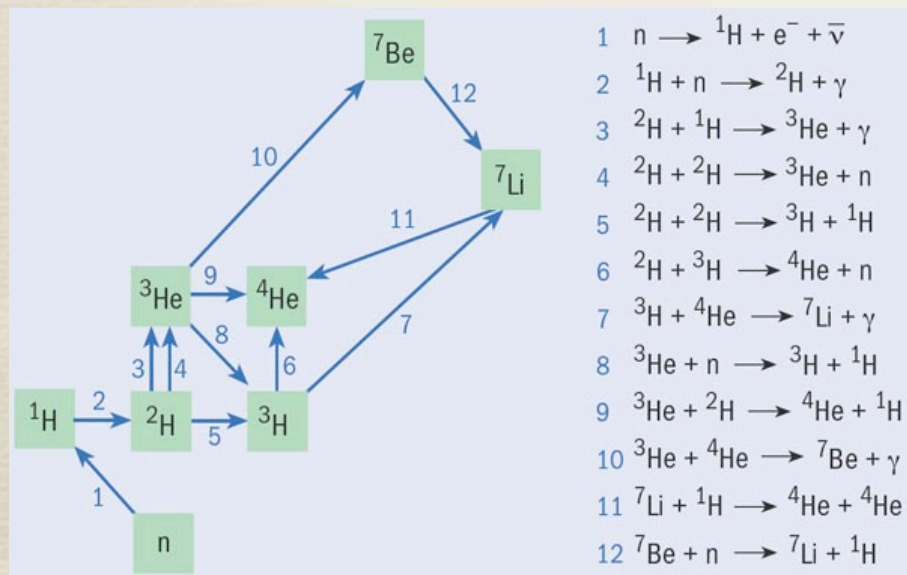
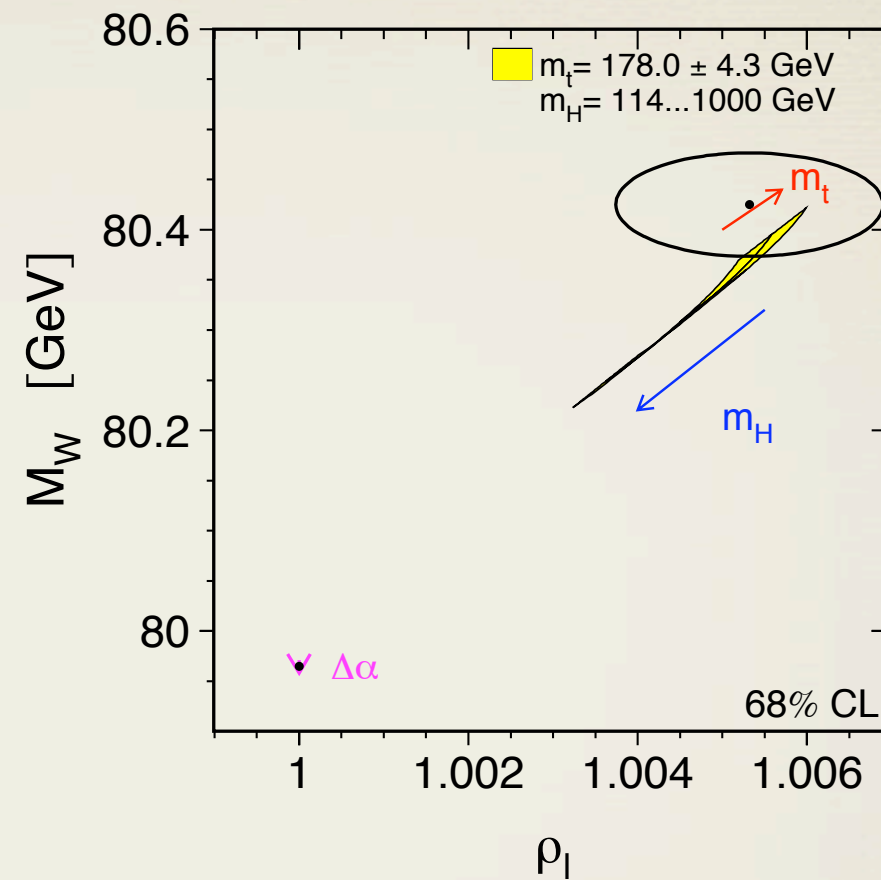
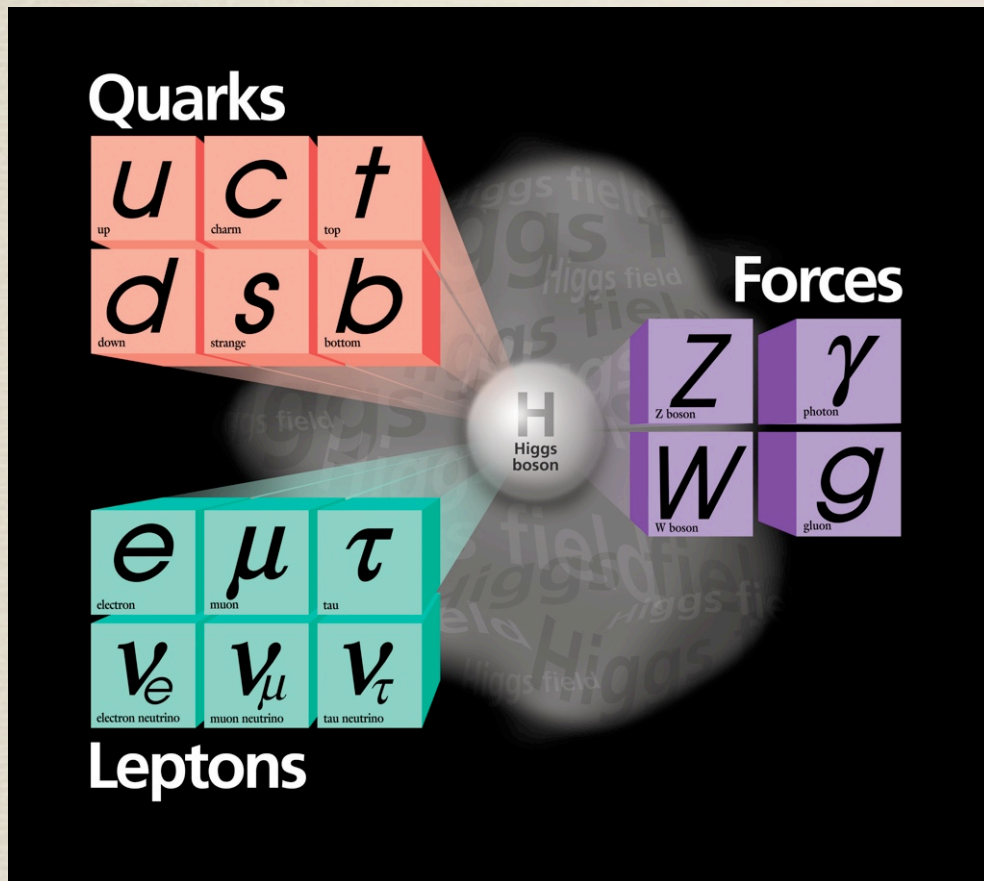
# Outline

- \* Quick review of the SM and the Higgs mechanism
- \* Constraining the Higgs: theoretical constraints and electroweak precision
- \* A phenomenological profile: decays of the Higgs boson
- \* Production mechanisms at  $e^+e^-$  and hadron colliders
- \* A case study in QCD: gluon-fusion production
- \* Searches at the Tevatron and the LHC

Mostly SM, but will try to mention possible deviations



# Success of the Standard Model





# Building a gauge theory

- \* Guiding principle in construction of SM is *gauge symmetry*
- \* Pick a gauge group
- \* Assign matter fields (fermions, scalars) to a *representation* of the gauge group, e.g., the *fundamental* N-component vector for SU(N)
- \* To make the matter Lagrangian gauge invariant, replace  $\partial_\mu \rightarrow D_\mu$

$$\mathcal{L} = -\frac{1}{2} \text{Tr} [F_{\mu\nu} F^{\mu\nu}] + \mathcal{L}_{matter} (\Psi, D_\mu \Psi)$$

gives Feynman rules  
for gauge self-interactions

governs gauge-matter  
interactions



# The Standard Model

- \* Gauge group:  $SU(3)_C \times SU(2)_L \times U(1)_Y$  (8 gluons; eventually photon,  $W^\pm, Z$ )
- \* Three generations of fermionic matter

	<u><math>SU(3)_C</math></u>	<u><math>SU(2)_L</math></u>	<u><math>U(1)_Y</math></u>
$Q_L = \begin{pmatrix} u_L \\ d_L \end{pmatrix} :$	3	2	1/6
$u_R :$	3	1	2/3
$d_R :$	3	1	-1/3
$L_L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} :$	1	2	-1/2
$e_R :$	1	1	-1

- \* Electric charge:  $Q = T_3 + Y$



# Problems with mass

- \* The Lagrangian of the SM:

$$\mathcal{L}_{gauge+ferm} = -\frac{1}{4} \overbrace{B_{\mu\nu} B^{\mu\nu}}^{U(1)_Y} - \frac{1}{4} \overbrace{W_{\mu\nu}^a W_a^{\mu\nu}}^{SU(2)_L} - \frac{1}{4} \overbrace{G_{\mu\nu}^a G_a^{\mu\nu}}^{SU(3)_C} + \underbrace{\sum_f i \bar{f} \not{D} f}_{f=Q_L, u_R, d_R, L_L, e_R}$$

- \* We know the  $W^\pm$ ,  $Z$  bosons have mass, but this is not allowed by gauge symmetry

$$\mathcal{L}_{mass}^{SU(2)} = \frac{1}{2} m^2 W_\mu^a W_a^\mu \Rightarrow \Delta \mathcal{L}_{mass}^{SU(2)} \neq 0 \text{ under G.T.}$$

- \* Similarly, fermion mass terms are not allowed by  $SU(2)_L$  or  $U(1)_Y$

$$\mathcal{L}_{mass}^{ferm} = -m \underbrace{[\bar{f}_R f_L + \bar{f}_L f_R]}$$

transforms as  $SU(2)_L$  doublet,  $\sum Y \neq 0$



# Spontaneous symmetry breaking

- \* The solution: Lagrangian is symmetric, ground state isn't  $\Rightarrow$  *spontaneous symmetry breaking*
- \* Complex scalar transforming as  $(1,2,1/2)$  under  $SU(3)_C \times SU(2)_L \times U(1)_Y$

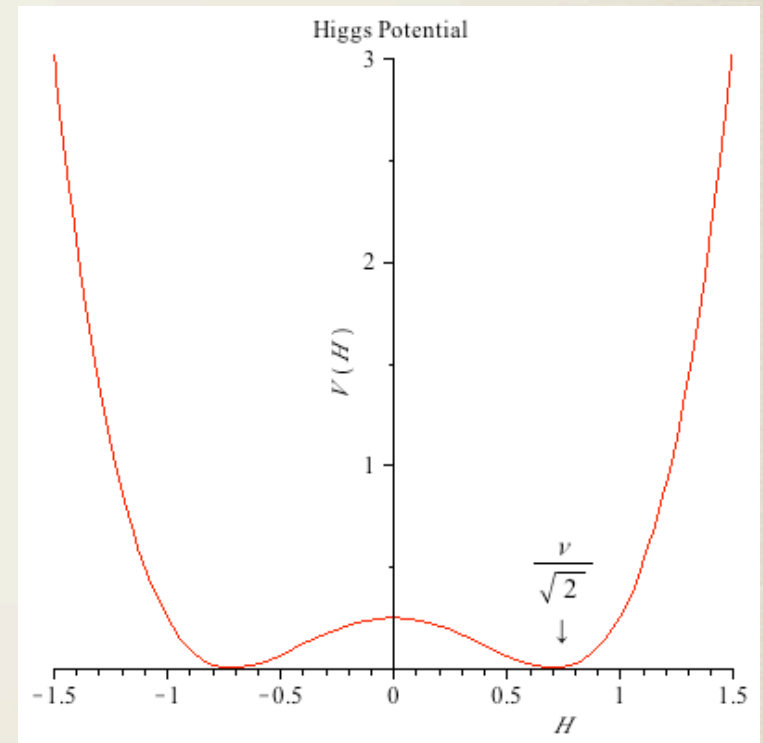
$$\mathcal{L}_{Higgs} = (D_\mu H)^\dagger D^\mu H - \lambda \overbrace{\left( H^\dagger H - \frac{v^2}{2} \right)^2}^{V(H)}$$

$$H = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix}$$

$$D^\mu = \partial^\mu - igW_a^\mu \frac{\sigma^a}{2} - ig' B^\mu \frac{1}{2}$$

Vacuum expectation value:  $\langle H \rangle = \begin{pmatrix} 0 \\ \frac{v}{\sqrt{2}} \end{pmatrix}$

Expand around vev:  $H = \begin{pmatrix} \phi^+ \\ \frac{v+h+i\chi}{\sqrt{2}} \end{pmatrix}$



$(\phi^+, \chi)$  can be removed by G.T., set to zero



# The Higgs mechanism

\* Work out the kinetic part of Higgs Lagrangian

$$D_\mu H = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \partial_\mu h \end{pmatrix} - \frac{i}{2} \left[ \frac{v+h}{\sqrt{2}} \right] \begin{pmatrix} \sqrt{2}gW_\mu^+ \\ \sqrt{g^2 + g'^2}Z_\mu \end{pmatrix}$$

$$(D^\mu H)^\dagger D_\mu H = \frac{1}{2} \partial_\mu h \partial^\mu h + \left(1 + \frac{h}{v}\right)^2 \left( \underbrace{\frac{g^2 v^2}{4}}_{M_W^2} W^{\mu+} W_\mu^- + \frac{1}{2} \underbrace{\frac{(g^2 + g'^2)v^2}{4}}_{M_Z^2} Z_\mu Z^\mu \right)$$

$$Z_\mu = c_W W_\mu^3 - s_W B_\mu, \quad A_\mu = s_W W_\mu^3 + c_W B_\mu, \quad W_\mu^\pm = \frac{W_\mu^1 \mp iW_\mu^2}{\sqrt{2}}$$

$$c_W = \frac{g}{\sqrt{g^2 + g'^2}}, \quad s_W = \frac{g'}{\sqrt{g^2 + g'^2}}$$

\*  $W^\pm, Z$  acquire mass by “eating”  $\varphi^\pm, \chi$

$$\text{Prediction: } \rho = \frac{M_W^2}{M_Z^2 c_W^2} = 1$$

(tree-level; more later)



# Fermion masses

- \* Yukawa interactions with Higgs doublets give fermions mass

$$\begin{aligned}\mathcal{L}_{Yuk} &= -\lambda_d \bar{Q}_L H d_R - \lambda_u \bar{Q}_L (i\sigma_2 H^*) u_R - \lambda_e \bar{L}_L H e_R + \text{h.c.} \\ &\Rightarrow - \left(1 + \frac{h}{v}\right) \sum_{f=u,d,e} m_f \bar{f} f \quad \text{with} \quad m_f = \frac{\lambda_f v}{\sqrt{2}}\end{aligned}$$

(matrix in generation space, implicitly diagonalized at price of  $V_{CKM}$  in charged currents)

- \* Sum of all pieces so far give the SM Lagrangian:

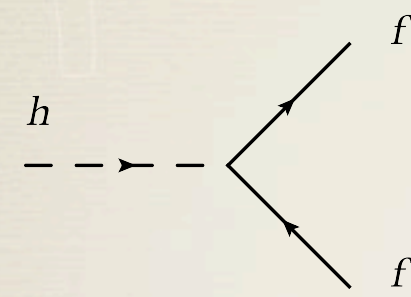
$$\mathcal{L}_{SM} = \mathcal{L}_{gauge+ferm} + \mathcal{L}_{Higgs} + \mathcal{L}_{Yuk}$$

- \* The single Higgs doublet is just the simplest way to break  $SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$ ; EWSB could be more intricate. But this is the benchmark to compare other theories against.

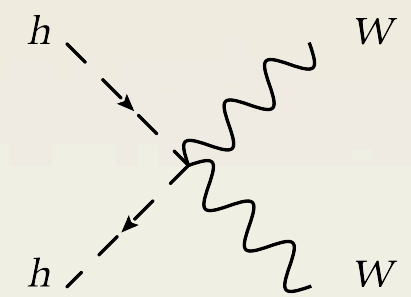


# Feynman rules

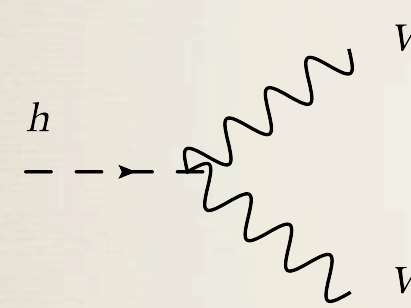
\* Work out the experimental predictions with Feynman rules:



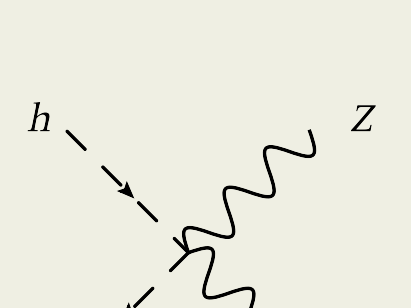
$$= -i \frac{m_f}{v}$$



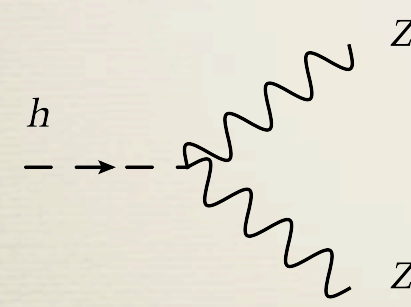
$$= 2i \frac{M_W^2}{v^2} g_{\mu\nu}$$



$$= 2i \frac{M_W^2}{v} g_{\mu\nu}$$



$$= 2i \frac{M_W^2}{v^2} g_{\mu\nu}$$



$$= 2i \frac{M_Z^2}{v} g_{\mu\nu}$$

From muon decay,  
 $v^2 = 1/(G_F \sqrt{2}) \Rightarrow v \approx 246 \text{ GeV}$

\* Only scalars with vevs have linear HVV couplings

Test the consequences of the Higgs mechanism



# Unitarity of S-matrix

- \* Conservation of probability in QFT:

$$S^\dagger S = 1 \Rightarrow \sigma = \frac{1}{s} \operatorname{Im} \underbrace{\{\mathcal{M}(\theta = 0)\}}_{\text{forward scattering}}$$

- \* Decompose into Legendre polynomials

$$\mathcal{M} = 16\pi \sum_{l=0}^{\infty} (2l+1) P_l(c_\theta) a_l$$

$$a_l = \frac{1}{32\pi} \int_{-1}^1 dc_\theta P_l(c_\theta) \mathcal{M}$$

$$\Rightarrow \sigma = \frac{16}{s} \sum_{l=0}^{\infty} (2l+1) |a_l|^2$$

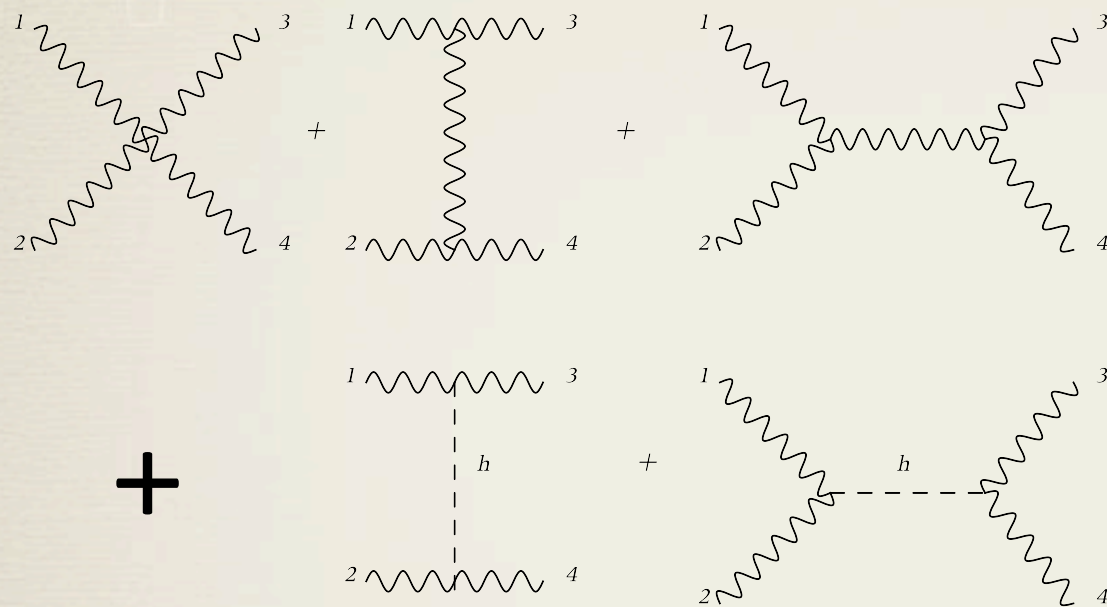
$$\Rightarrow |a_L|^2 = \operatorname{Im}(a_l)$$

$$\Rightarrow \operatorname{Re}(a_l) \leq 1/2$$



# WW scattering

\* Longitudinal modes:  $\epsilon_L = (p/M, 0, 0, E/M)$  (boost from  $(0,0,0,1)$ )



$$a_0(W_L W_L \rightarrow W_L W_L) \rightarrow -\frac{s}{32\pi v^2}$$

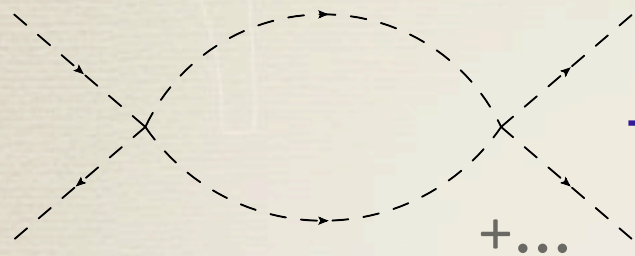
$$a_0(W_L W_L \rightarrow W_L W_L) \rightarrow -\frac{M_H^2}{8\pi v^2}$$

\* Probability not conserved without Higgs; with,  $M_H < 900$  GeV (perturbative argument)



# Theoretical constraints

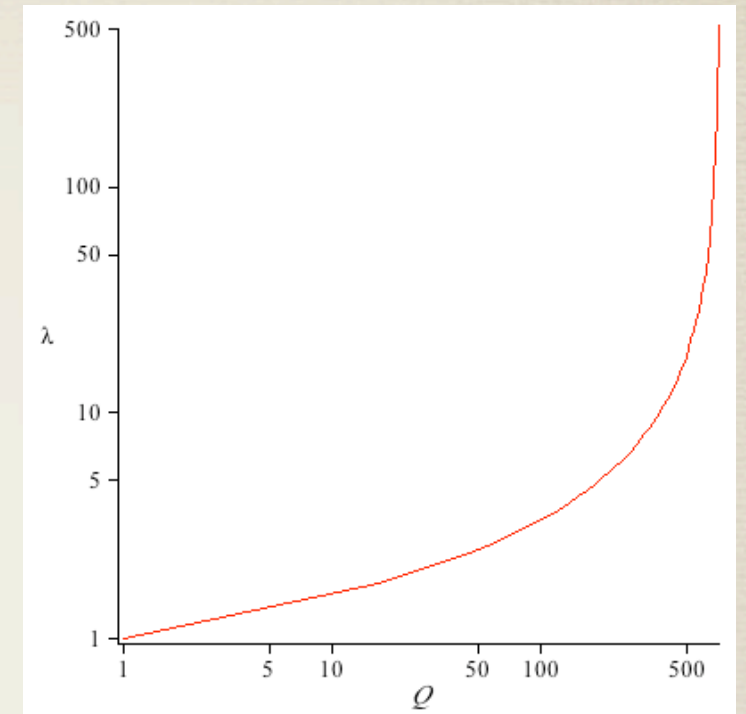
\* Landau pole of  $\lambda h^4$  coupling



$$\lambda(Q) = \frac{M_H^2}{2v^2} \frac{1}{1 - \frac{3}{4\pi^2} \frac{M_H^2}{v^2} \ln \frac{Q}{v}}$$

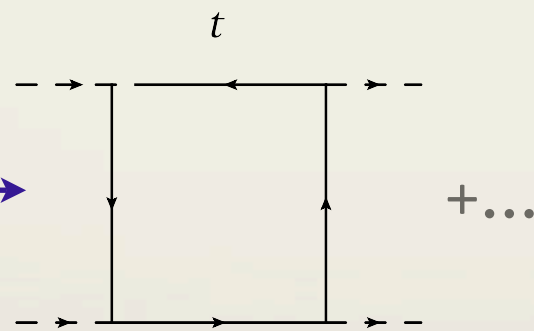
(large  $\lambda$  limit)

Breaks down at some  $Q$   
For validity up to  $Q=\Lambda$  ( $\lambda < \infty$ ),  
upper bound on  $M_H$



\* Shape of Higgs potential:  $\lambda > 0 \Rightarrow$  lower bound on  $M_H$

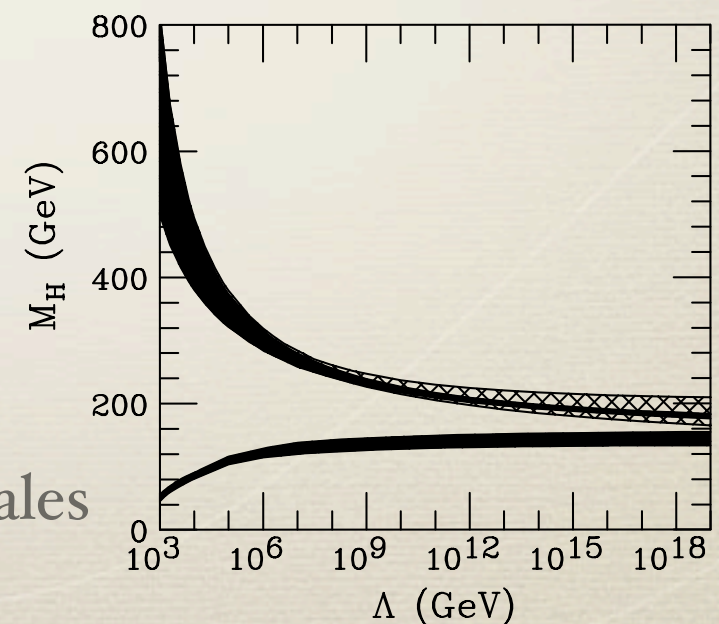
top quark drives  
coupling negative



$$\lambda(Q) = \lambda_0 - \frac{\frac{3y_t^4}{8\pi^2} \ln \frac{Q}{Q_0}}{1 - \frac{9y_t^2}{16\pi^2} \ln \frac{Q}{Q_0}}$$

(small  $\lambda$  limit)

Validity of SM to high scales  
restricts allowed  $M_H$





# Electroweak precision

- \* Can experimentally probe properties of the Higgs directly (try to produce at a collider) or indirectly (through quantum effects)
- \* LEP+SLC: millions of  $e^+e^- \rightarrow Z \rightarrow f\bar{f}$ , high-precision measurements of SM electroweak parameters  $\Rightarrow$  effect of Higgs?
- \* Study one-loop predictions of SM
- \* Basic idea in renormalizable theory: fix most precisely known quantities, calculation others in terms of them

$$G_F = 1.166367(5) \times 10^{-5} \text{ GeV}^{-2} \quad (\text{muon decay})$$

$$\alpha^{-1} = 137.035999679(94) \quad (\text{low-energy experiments})$$

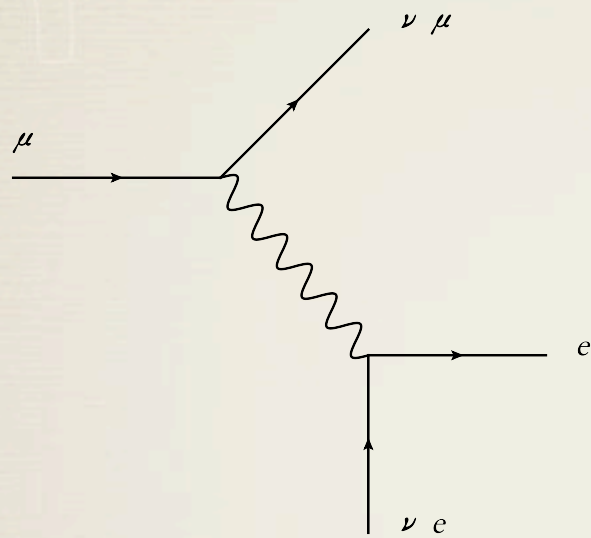
$$M_Z = 91.1875(21) \quad (\text{LEP})$$

- \* Example: we'll outline prediction for  $M_W$



# Muon decay

\* Muon-decay at tree-level:



$$\frac{G_F}{\sqrt{2}} = \frac{e^2}{8M_W^2 s_W^2} \quad (m_{e,\mu} = 0)$$

$$s_W^2 = 1 - \frac{M_W^2}{M_Z^2} \quad (\text{on-shell scheme})$$

$$\Rightarrow \frac{G_F}{\sqrt{2}} = \frac{\pi\alpha}{2M_W^2 (1 - M_W^2/M_Z^2)}$$

$$\Rightarrow M_W^2 = \frac{M_Z^2}{2} \left\{ 1 + \left[ 1 - \frac{2\sqrt{2}\pi\alpha}{G_F M_Z^2} \right]^{1/2} \right\}$$

$$\approx 80.94 \text{ GeV} \quad \Rightarrow \text{experiment gets } 80.4 \text{ GeV!}$$

\* Keep only leading corrections ( $m_t$ ,  $M_H$ , running of  $\alpha$ ; others defined as 'small')

$$\frac{G_F}{\sqrt{2}} = \frac{e^2}{8M_W^2 s_W^2} (1 + \Delta r)$$

$$\Rightarrow M_W^2 = \frac{M_Z^2}{2} \left\{ 1 + \left[ 1 - \frac{2\sqrt{2}\pi\alpha (1 + \Delta r)}{G_F M_Z^2} \right]^{1/2} \right\}$$

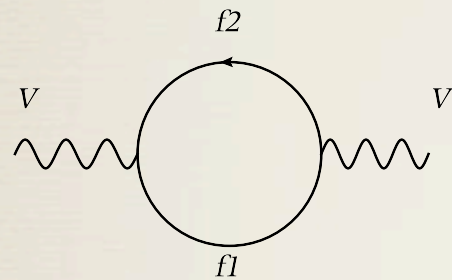


# $\Delta\rho$ and non-decoupling

$\Delta r$  receives important contribution from gauge-boson self-energies

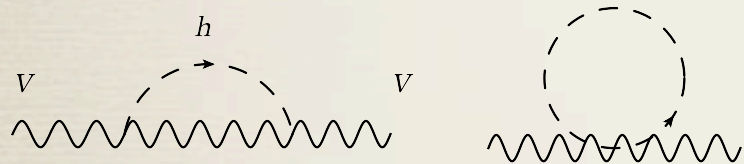
$$\left[ \begin{aligned} \Delta r &= \Delta\alpha - \frac{c_W^2}{s_W^2} \Delta\rho \\ \Delta\rho &= \frac{\Pi_{WW}(0)}{M_W^2} - \frac{\Pi_{ZZ}(0)}{M_Z^2} \end{aligned} \right]$$

quadratic in  $m_t$



$$\Delta\rho_{ferm} = \frac{3G_F m_t^2}{8\pi^2 \sqrt{2}} + \text{subleading terms}$$

Exercise: Derive these



$$\Delta\rho_{Higgs} = -\frac{3G_F M_Z^2 s_W^2}{4\pi^2 \sqrt{2}} \underbrace{\ln \frac{M_H}{M_Z}}_{\text{logarithmic in } M_H} + \text{subleading terms}$$

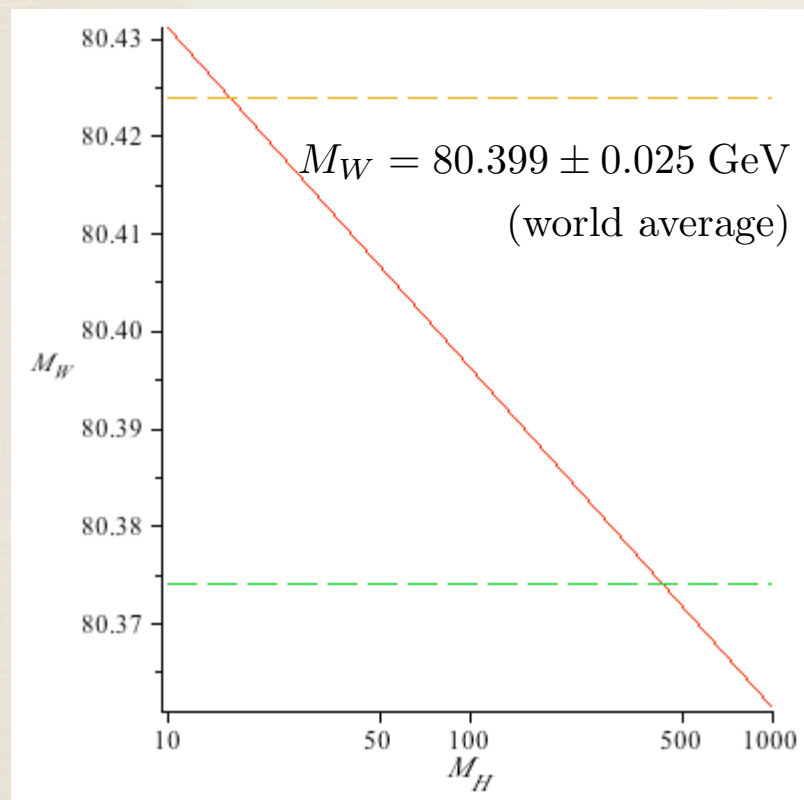
Decoupling theorem holds only if dimensionful parameters made large

$$\begin{aligned} m_t = \frac{\lambda_t v}{\sqrt{2}} &\Rightarrow m_t \rightarrow \infty, \quad v \text{ fixed} \Rightarrow \lambda_t \rightarrow \infty \\ M_H^2 = 2\lambda v^2 &\Rightarrow M_H \rightarrow \infty, \quad v \text{ fixed} \Rightarrow \lambda \rightarrow \infty \end{aligned}$$

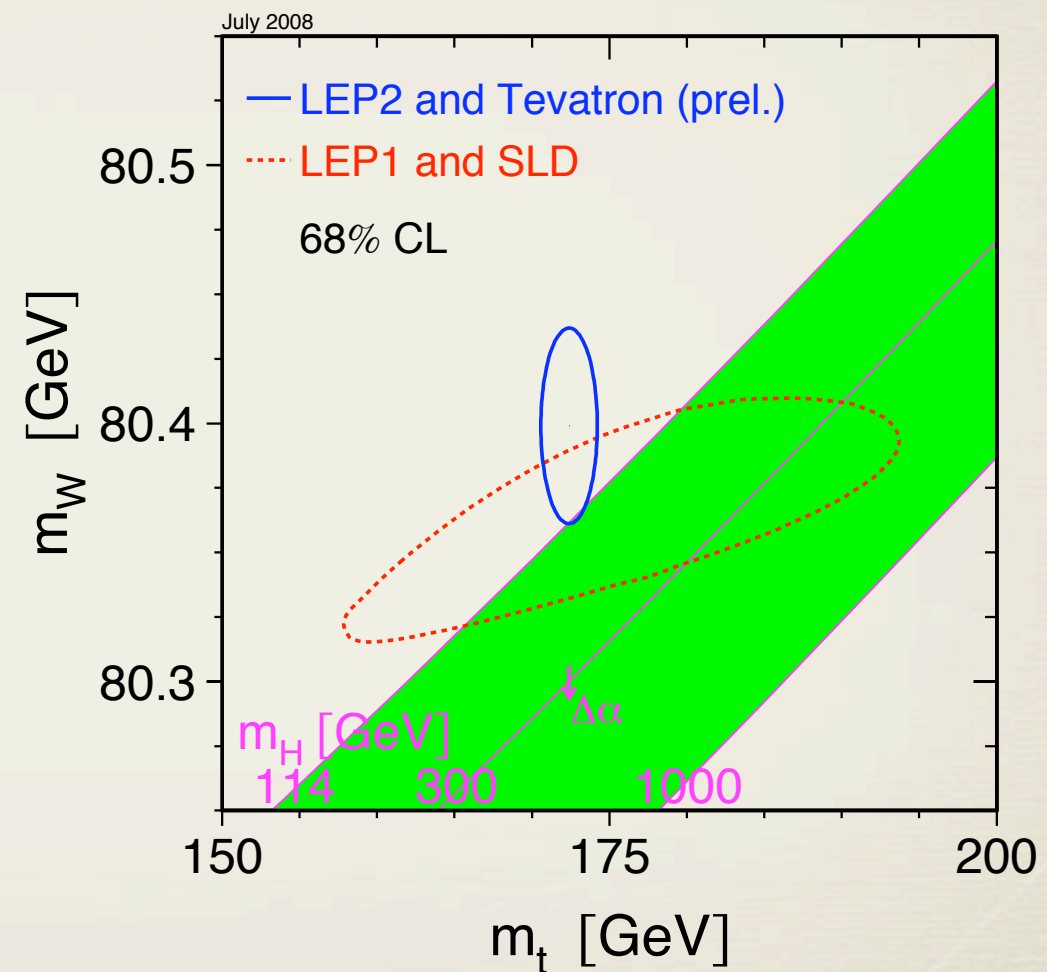


# Bounding the Higgs mass

- \* Logarithmic dependence on  $M_H$  allows  $M_W$  to bound it (but very sensitive to the top-quark mass)



(Refinements needed for real comparison to data; important  $\ln(m_t)$  and other terms; see PDG and refs within)



$$M_W^{tree} = 80.94 \text{ GeV} \Rightarrow M_W^{1-loop} = 80.39 \text{ GeV} (M_H = 120 \text{ GeV})$$

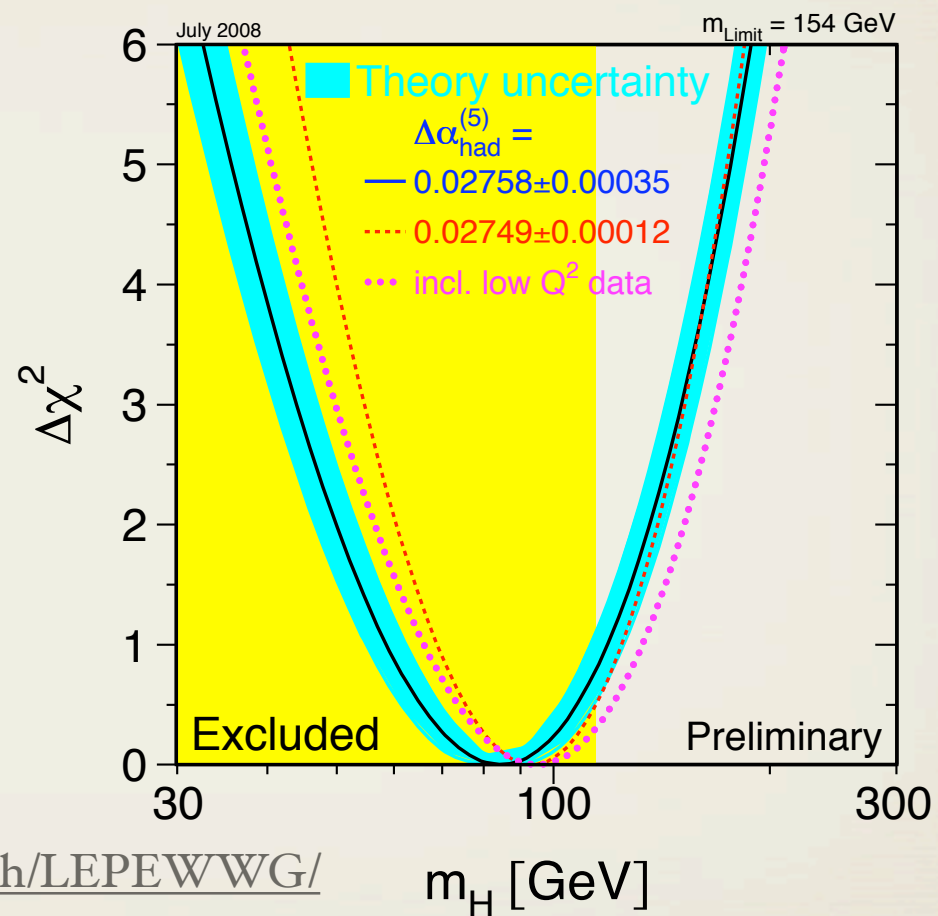


# Global EW fit

\* Do the same for large set of LEP-SLC measurements

	Measurement	Fit	$10^{\text{meas}} - \text{fit} / 10^{\text{meas}}$
$\Delta\alpha_{\text{had}}^{(5)}(m_Z)$	$0.02758 \pm 0.00035$	0.02767	
$m_Z$ [GeV]	$91.1875 \pm 0.0021$	91.1875	
$\Gamma_Z$ [GeV]	$2.4952 \pm 0.0023$	2.4958	
$\sigma_{\text{had}}^0$ [nb]	$41.540 \pm 0.037$	41.478	
$R_l$	$20.767 \pm 0.025$	20.743	
$A_{\text{fb}}^{0,l}$	$0.01714 \pm 0.00095$	0.01644	
$A_l(P_\tau)$	$0.1465 \pm 0.0032$	0.1481	
$R_b$	$0.21629 \pm 0.00066$	0.21582	
$R_c$	$0.1721 \pm 0.0030$	0.1722	
$A_{\text{fb}}^{0,b}$	$0.0992 \pm 0.0016$	0.1038	
$A_{\text{fb}}^{0,c}$	$0.0707 \pm 0.0035$	0.0742	
$A_b$	$0.923 \pm 0.020$	0.935	
$A_c$	$0.670 \pm 0.027$	0.668	
$A_l(\text{SLD})$	$0.1513 \pm 0.0021$	0.1481	
$\sin^2\theta_{\text{eff}}^{\text{lept}}(Q_{\text{fb}})$	$0.2324 \pm 0.0012$	0.2314	
$m_W$ [GeV]	$80.399 \pm 0.025$	80.376	
$\Gamma_W$ [GeV]	$2.098 \pm 0.048$	2.092	
$m_t$ [GeV]	$172.4 \pm 1.2$	172.5	

July 2008



<http://lepewwg.web.cern.ch/LEPEWWG/>

SM Higgs mass:  $M_H < \sim 160$  GeV from EW precision measurements



# S, T, and hiding a heavy Higgs

- \* How robust are these bounds? Consider corrections that are *oblique*: affect only gauge boson propagators

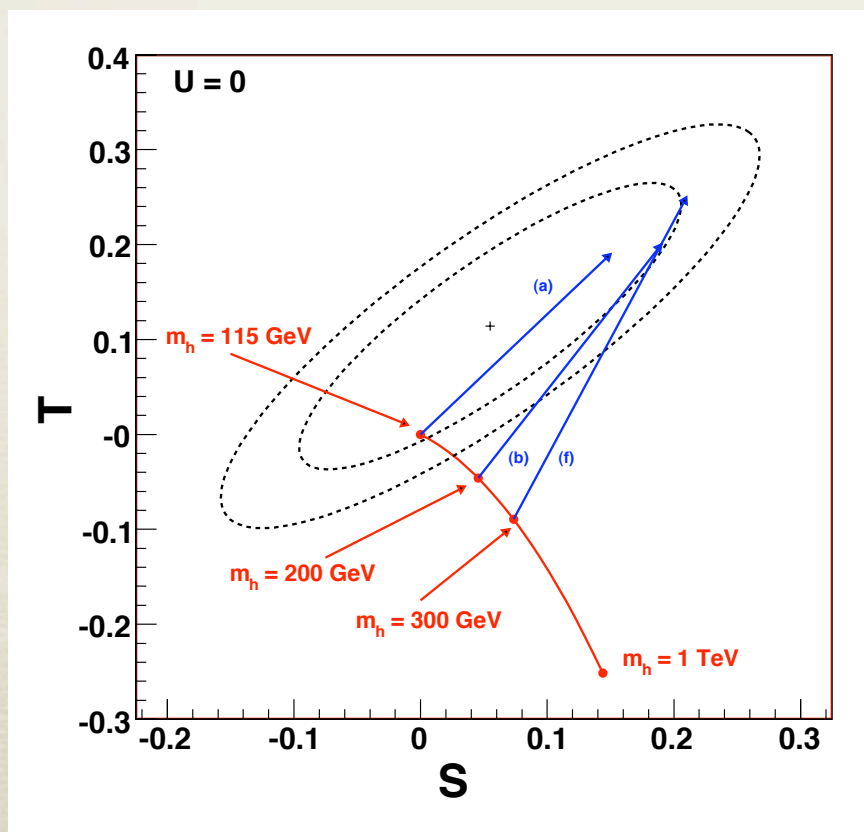
$$\alpha T = \frac{\Pi_{WW}(0)}{M_W^2} - \frac{\Pi_{ZZ}(0)}{M_Z^2} = \Delta\rho$$

$$\frac{\alpha}{4s_W^2 c_W^2} S = \frac{\Pi_{ZZ}(M_Z^2)}{M_Z^2} - \frac{\Pi_{ZZ}(0)}{M_Z^2}$$

(Not a complete basis, but these are often the most important ones)

- \* Calculate for reference  $M_H$ , propagate through all EW parameters

Example: 4th generation  
(Kribs et al.,  
0706.3718)



$$\Delta\rho_{new} = \frac{3G_F \overbrace{\Delta m_{ferm}^2}^{\text{doublet mass splitting}}}{8\pi^2 \sqrt{2}} - \frac{3G_F M_Z^2 s_W^2}{4\pi^2 \sqrt{2}} \ln \frac{M_H}{M_H^{ref}}$$

⇒ increase  $M_H$ , cancel with  $\Delta m$

**Need direct searches!**



# **Decays of the Higgs boson**



# Higgs decays

\* Since  $g_{Hxx} \sim m_x$ , Higgs tends to decay to heaviest kinematically accessible states (with many important caveats...)

\* Tree-level decays to various massive final states:

$$\Gamma_{qq} = N_c \frac{G_F}{4\sqrt{2}\pi} M_H m_f^2 \left(1 - \frac{4m_f^2}{M_H^2}\right)^{3/2}, \quad \Gamma_{ll} = \frac{G_f}{4\sqrt{2}\pi} M_H m_f^3 \left(1 - \frac{4m_f^2}{M_H^2}\right)^{3/2}$$
$$\Gamma_{VV} = \frac{G_F}{8\sqrt{2}\pi n_V} M_H^3 (1 - 4x)^{1/2} (1 - 4x + 12x^3) \quad \text{with } x = \frac{M_V^2}{M_H^2}, n_W = 1, n_Z = 2$$

\* Threshold structure depends on spin, CP ( $3/2 \rightarrow 1/2$  for CP-odd A)

\* Note  $\Gamma_{ff} \sim M_H$ , while  $\Gamma_{VV} \sim (M_H)^3 \Rightarrow$  when W, Z channels open, Higgs becomes very broad

\* For light Higgs ( $M_H \leq 130$  GeV), expect bb,  $\tau\tau$ , cc to be important



# Equivalence theorem

- \* Growth of VV width comes from longitudinal gauge modes

$$\mathcal{A}(h \rightarrow W_L^+ W_L^-) = 2 \frac{M_W^2}{v} \epsilon_L^+ \cdot \epsilon_L^-, \quad \epsilon_L^\pm = \frac{E}{M_W} (\pm \beta_W, \vec{0}, 1)$$

$$\mathcal{A}(h \rightarrow W_L^+ W_L^-) \rightarrow -\frac{M_H^2}{v} + \mathcal{O}\left(\frac{M_V^2}{M_H^2}\right)$$

$$\Gamma_{WW} = \frac{1}{16\pi M_H} |\mathcal{A}|^2 \rightarrow \frac{G_F M_H^3}{8\pi\sqrt{2}} + \mathcal{O}\left(\frac{M_V^2}{M_H^2}\right)$$

- \* In the high energy limit, longitudinal mode interactions equivalent to those of eaten scalar  $\Rightarrow$  *Goldstone boson equivalence theorem*



The diagram shows a Higgs boson  $h$  (represented by a dashed line with an arrow) decaying into two Goldstone bosons,  $\phi^+$  and  $\phi^-$  (represented by dashed lines with arrows). The vertex is a simple point where the lines meet.

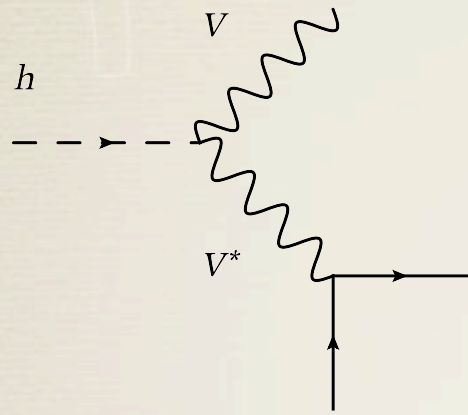
$$= -i \frac{M_H^2}{v} \quad \mathcal{A}(h \rightarrow \phi^+ \phi^-) = -\frac{M_H^2}{v}$$

Exercise: Work out from  $L_{\text{Higgs}}$



# Three-body decays

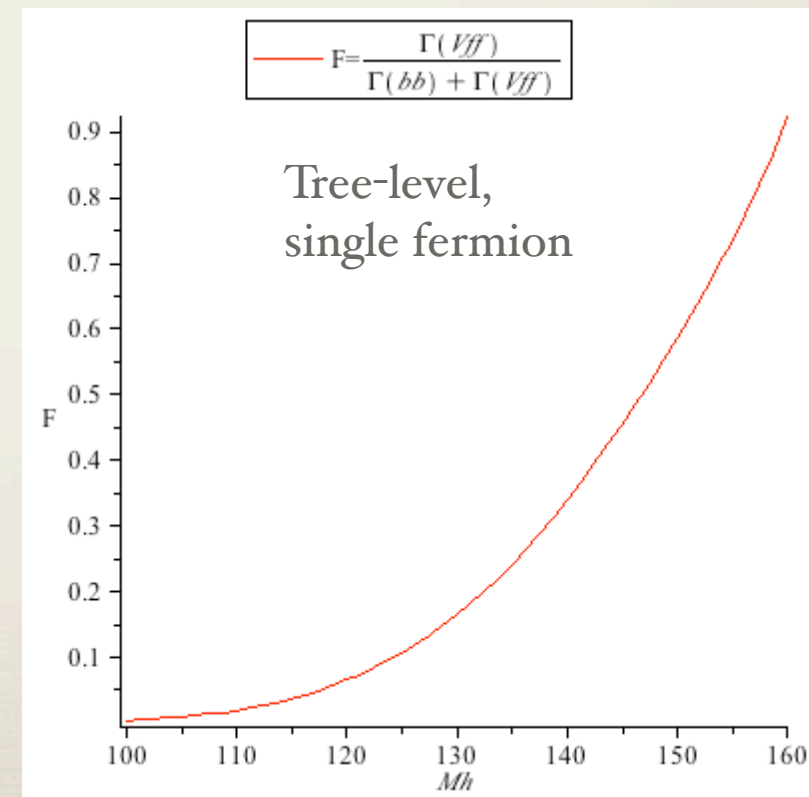
- \* Since  $M_{W,Z} \gg m_{b,c,\tau}$ ,  $H \rightarrow VV^* \rightarrow Vff$  important for  $M_H < 2M_{W,Z}$



$$\Gamma_{Wf\bar{f}} = \frac{3G_F^2 M_W^4}{16\pi^3} M_H \left\{ \frac{3(1 - 8x + 20x^2)}{\sqrt{4x - 1}} \arccos\left(\frac{3x - 1}{2x^{3/2}}\right) - \frac{1 - x}{2x} (2 - 13x + 47x^2) - \frac{3}{2} (1 - 6x + 4x^2) \ln x \right\}$$

$$x = M_W^2 / M_H^2$$

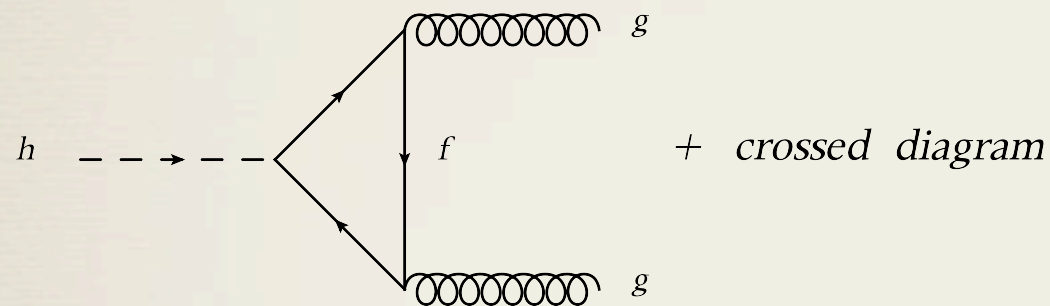
- \* Important mode even down at  $M_H \approx 130$  GeV since  $f=e,\mu$





# Loop-induced $H \rightarrow gg$

- \* Can we leverage the large  $H_{tt}$ ,  $H_{VV}$  couplings at low  $M_H$ ?
- \* Two important cases:  $h \rightarrow gg$  (production more important),  $h \rightarrow \gamma\gamma$



$$\Gamma_{gg} = \frac{G_F \alpha_s^2 M_H^3}{36\pi^3 \sqrt{2}} \left| \frac{3}{4} \sum_Q \mathcal{F}_{1/2}(\tau_Q) \right|^2 \quad \text{with } \tau_Q = \frac{M_H^2}{4m_Q^2}$$

$$\mathcal{F}_{1/2}(\tau) = \frac{2}{\tau^2} [\tau + (\tau - 1)f(\tau)]$$

$$f(\tau) = \begin{cases} \arcsin^2 \sqrt{\tau} & \tau \leq 1 \\ -\frac{1}{4} \left[ \ln \frac{1 + \sqrt{1 - \tau^{-1}}}{1 - \sqrt{1 - \tau^{-1}}} - i\pi \right]^2 & \tau > 1 \end{cases}$$

$$\tau \rightarrow 0 \Rightarrow \mathcal{F}_{1/2} \rightarrow \frac{4}{3}$$

$$\tau \rightarrow \infty \Rightarrow \mathcal{F}_{1/2} \rightarrow -\frac{2m_Q^2}{M_H^2} \ln \frac{M_H^2}{m_Q^2}$$

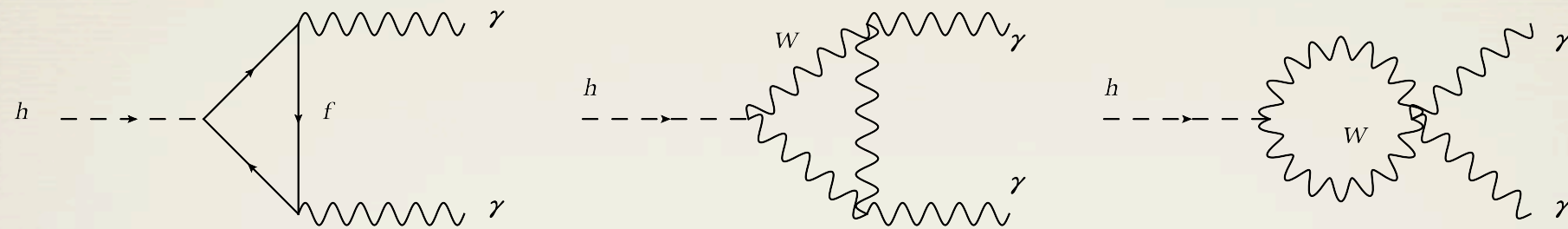
- Independent of  $m_f$  when  $m_f \rightarrow \infty \Rightarrow$  true for *any* heavy fermion that gets its mass from Higgs

Exercise: Derive  $m_t \rightarrow \infty$  result from direct integration



# Loop-induced $H \rightarrow \gamma\gamma$

\* Crucial for low-mass Higgs search at LHC



$$\Gamma_{\gamma\gamma} = \frac{G_F \alpha^2 M_H^3}{128 \pi^3 \sqrt{2}} \left| \sum_f N_c Q_f^2 \mathcal{F}_{1/2}(\tau_f) + \mathcal{F}_1(\tau_W) \right|^2$$

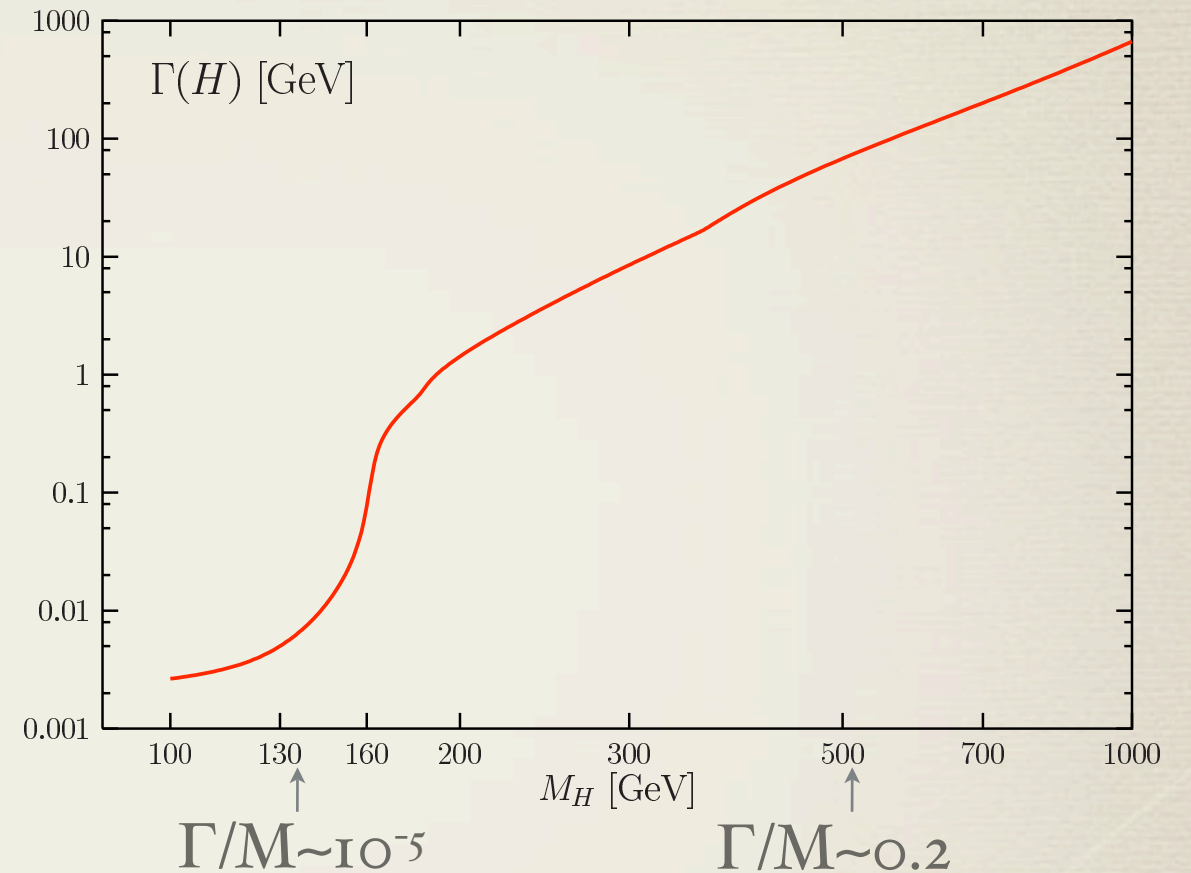
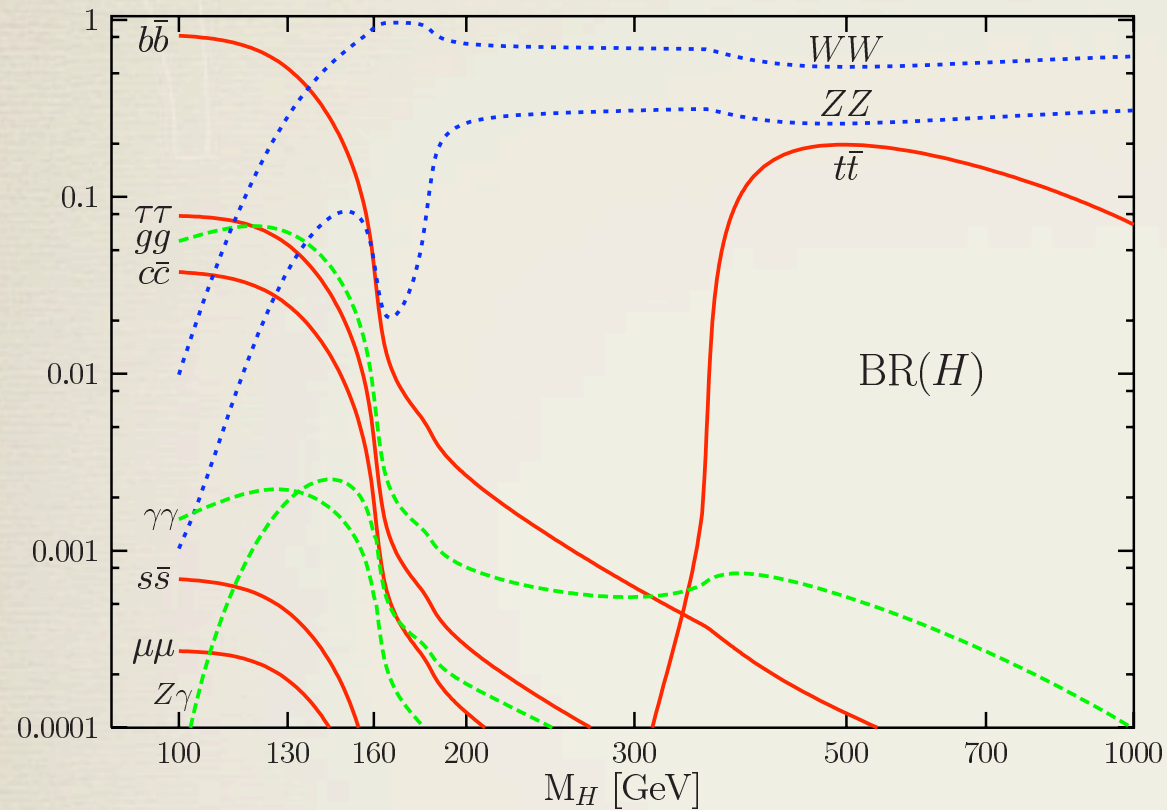
$$\mathcal{F}_1(\tau) = -\frac{1}{\tau^2} [2\tau^2 + 3\tau + 3(2\tau - 1)f(\tau)]$$

$$\tau \rightarrow 0 \Rightarrow \mathcal{F}_1 \rightarrow -7$$

$W$  contribution larger than top-quark, they interfere destructively



# Putting it all together



Most important channels:

$M_H \leq 130$  GeV:  $bb$ ,  $\tau\tau$ ,  $\gamma\gamma$  (clean signature)

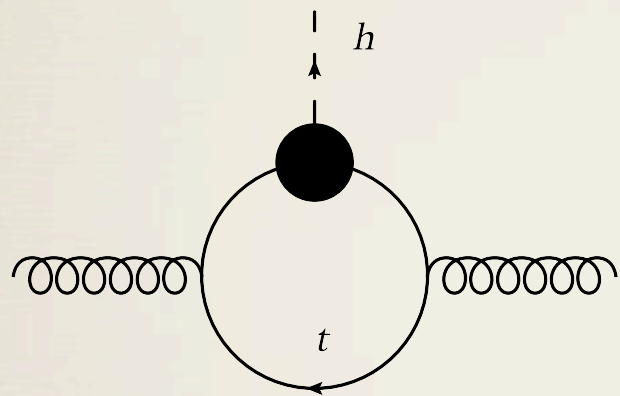
$M_H \geq 130$  GeV:  $WW$ ,  $ZZ$

(boundaries are rough)



# Refinement: low-energy theorems

- \* Can exactly calculate QCD corrections to  $h \rightarrow gg, \gamma\gamma$  (two-loop diagrams plus real radiation for  $gg$  decay) Djouadi, Spira, Zerwas early 1990s
- \* Useful, illuminating alternative approach for  $2m_t > M_H$



$$\frac{i}{\not{k} - m_t} \rightarrow \frac{i}{\not{k} - m_t} \frac{-im_t}{v} \frac{i}{\not{k} - m_t} = i \frac{m_t}{v} \left( \frac{1}{\not{k} - m_t} \right)^2$$

$$= \frac{m_t}{v} \frac{\partial}{\partial m_t} \frac{i}{\not{k} - m_t}$$

Generates both diagrams in the  $M_H \rightarrow 0$  limit

- \* Diagrammatically, clear that Higgs interaction comes from derivatives of the top part of the gluon self-energy:

$$\mathcal{M}(hgg) \underset{p_H \rightarrow 0}{=} \frac{m_t}{v} \frac{\partial}{\partial m_t} \mathcal{M}(gg)$$



# Effective Lagrangian

\* Integrate out top quark to produce effective Lagrangian

Equate propagators in full QCD and EFT

$$\begin{aligned}
 \mathcal{L} &= -\frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu} + \mathcal{L}_{top} \\
 \Rightarrow \underbrace{G_{\mu}^{a'}}_{\text{EFT field}} &= \zeta_3 \underbrace{G_{\mu}^a}_{\text{full QCD}} \\
 \Rightarrow \mathcal{L}_{EFT} &= -\frac{\zeta_3}{4} G_{\mu\nu}^{a'} G_a^{\mu\nu'}
 \end{aligned}
 \quad \Rightarrow \quad
 \begin{aligned}
 -\frac{ig_{\mu\nu}}{p^2} \zeta_3 &= -\frac{ig_{\mu\nu}}{p^2} \underbrace{[1 + \Pi_t(0)]}_{m_t^2 \gg p^2} \\
 \Rightarrow \zeta_3 &= 1 + \Pi_t(0) \\
 \Rightarrow \mathcal{L}_{EFT} &= -\frac{[1 + \Pi_t(0)]}{4} G_{\mu\nu}^{a'} G_a^{\mu\nu'}
 \end{aligned}$$

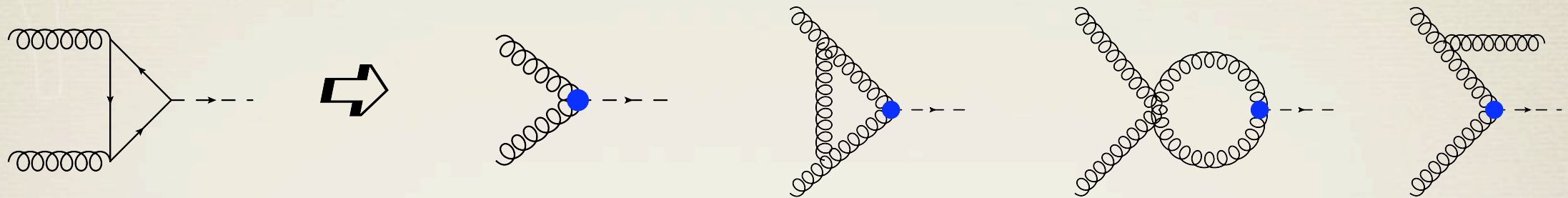
\* Can generate hgg amplitudes from derivatives of gg amplitudes:

$$\begin{aligned}
 \mathcal{L}_{EFT}^{hgg} &= -\frac{m_t}{4v} \left( \frac{\partial}{\partial m_t} \Pi_t(0) \right) h G_{\mu\nu}^{a'} G_a^{\mu\nu'} \\
 \Rightarrow \Pi_t(0) &= \frac{\alpha_s}{6\pi} \left[ \frac{\bar{\mu}^2}{m_t^2} \right]^\epsilon \frac{\Gamma(1+\epsilon)}{\epsilon} \\
 \Rightarrow \mathcal{L}_{EFT}^{hgg} &= \frac{\alpha_s}{12\pi} \frac{h}{v} G_{\mu\nu}^{a'} G_a^{\mu\nu'}
 \end{aligned}$$



# Decay in the EFT

- \* Reduces 2-loop calculation  $\Rightarrow$  1-loop; separates  $m_t$  dependence



- \* Systematically improvable to all orders in  $\alpha_s$

$$\mathcal{L}_{EFT}^{hgg} = -C_1 \frac{h}{v} G_{\mu\nu}^{a'} G_a^{\mu\nu'}$$

$$C_1 = -\frac{1}{12} \frac{\alpha_s}{\pi} \left\{ 1 + \frac{\alpha_s}{\pi} \left( \frac{11}{4} - \frac{1}{6} \ln \frac{\mu^2}{m_t^2} \right) + \dots \right\}$$

Correction to  $h \rightarrow$  light hadrons:  
(must include qq at higher orders)

$$K = 1 + 17.9167 a'_s + 152.5(a'_s)^2 + 381.5(a'_s)^3$$

$$= 1 + \underbrace{0.65038}_{\text{Large!}} + 0.20095 + 0.01825.$$

Large!

Baikov, Chetyrkin  
hep-ph/0604194

- \* Can do same for  $h \rightarrow \gamma\gamma$  decay, for W contribution also

For references and subtleties, see Chetyrkin et al. hep-ph/9708255, Kniehl, Spira hep-ph/9504378



# Decays beyond the SM

- \* NMSSM: decays to light CP-odd scalar can produce final states  $h \rightarrow aa \rightarrow bb\tau\tau, \tau\tau\tau, \tau\tau\gamma\gamma, \dots$
- \* Extended scalar sectors: decays to stable scalars (dark matter) can make Higgs invisible decaying

$m_{h_1}/m_{a_1}$ (GeV)	Branching Ratios			$n_{\text{obs}}/n_{\text{exp}}$ units of $1\sigma$	$s_{95}$	$N_{SD}^{LHC}$
	$h_1 \rightarrow b\bar{b}$	$h_1 \rightarrow a_1 a_1$	$a_1 \rightarrow \tau\bar{\tau}$			
98.0/2.6	0.062	0.926	0.000	2.25/1.72	2.79	1.2
100.0/9.3	0.075	0.910	0.852	1.98/1.88	2.40	1.5
100.2/3.1	0.141	0.832	0.000	2.26/2.78	1.31	2.5
102.0/7.3	0.095	0.887	0.923	1.44/2.08	1.58	1.6
102.2/3.6	0.177	0.789	0.814	1.80/3.12	1.03	3.3
102.4/9.0	0.173	0.793	0.875	1.79/3.03	1.07	3.6
102.5/5.4	0.128	0.848	0.938	1.64/2.46	1.24	2.4
105.0/5.3	0.062	0.926	0.938	1.11/1.52	2.74	1.2

Dermisek, Gunion hep-ph/0510322

$$\mathcal{L}_S = \frac{1}{2} \partial_\mu S \partial^\mu S - \frac{1}{2} m_S^2 S^2 - \frac{k}{2} |H|^2 S^2 - \frac{h}{4!} S^4$$

$h \rightarrow SS$  decays can dominate

Burgess, Pospelov, ter Veldhuis NPB 619  
(2001); Davoudiasl et al. hep-ph/0405097

**Many** deviations, some drastic, from SM predictions possible!



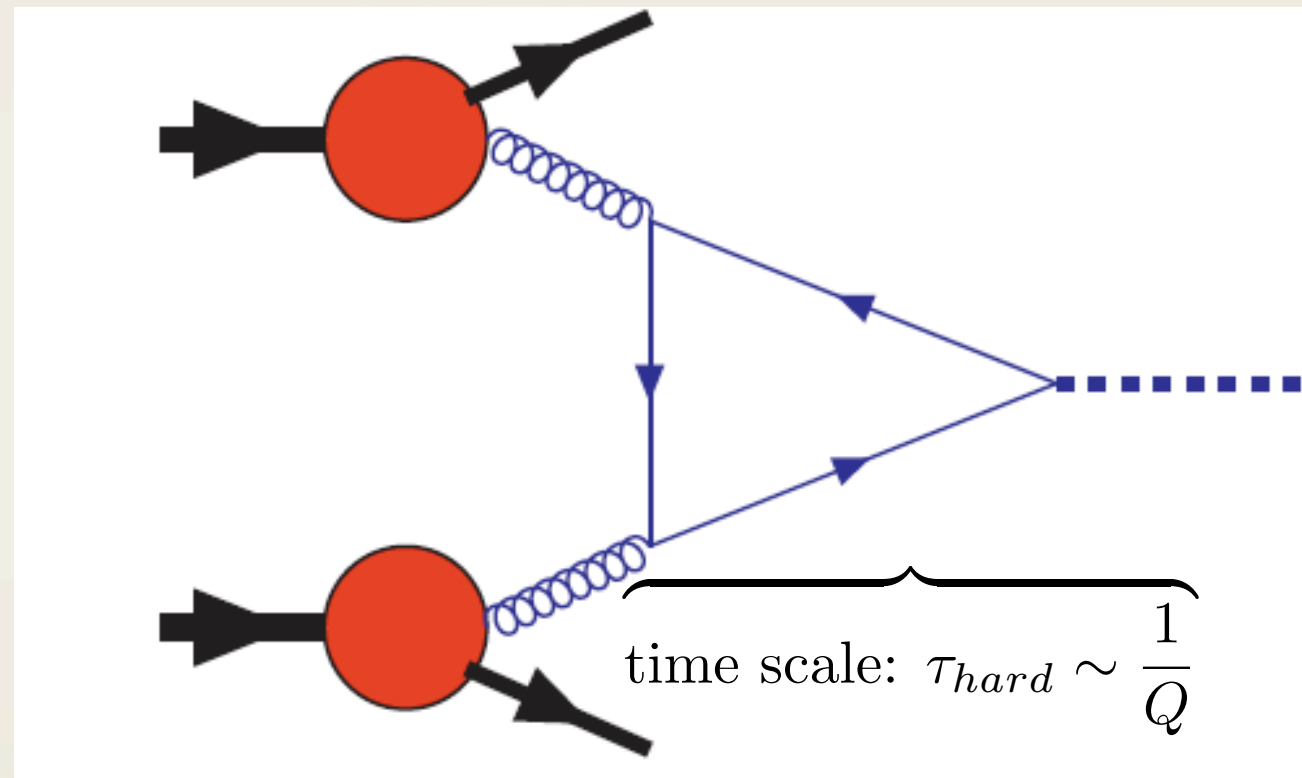
# **Producing the Higgs boson**



# Hadron collider basics

- \* The basic picture of hadronic collisions: factorize long and short time processes

$$\underbrace{\text{time scale: } \tau_{proton} \sim \frac{1}{\Lambda_{QCD}}}$$

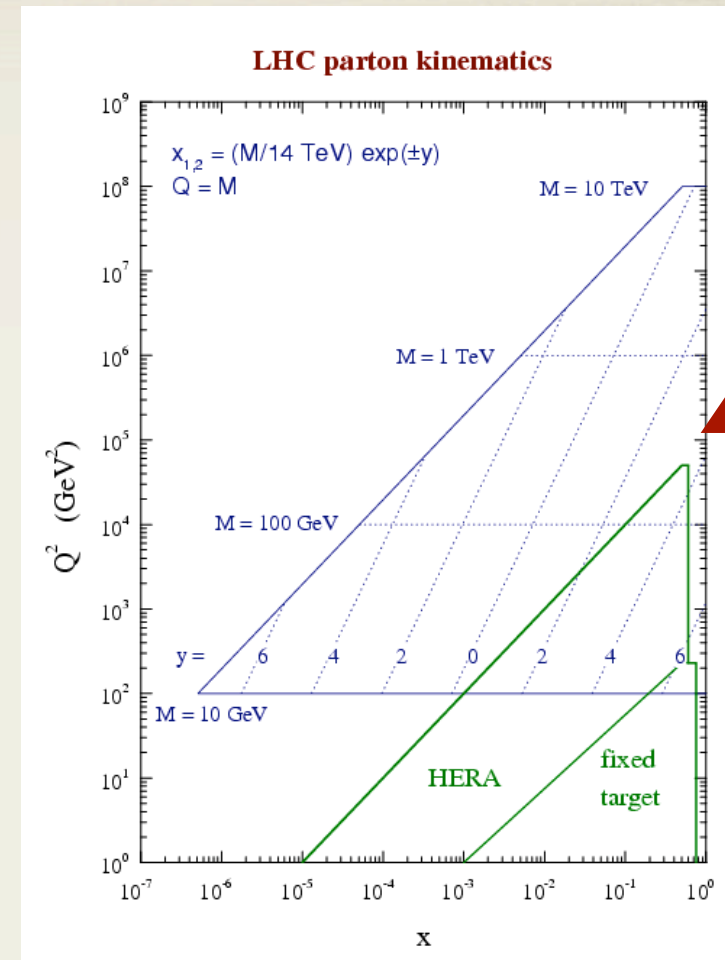
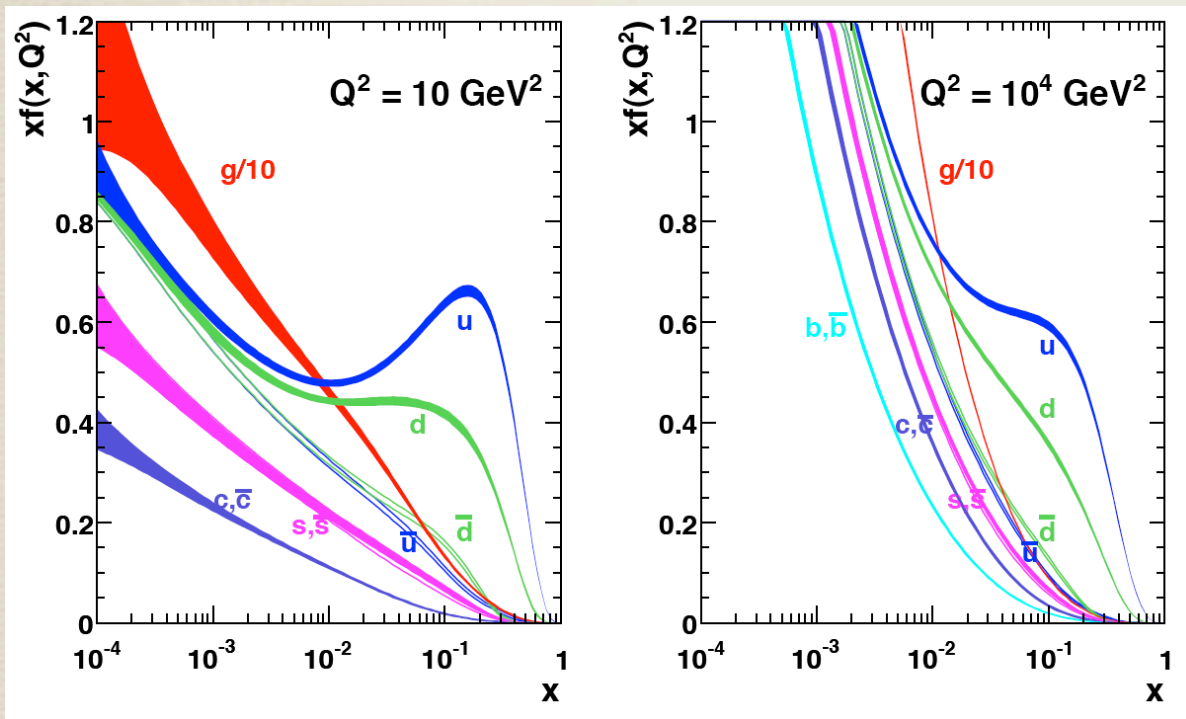


$$\sigma_{h_1 h_2 \rightarrow X} = \int dx_1 dx_2 \underbrace{f_{h_1/i}(x_1; \mu_F^2) f_{h_2/j}(x_2; \mu_F^2)}_{PDFs} \underbrace{\sigma_{ij \rightarrow X}(x_1, x_2, \mu_F^2, \{q_k\})}_{\text{partonic cross section}} + \underbrace{\mathcal{O}\left(\frac{\Lambda_{QCD}}{Q}\right)^n}_{\text{power corrections}}$$

factorization scale



# Parton distribution functions



DGLAP

$$x \sim M_H / \sqrt{s}$$

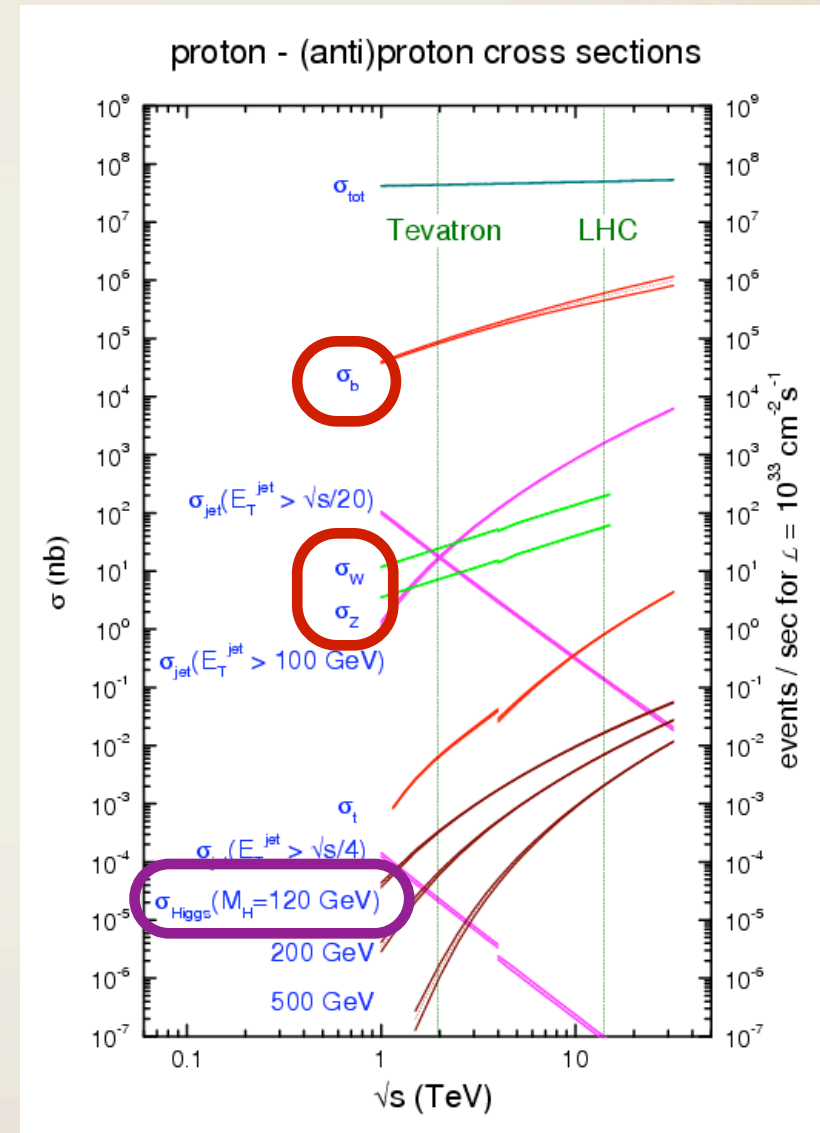
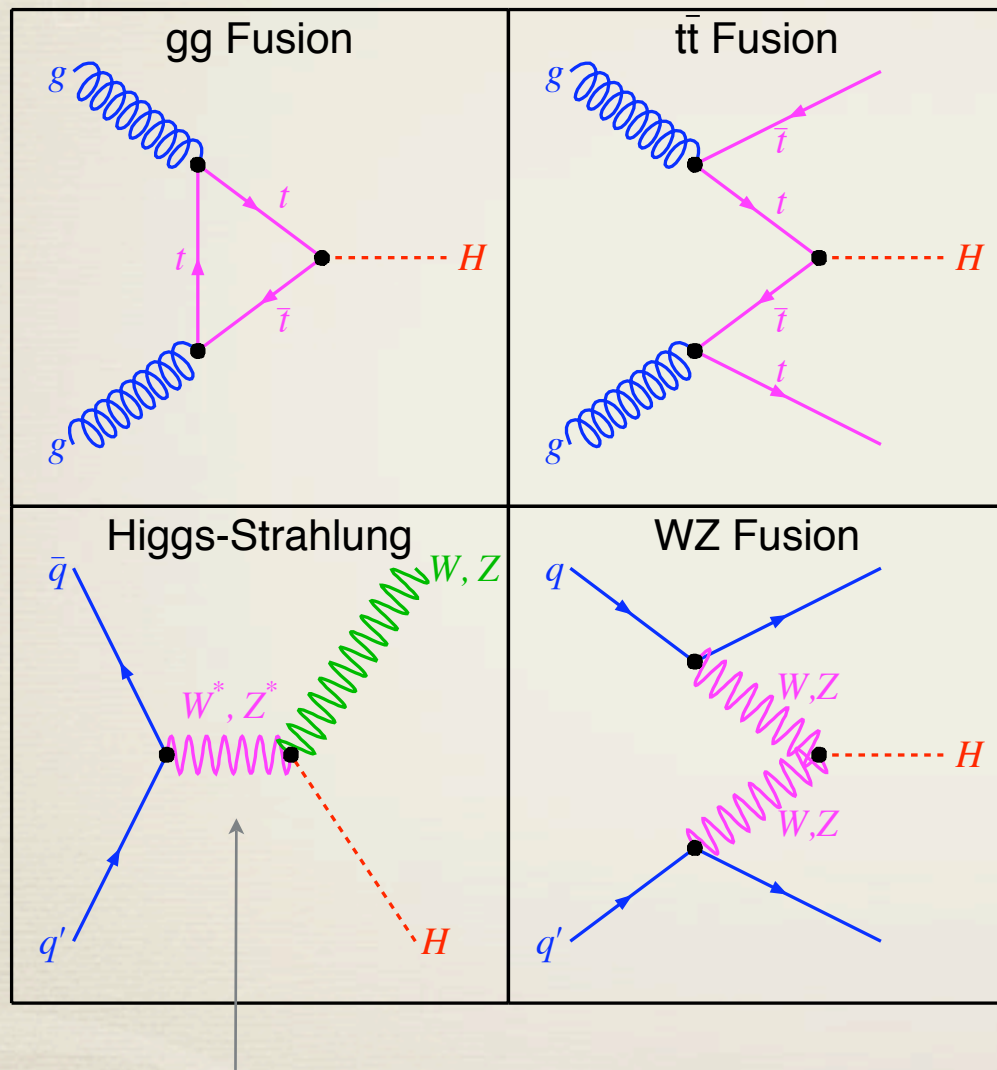
$\uparrow$  LHC       $\uparrow$  Tevatron

Lots of gluons, at LHC especially



# Higgs at hadron colliders

- \* Clearly want to use large gluon luminosity; W, Z assisted production another option



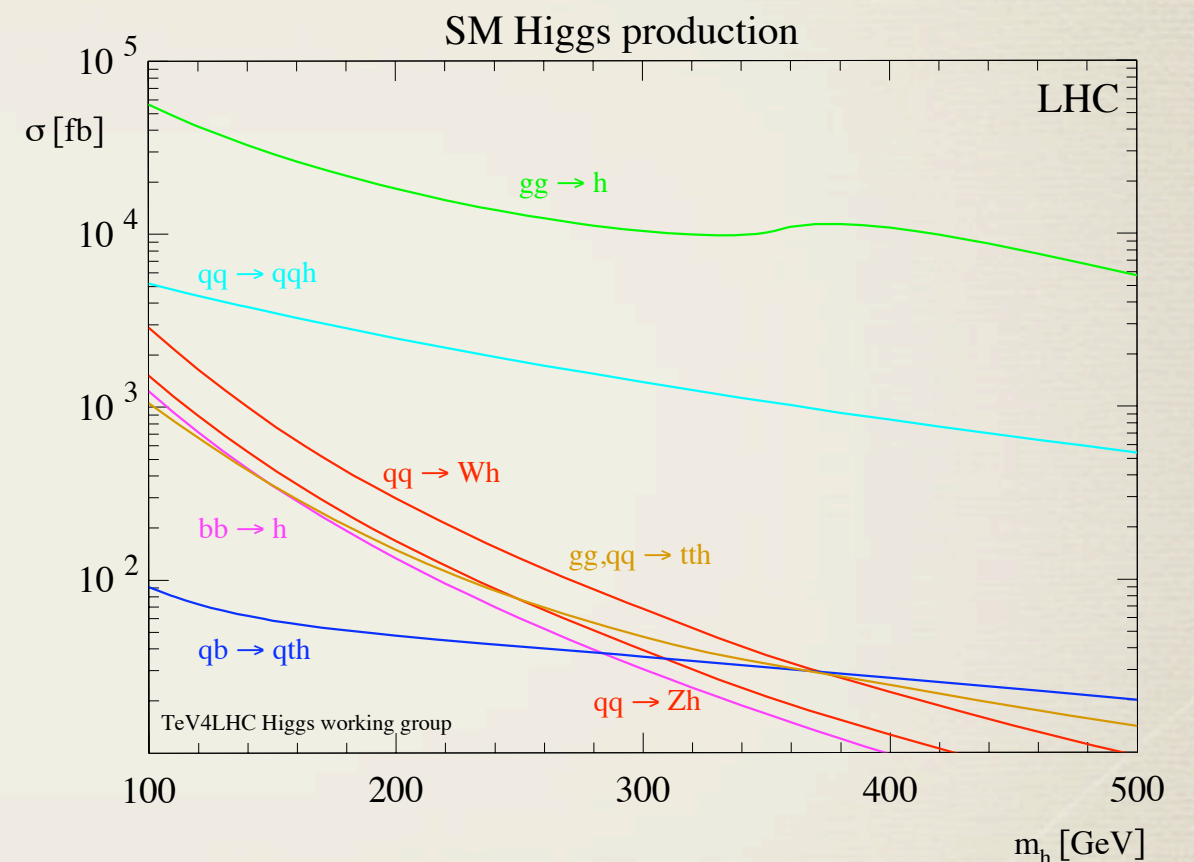
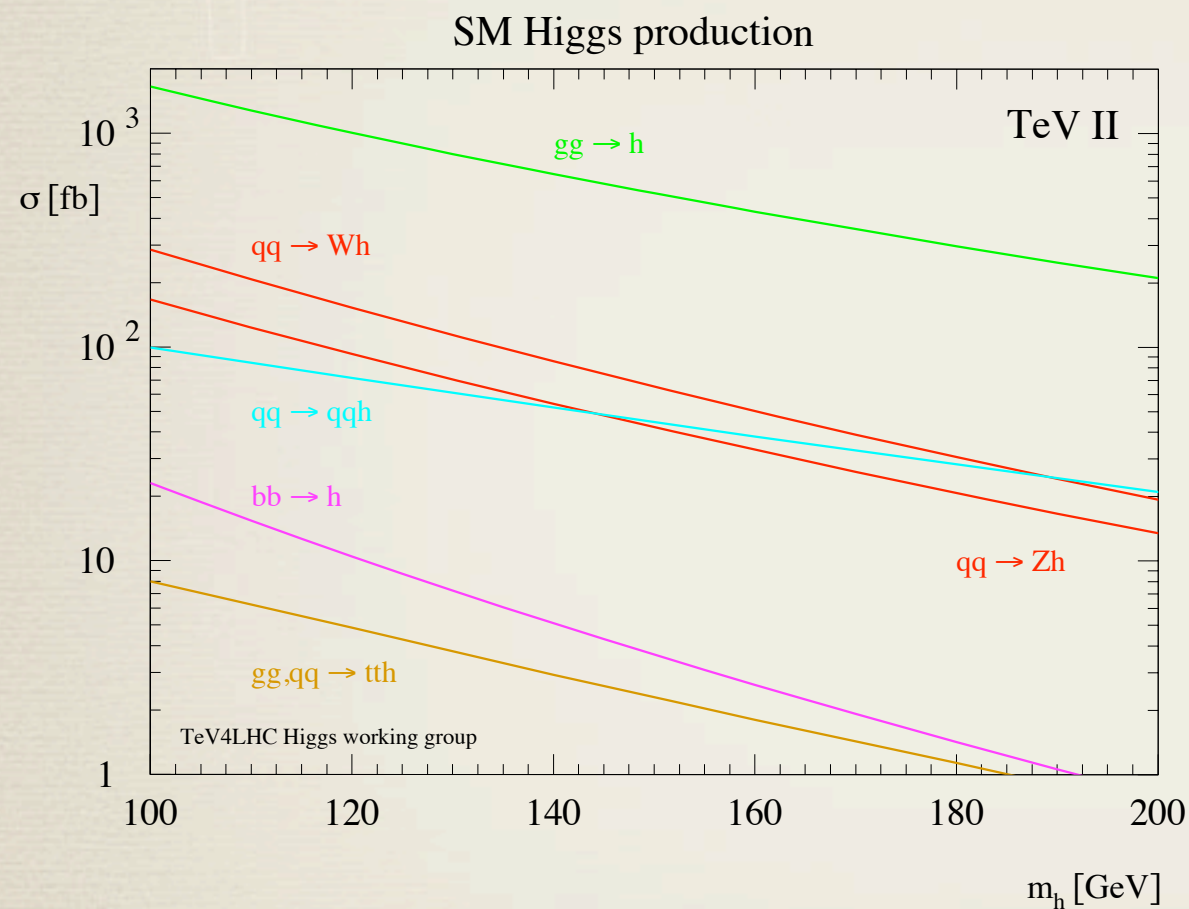
Can't do LEP search,  $\sqrt{s}$  not fixed at hadron machine

Any hadron collider search must confront backgrounds



# Overview of Higgs cross sections

- \* Gluon-fusion dominant at both colliders; WH next at Tevatron, WBF at LHC

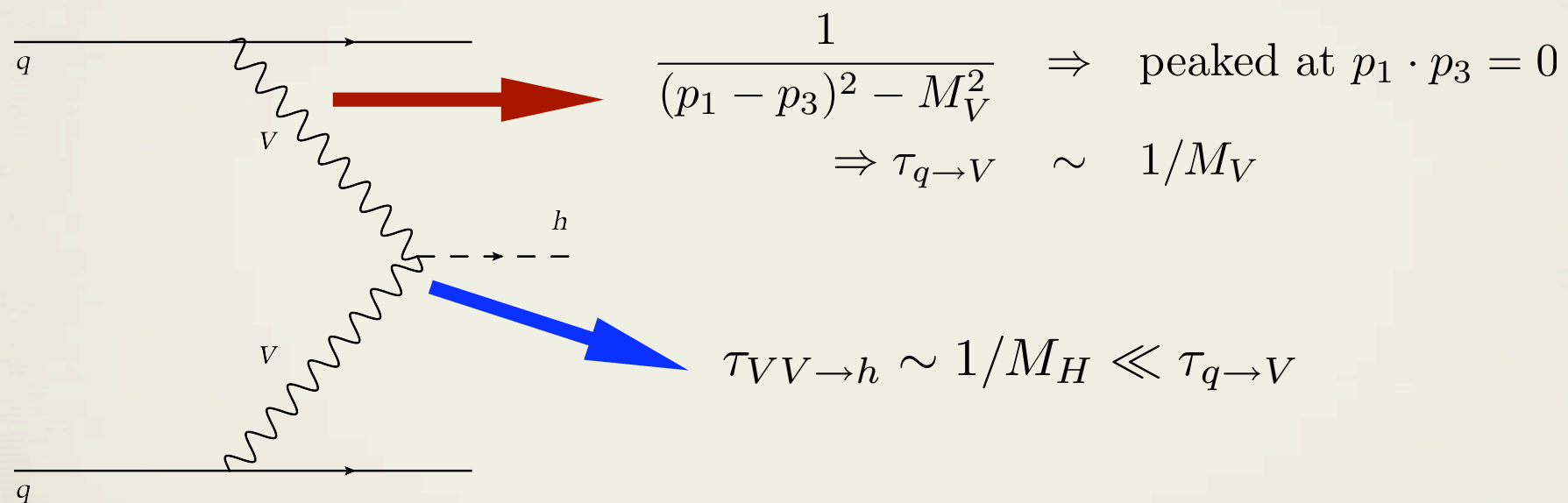


- \* SUSY:  $g_{bbh} \sim \tan^2 \beta$ ; becomes dominant at  $\tan \beta \sim 10$
- \* Plan: discuss WBF and gluon-fusion properties (some tricky/interesting aspects), then move on to searches at Tevatron/LHC



# Weak boson fusion: effective W/Z

- \* Important throughout large region of Higgs mass and in many decay modes; forward jets give experimental handle
- \* First approximation: inclusive cross section for  $M_H \gg M_{W,Z}$



- \* Should be able to factorize, think of V as a parton in q

$$\sigma_{qq \rightarrow VV \rightarrow h} = \int dz_1 dz_2 f_{q/V_1}(z_1) f_{q/V_2}(z_2) \sigma_{VV \rightarrow h}$$



# WBF + the equivalence theorem

- \* Can derive when  $M_V \ll \sqrt{s}$  (small angle scattering dominated)

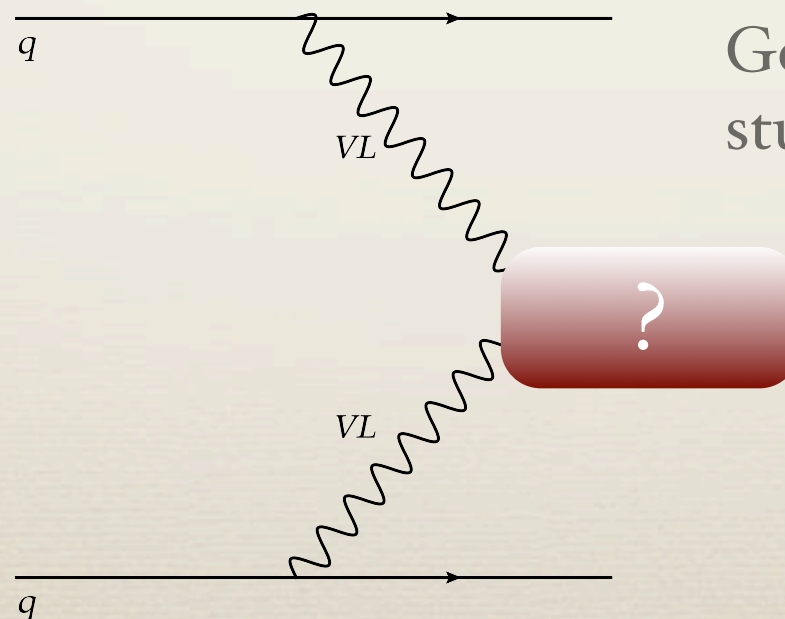
$$\sigma_{q_1 q_2 \rightarrow VV \rightarrow h} = \int_{2M_V/\sqrt{\hat{s}}}^1 dz_1 \int_{2M_V/\sqrt{\hat{s}}}^1 dz_2 f_{q/V_L}(z_1) f_{q/V_L}(z_2) \sigma_{V_L V_L \rightarrow h}(z_1 z_2 \hat{s})$$

$$\sigma_{V_L V_L \rightarrow h}(x) = \frac{\pi}{36} g_{HVV}^2 \frac{x}{M_V^2} \delta(x - M_H^2)$$

$$f_{q/V_L}(z) = \frac{g_v^2 + g_a^2}{4\pi^2} \frac{1-z}{z}$$

Exercise: Derive this

- \* Angular momentum cons. prevents emission of transverse boson with forward quark:  $\bar{u}^\pm(p\hat{z}) \not{\epsilon} u^\pm(p'\hat{z}) \Rightarrow$  Set  $\not{\epsilon} = \gamma^{1,2} \Rightarrow \xi_\pm^\dagger \sigma^{1,2} \xi_\pm = 0$

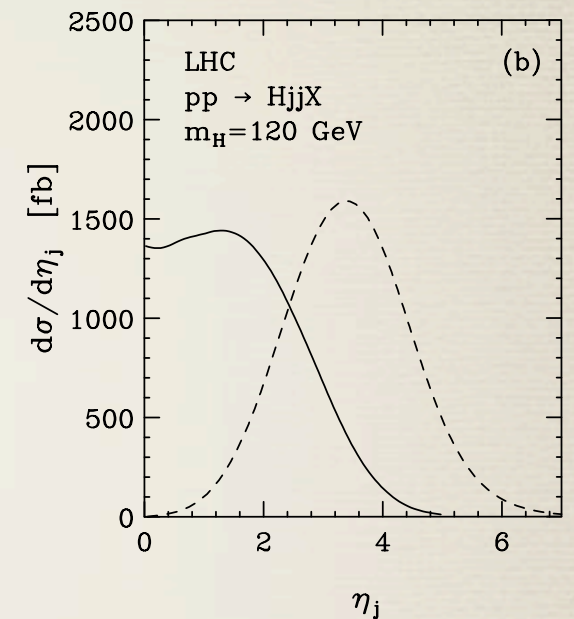
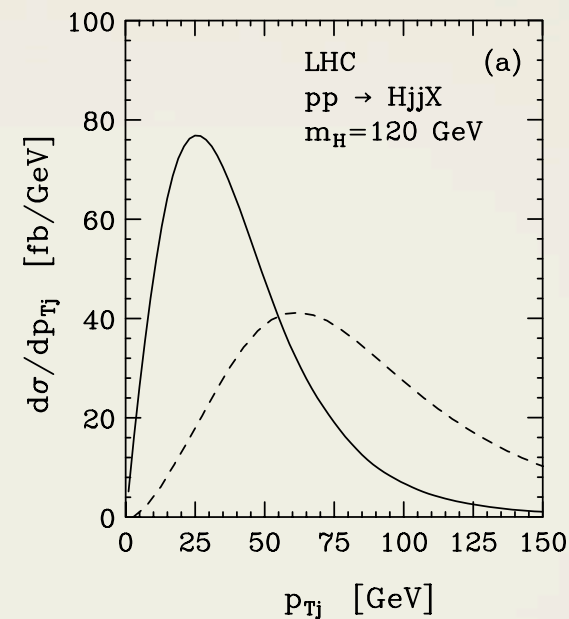
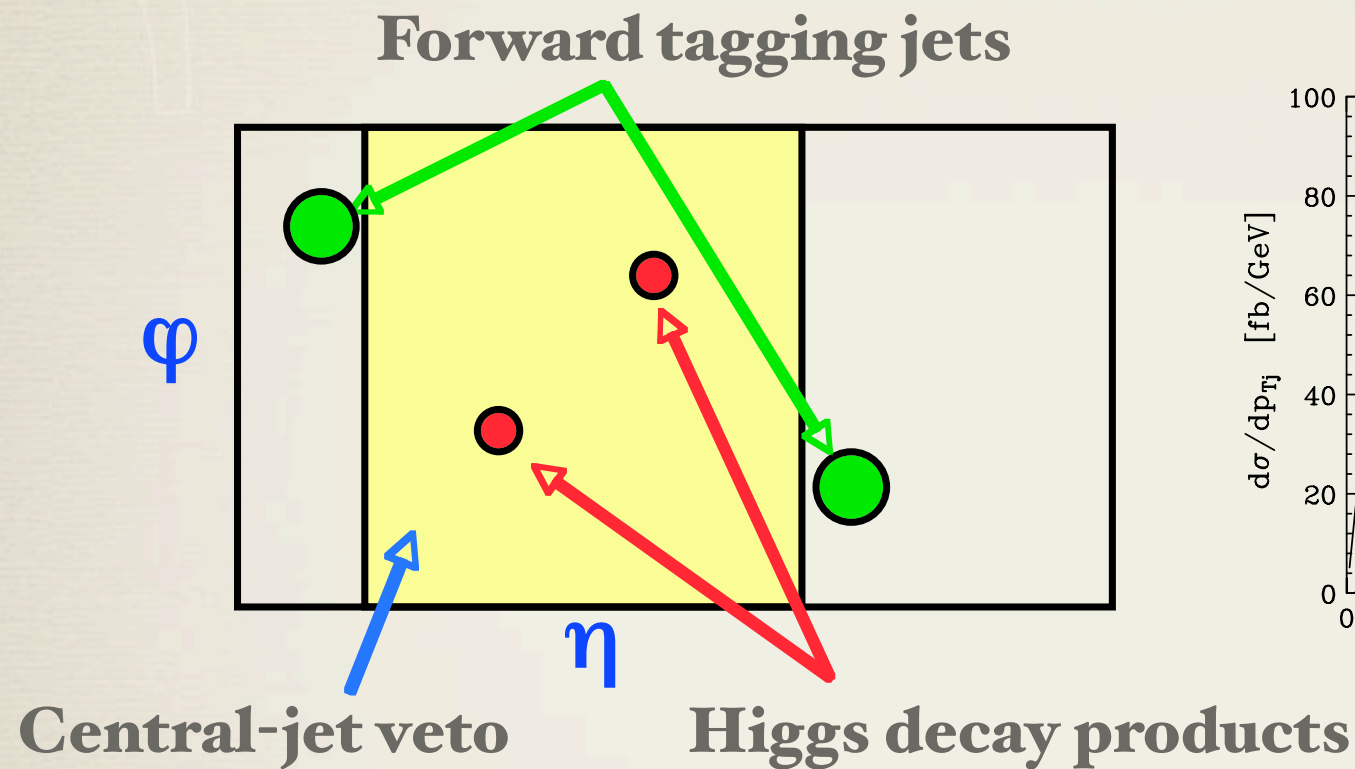


Good channel to study strong EWSB



# Kinematics of WBF

- \* Two energetic ( $p_T \sim 40$  GeV) jets with large rapidity separation



Rainwater, Zeppenfeld hep-ph/9906218  
and many others... check refs+citations

- \* Extra gluon emission suppressed; impose central jet veto

$$\mathcal{M}(q_1 q_2 \rightarrow q_3 q_4 h + g) \propto \mathcal{M}(q_1 q_2 \rightarrow q_3 q_4 h) T^a \left\{ \frac{p_3 \cdot \epsilon_g^a}{p_3 \cdot p_g} + \frac{p_4 \cdot \epsilon_g^a}{p_4 \cdot p_g} - \frac{p_1 \cdot \epsilon_g^a}{p_1 \cdot p_g} - \frac{p_2 \cdot \epsilon_g^a}{p_2 \cdot p_g} \right\}$$

$$\rightarrow 0 \text{ since } p_1 \parallel p_3, p_2 \parallel p_4$$

Exercise: Derive this

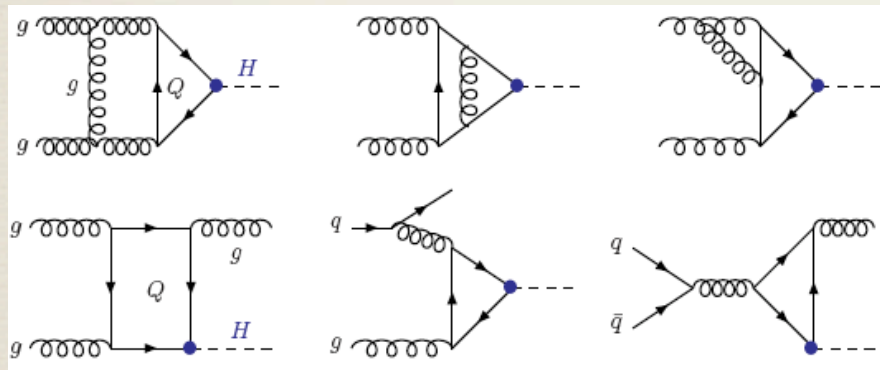


# Gluon fusion production

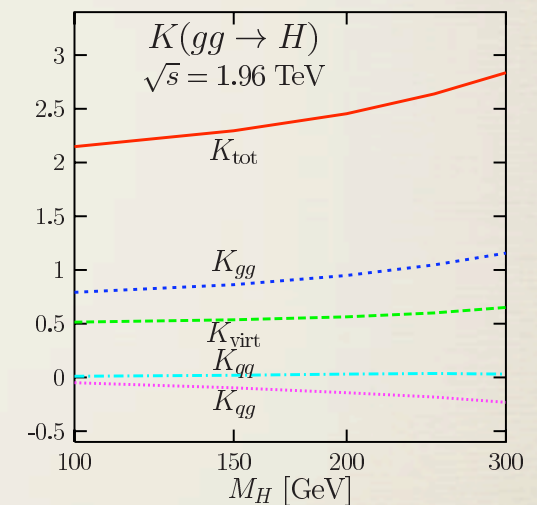
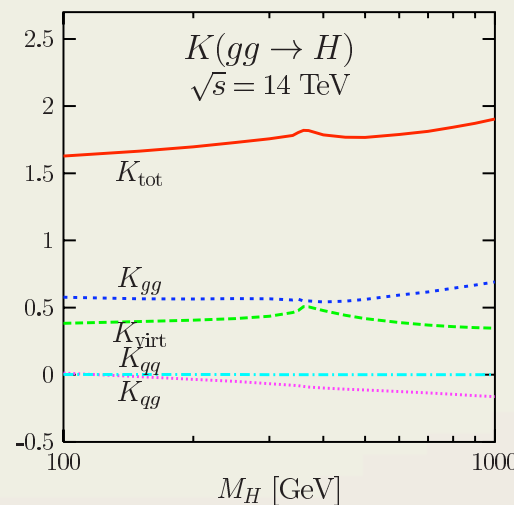
- \* Largest mode at Tevatron and LHC; through top-quark loops

$$\sigma_{gg \rightarrow h}^{LO} = \frac{G_F \alpha_s^2}{288\pi\sqrt{2}} \left| \frac{3}{4} \sum_Q \mathcal{F}_{1/2}(\tau_Q) \right|^2 \delta(1-z), \quad \tau_Q = \frac{M_H^2}{4m_Q^2}, \quad z = \frac{M_H^2}{\hat{s}}$$

- \* NLO QCD corrections require 2-loop virtual, 1-loop real-virtual



Djouadi, Graudenz, Spira, Zerwas PLB 264 (1991), hep-ph/9504378



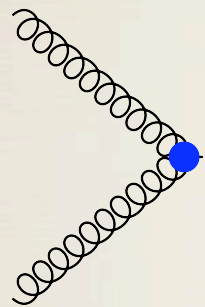
- \* Can reach  $K_{NLO} = \sigma_{NLO}/\sigma_{LO} \approx 2$  at LHC, 3 at Tevatron; why so large?



# EFT gluon-fusion

- \* Study carefully in the EFT with Hgg vertex

$$\sigma_{ij} = \sigma_0 \left\{ G_{ij}^{(0)} + \frac{\alpha_s}{\pi} G_{ij}^{(1)} + \mathcal{O}(\alpha_s^2) \right\} \quad \mathcal{L}_{EFT} = \frac{1}{12} \frac{\alpha_s}{\pi} \left[ 1 + \frac{11}{4} \frac{\alpha_s}{\pi} + \mathcal{O}(\alpha_s^2) \right]$$



$$G_{ij}^{(0)} = \delta(1-z) \delta_{ig} \delta_{jg} \quad (\text{Overall factors in } \sigma_0)$$

( $z=M^2/x_1/x_2/s$ ; integral over PDFs  $\Rightarrow$  integral over  $z$ )

- \* NLO receives contributions from 5 pieces: virtual diagrams, real-radiation, ultraviolet renormalization, PDF renormalization correction to EFT coefficient

Notes:

- Everything in  $d=4-2\epsilon$  dimensions; gluon has  $d-2$  polarization states
- Scaleless integrals vanish  $\longrightarrow$
- Coupling constant gets dimensions:  
 $g \rightarrow g\mu^\epsilon$
- Feynman gauge
- Only gg initial-state (others smaller, simpler)

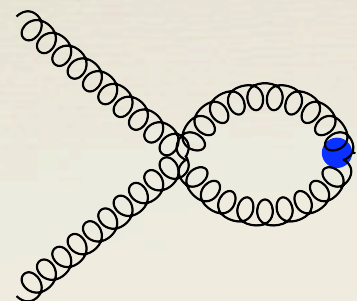
$$\int d^d k \frac{1}{k^2} \sim \frac{1}{\epsilon_{UV}} - \frac{1}{\epsilon_{IR}} \rightarrow 0$$

J. Collins, *Renormalization*.

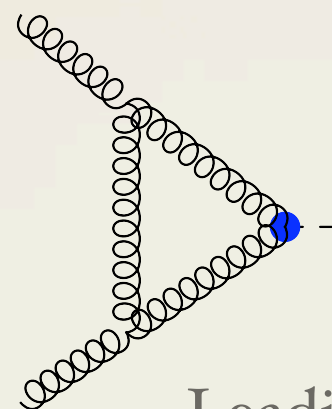


# Gluon-fusion: virtual

\* Virtual:



$$= \frac{\alpha_s}{\pi} \frac{\Gamma(1 + \epsilon)}{(4\pi)^{-\epsilon}} \left( \frac{\mu^2}{\hat{s}} \right)^\epsilon \left\{ -\frac{13}{4\epsilon} - \frac{83}{12} \right\} \delta(1 - z)$$



$$= \frac{\alpha_s}{\pi} \frac{\Gamma(1 + \epsilon)}{(4\pi)^{-\epsilon}} \left( \frac{\mu^2}{\hat{s}} \right)^\epsilon \left\{ \left[ -\frac{3}{\epsilon^2} \right] + \frac{1}{4\epsilon} + \frac{47}{12} + 2\pi^2 \right\} \delta(1 - z)$$

Leading soft+collinear singularity; emitting gluons from gluons gives color factor  $C_A=3$

\* UV renormalization: counterterm for  $\alpha_s$  at leading order

Full d-dimensional LO

First term in beta-function

$$= \frac{\alpha_s}{\pi} \frac{\Gamma(1 + \epsilon)}{(4\pi)^{-\epsilon}} \frac{1}{\epsilon} G_{gg}^{(0),d} \{-2b_0\}$$

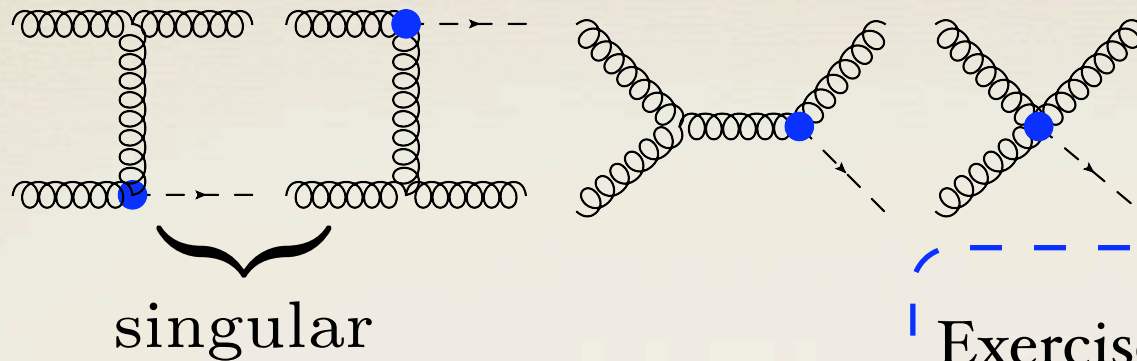
$$= \frac{\alpha_s}{\pi} \frac{\Gamma(1 + \epsilon)}{(4\pi)^{-\epsilon}} \left\{ -\frac{11}{2} + \frac{N_F}{3} \right\} \left[ \frac{1}{\epsilon} + 1 \right] \delta(1 - z)$$

Number of light fermions



# Gluon-fusion: real radiation

\* Real:



Phase space : 
$$\frac{1}{2\hat{s}} \int \frac{d^d p_g}{(2\pi)^d} \frac{d^d p_H}{(2\pi)^d} (2\pi) \delta(p_g^2) (2\pi) \delta(p_H^2 - M_H^2) (2\pi)^d \delta^{(d)}(p_1 + p_2 - p_g - p_H)$$

$$= \frac{1}{16\pi\hat{s}} \frac{s^{-\epsilon}}{(4\pi)^{-\epsilon} \Gamma(1-\epsilon)} (1-z)^{1-2\epsilon} \int_0^1 d\lambda \lambda^{-\epsilon} (1-\lambda)^{-\epsilon}$$

$$\Rightarrow \hat{t} = (p_1 - p_g)^2 = -\hat{s}(1-z)\lambda, \quad \hat{u} = (p_2 - p_g)^2 = -\hat{s}(1-z)(1-\lambda)$$

$$|\bar{\mathcal{M}}|^2 = 48 \alpha_s \left\{ \frac{(1-2\epsilon) M_H^8 + \hat{s}^4 + \hat{t}^4 + \hat{u}^4}{(1-\epsilon)^2} + \frac{\epsilon}{2(1-\epsilon)^2} \frac{(M_H^4 + \hat{s}^2 + \hat{t}^2 + \hat{u}^2)^2}{\hat{s}\hat{t}\hat{u}} \right\}$$

$$\Rightarrow (1-z)^{-1-2\epsilon} \lambda^{-1-\epsilon} (1-\lambda)^{-1-\epsilon}$$

singular                      regulator

$\lambda$ : collinear  
 $z$ : soft



# Real radiation and plus dists.

\* Extract singularities using plus distribution expansion

$$\lambda^{-1-\epsilon} = -\frac{1}{\epsilon}\delta(\lambda) + \frac{1}{[\lambda]_+} - \epsilon \left[ \frac{\ln \lambda}{\lambda} \right]_+ + \mathcal{O}(\epsilon^2), \text{ etc.}$$

$$\int_0^1 dx f(x)[g(x)]_+ = \int_0^1 dx [f(x) - f(0)]g(x)$$

$$\Rightarrow \frac{\alpha_s}{\pi} \frac{\Gamma(1+\epsilon)}{(4\pi)^{-\epsilon}} \left( \frac{\mu^2}{\hat{s}} \right)^\epsilon \left\{ \begin{array}{l} \overbrace{\left[ \frac{3}{\epsilon^2} + \frac{3}{\epsilon} \right] \delta(1-z)}^{\text{cancels virtual poles}} - \frac{6}{\epsilon} \frac{1}{[1-z]_+} + \frac{6z(z^2 - z + 2)}{\epsilon} \\ + (3 - \pi^2) \delta(1-z) - \frac{6}{[1-z]_+} + 12 \left[ \frac{\ln(1-z)}{1-z} \right]_+ - \frac{6(z^2 - z + 1)^2 \ln z}{1-z} \\ - 12z(z^2 - z + 2) \ln(1-z) - \frac{11}{2} + \frac{57z}{2} - \frac{45z^2}{2} + \frac{23z^3}{2} \end{array} \right\}$$



# Remaining terms

- \* PDF renormalization: counterterm for initial-state collinear sings.

$$= \frac{\alpha_s}{\pi} \frac{\Gamma(1+\epsilon)}{(4\pi)^{-\epsilon}} \frac{1}{\epsilon} G_{gg}^{(0),d}(\underline{P}_{gg}(z)) \longrightarrow \text{Altarelli-Parisi splitting function}$$

$$= \frac{\alpha_s}{\pi} \frac{\Gamma(1+\epsilon)}{(4\pi)^{-\epsilon}} \left\{ \underbrace{\left( \frac{11}{2} - \frac{N_F}{3} \right) \delta(1-z)}_{\text{cancels UV counterterm}} + \underbrace{\frac{6}{[1-z]_+} - 6z(z^2 - z + 2)}_{\text{cancels real radiation}} \right\} \left[ \frac{1}{\epsilon} + 1 \right]$$

- \* Coefficient correction:  $= \frac{\alpha_s}{\pi} \frac{11}{2} \delta(1-z)$

- \* Can check that  $(\mu^2/s)^\epsilon$  terms give  $\ln(\mu^2/s)$  upon expansion  $\Rightarrow$  combined with scale dependence of  $\alpha_s$  (implicit so far) and PDFs give estimate of theoretical uncertainty (can also get these logs from renormalization group considerations)



# Final result

\* Final result for NLO correction:

$$G_{gg}^{(1)} = \left( \frac{11}{2} + \pi^2 \right) \delta(1-z) + 12 \left[ \frac{\ln(1-z)}{1-z} \right]_+ - 12z(-z + z^2 + 2)\ln(1-z) - 6 \frac{(z^2 + 1 - z)^2}{1-z} \ln(z) - \frac{11}{2} (1-z)^3$$

(M<sup>2</sup>/s ≤ z ≤ 1)  
(integrate over PDFs, removes singularity)

\* What is the source of the π<sup>2</sup>? Since 1/ε<sup>2</sup> poles cancel, can change that Γ(1+ε) normalizing the real, virtual can be exchanged for something that differs at O(ε<sup>2</sup>) ⇒ shuffles terms between R, V

$$\Gamma(1 + \epsilon) \rightarrow \underbrace{\frac{1}{\Gamma^2(1 - \epsilon)\Gamma(1 + \epsilon)}}_{\mathcal{N}} \Gamma^2(1 - \epsilon)\Gamma^2(1 + \epsilon) = \mathcal{N} \left( 1 + \frac{\pi^2}{3}\epsilon^2 + \mathcal{O}(\epsilon^4) \right)$$

Real:  $\mathcal{N} \left( 1 + \frac{\pi^2}{3}\epsilon^2 \right) \left( \frac{3}{\epsilon^2} - \pi^2 + \dots \right) \delta(1-z) = \mathcal{N} \left( \frac{3}{\epsilon^2} + \dots \right)$

Virtual:  $\mathcal{N} \left( 1 + \frac{\pi^2}{3}\epsilon^2 \right) \left( -\frac{3}{\epsilon^2} + 2\pi^2 + \dots \right) \delta(1-z) = \mathcal{N} \left( -\frac{3}{\epsilon^2} + \pi^2 + \dots \right)$

Completely from analytic continuation:  $6(-\mu^2/s)^\epsilon = (\mu^2/s)^\epsilon \times (6 + \pi^2 + \text{imaginary parts} + \dots)$

From C<sub>A</sub>=3 color, 2×Re(M<sub>O</sub>M<sub>I</sub><sup>\*</sup>)

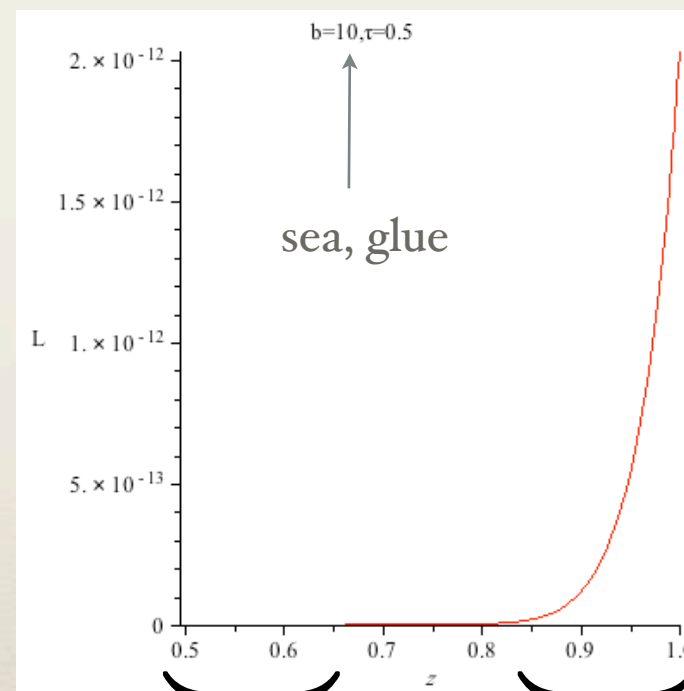
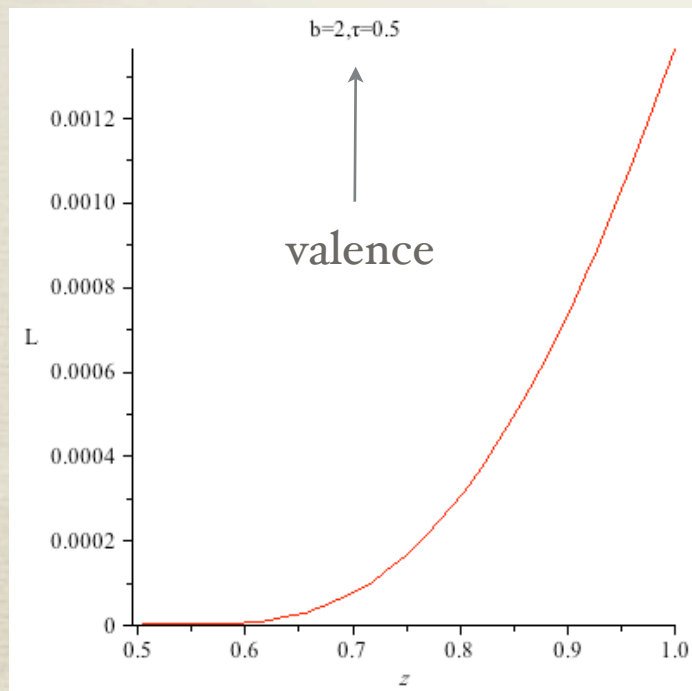


# Threshold logs and PDFs

- \* Logarithm is associated with soft radiation; is  $z \rightarrow 1$  region enhanced?
- \* Begin with hadronic cross section in following form ( $\tau = M^2/s$ ,  $z = M^2/x_1 x_2 s$ )  
partonic luminosity

$$\sigma_{had} = \tau \int_{\tau}^1 dz \frac{\sigma(z)}{z} \mathcal{L}\left(\frac{\tau}{z}\right), \quad \mathcal{L}(y) = \int_y^1 dx \frac{y}{x} f_1(x) f_2(y/x)$$

Assume  $f_i \sim x^a (1-x)^b$ ; plot L for various  $\tau$ , b ('a' less important)  
Look for peak near  $z \approx 1$



Clear importance for  $\tau \approx 1$ ; rapid fall-off of large- $z$  PDFs

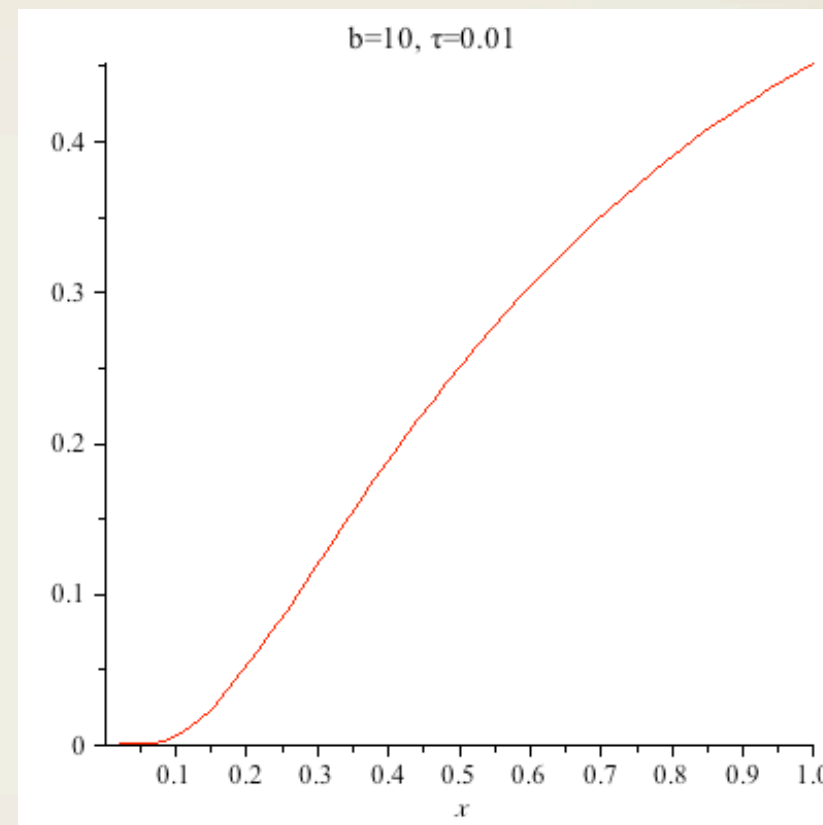
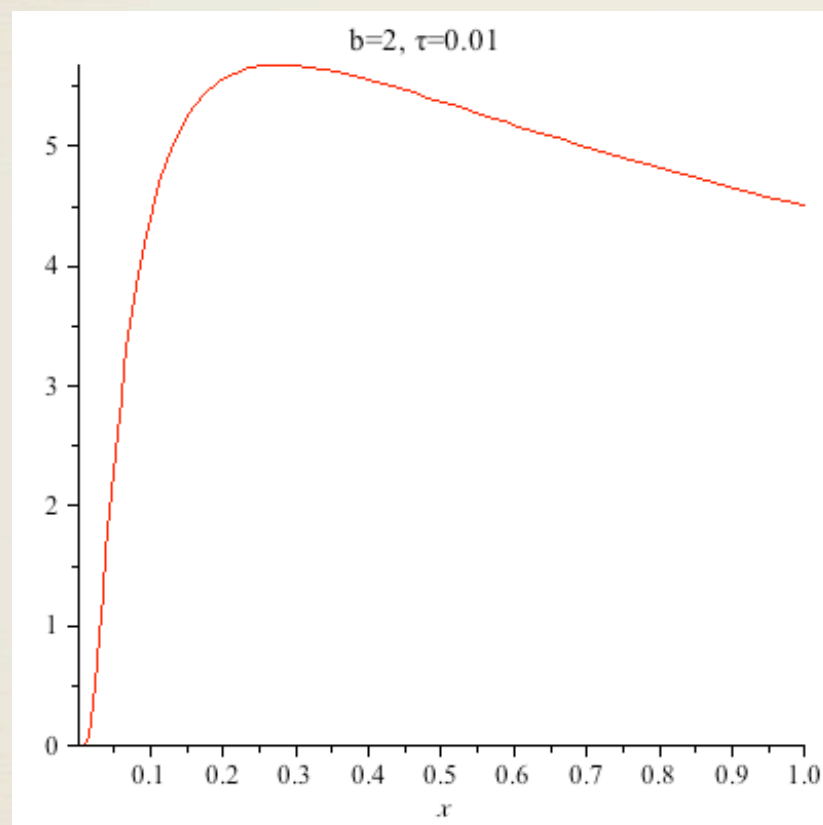
$$\int_0^1 dx \left[ \frac{\ln^n(1-x)}{1-x} \right]_+ \overset{\text{approximate } \mathcal{L}/x}{\theta(x-x_{cut})} = -\frac{1}{n+1} \ln^{n+1}(1-x_{cut})$$

Hard emissions      Threshold



# Threshold logs and PDFs

- \* Shape of PDFs near  $1$  important for small  $\tau$ ; large exponents in  $(1-z)^b$  can enhance region where logs are large



- \* A numerical question regarding how dominant the logarithmic terms are in the perturbative expansion; for Higgs, both plus dist. and  $\delta(1-z)$  give large corrections

(discussions in Kramer, Laenen, Spira hep-ph/9611272, Catani et al. hep-ph/0306211, Ahrens, Becher, Neubert, Yang 0809.4283)

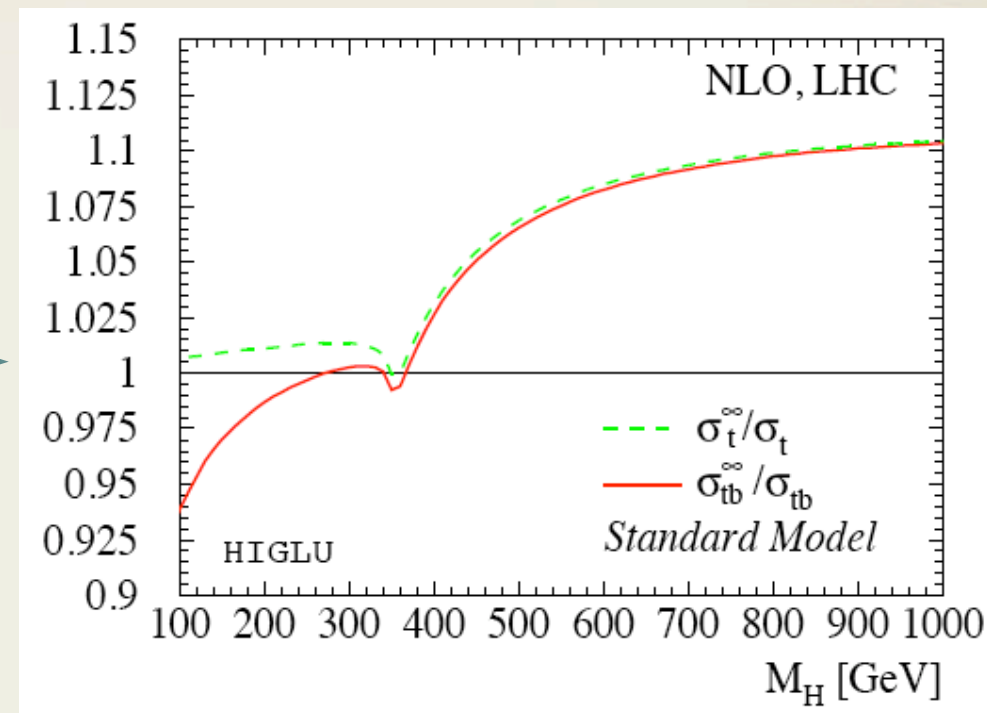


# Effective theory validity

- \* Clearly want to go beyond NLO, but the 3-loop massive computations in the full theory are intractable

$$\sigma_{NLO}^{approx} = \left( \frac{\sigma_{NLO}^{EFT}}{\sigma_{LO}^{EFT}} \right) \sigma_{LO}^{QCD}$$

%-level or better for  $M_H < 2m_t$ , even gets >90% of correction above



Harlander, 2009 Zurich Higgs workshop

Soft, collinear gluons do not resolve top-quark loop (e.g., soft gluons are eikonal×tree)

Kramer, Laenen, Spira; Marzani et al. 0801.2544

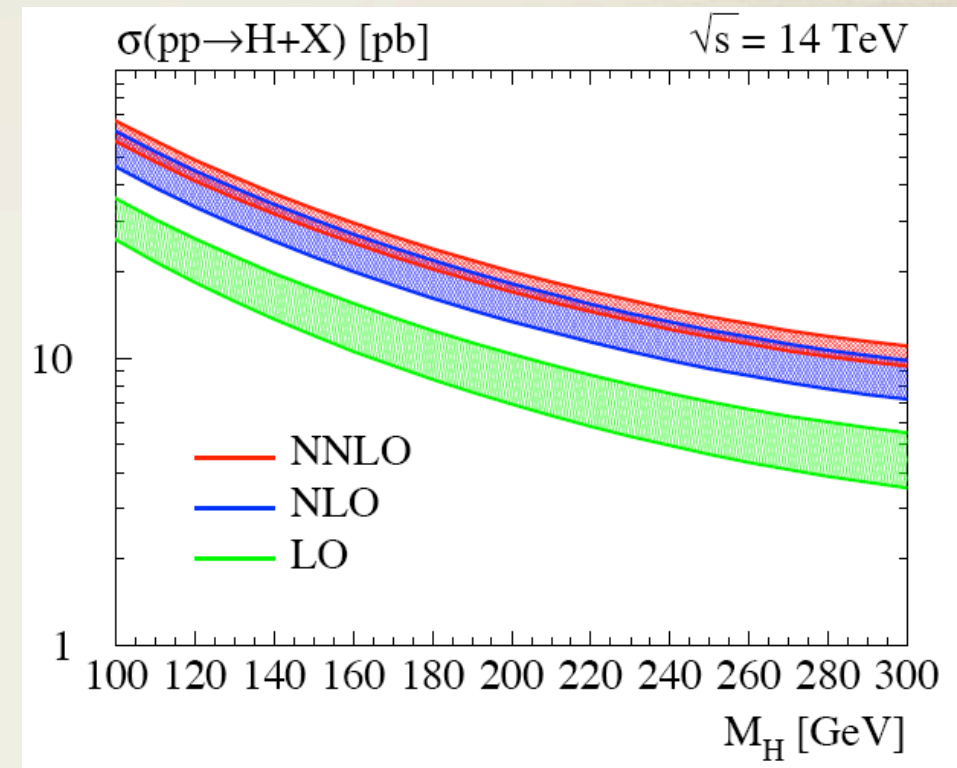
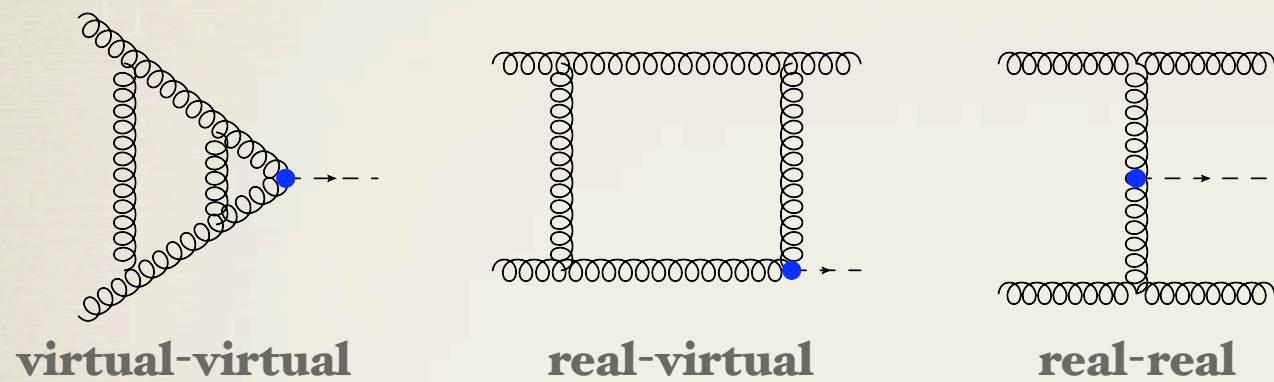
- \* Use EFT to go to NNLO

$$\sigma_{NNLO}^{approx} = \left( \frac{\sigma_{NNLO}^{EFT}}{\sigma_{LO}^{EFT}} \right) \sigma_{LO}^{QCD}$$

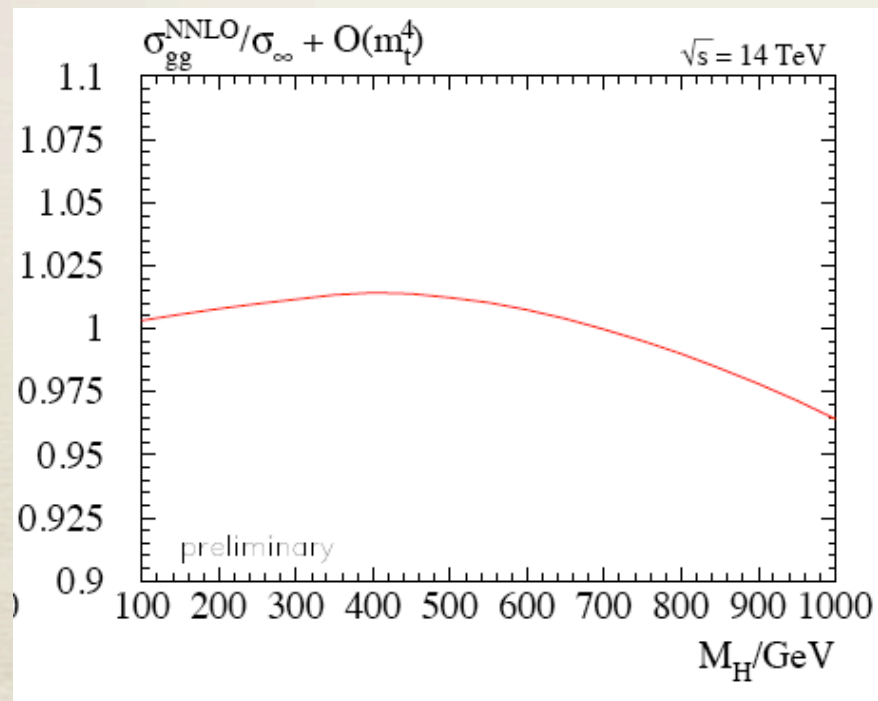


# Inclusive Higgs at NNLO

- \* Full calculation at NNLO in the EFT and resummation of logarithms



Harlander, Kilgore '02; Anastasiou, Melnikov '02; Ravindran, Smith van Neerven '03



K. Ozeren (w/ R. Harlander), LoopFest 2009

Recent asymptotic expansion of sub-leading  $1/m_t$  terms at NNLO indicates they are small



# Low- $p_T$ resummation

- \* One more issue with result; go back and look at real radiation

$$p_T^2 = \frac{\hat{t}\hat{u}}{\hat{s}} = \hat{s}(1-z)^2\lambda(1-\lambda)$$

$$\Rightarrow |\bar{\mathcal{M}}|^2 \times PS \sim (p_T^2)^{-1-\epsilon}$$

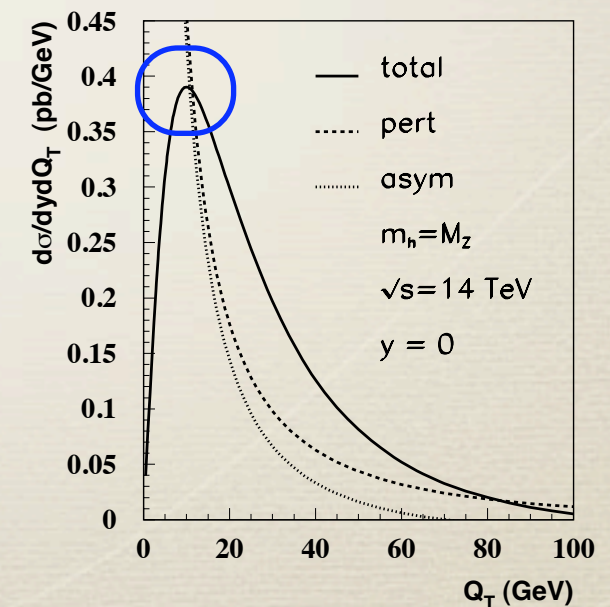
Fine if  $p_T$  integrated, but what if experiment selects low  $p_T$ ?

$$\int_0^{p_T^{max}} (p_T^2)^{-1-\epsilon} \rightarrow \ln \frac{M_H}{p_T^{max}} \gg 1 \text{ for } M_H \gg p_T^{max}$$

- \* If low  $p_T$  selected, need resummation of  $\ln(M_H/p_T)$  terms  
(Collins, Soper, Sterman '85; Berger, Qiu hep-ph/0210135; Bozzi et al. hep-ph/0302104; Balazs, Yuan and others)

Can show  $\frac{d\sigma}{dY dp_T^2} \approx \left(\frac{d\sigma}{dY}\right)_{LO} \exp\left(-\frac{3\alpha_s}{2\pi} \ln^2 s/p_T^2\right)$   
(J. Owens, CTEQ SS 2000)

Systematically improvable beyond this leading approximation



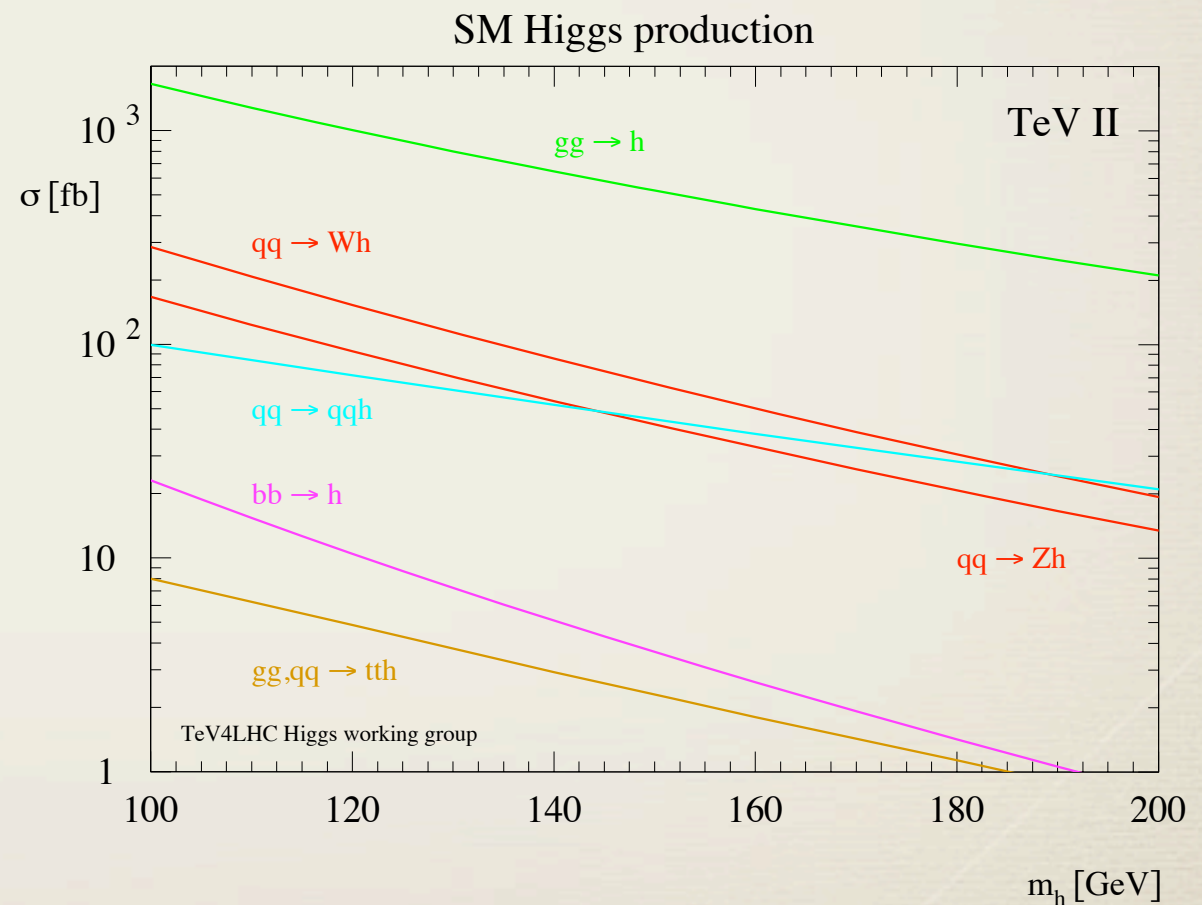
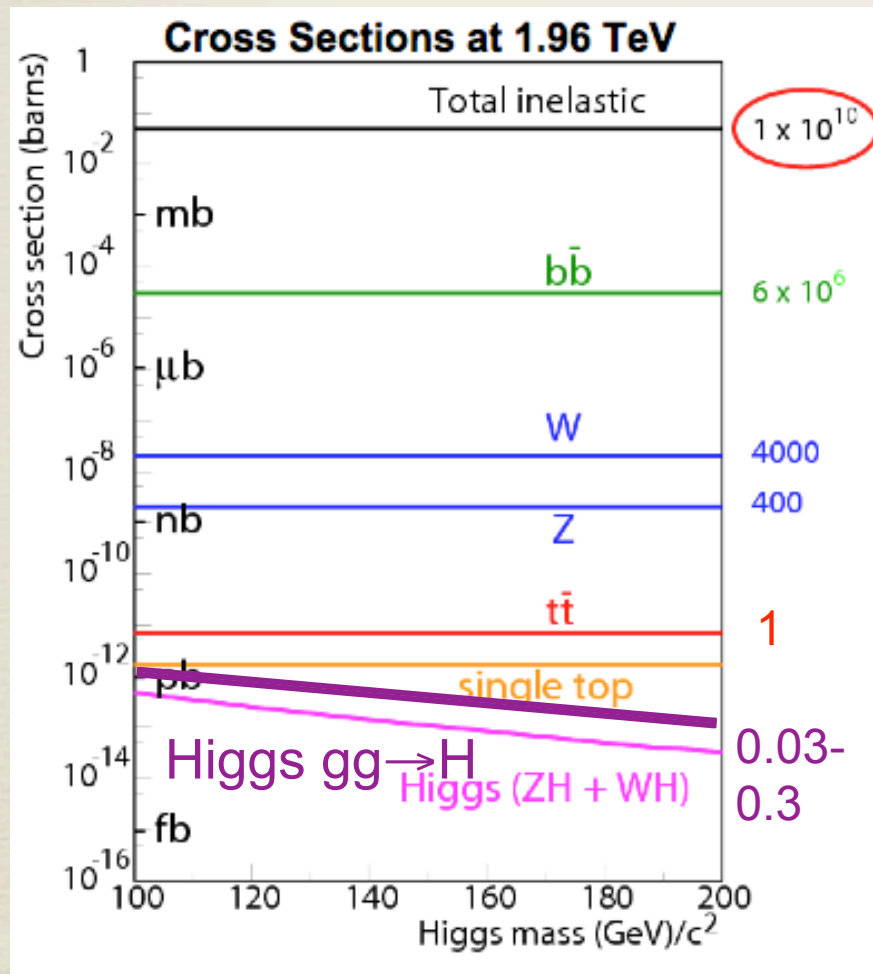


# **Searches at the Tevatron and LHC**



# Tevatron analysis overview

- \* Inclusive  $gg \rightarrow h \rightarrow bb$  not feasible at low masses
- \* WBF only slightly adds to analyses designed for other channels

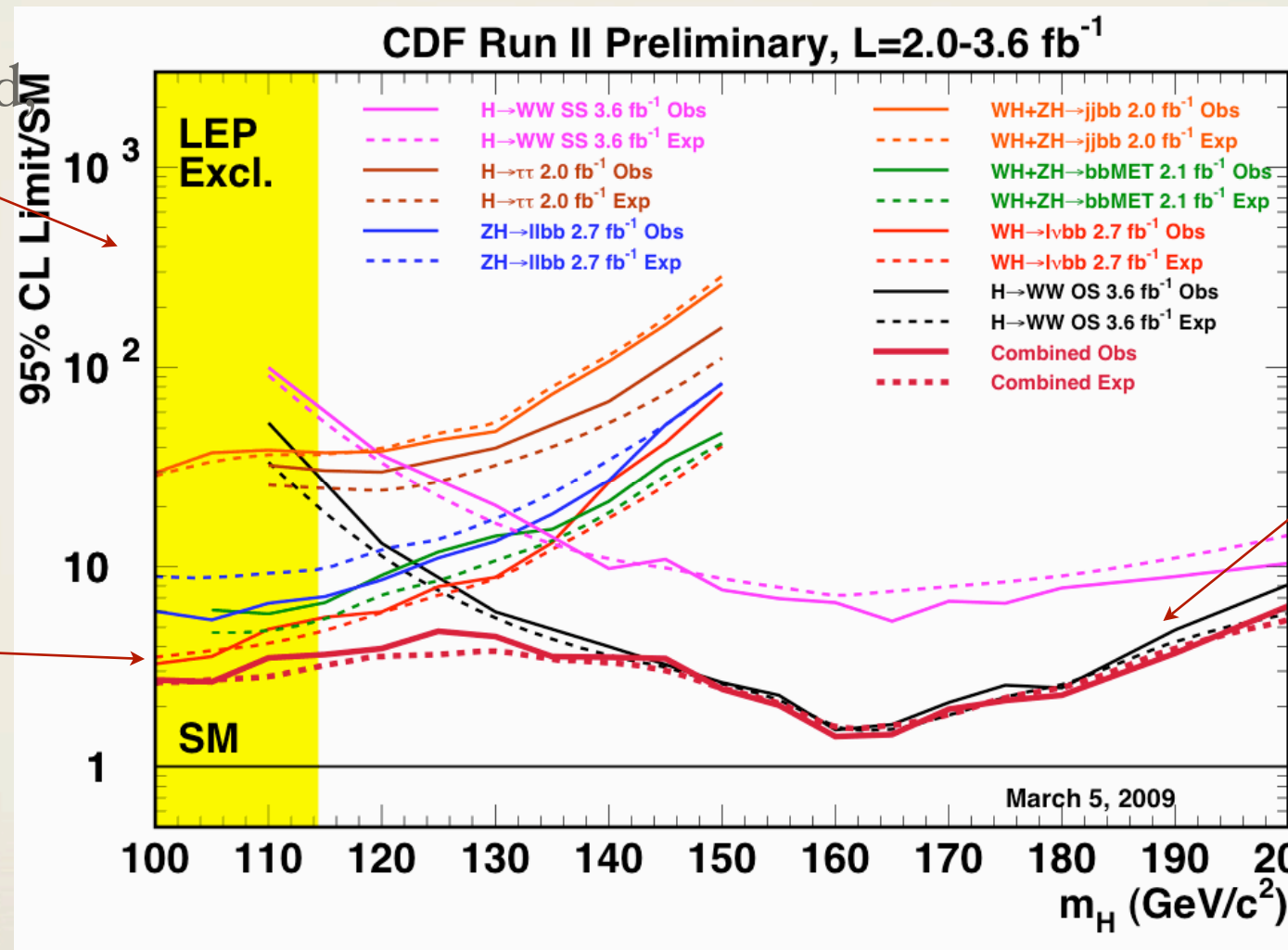




# Combined exclusion limit

- \* No observation, so collaborations report 95% C.L. exclusion by combining many possible channels

Cross section excluded normalized to SM

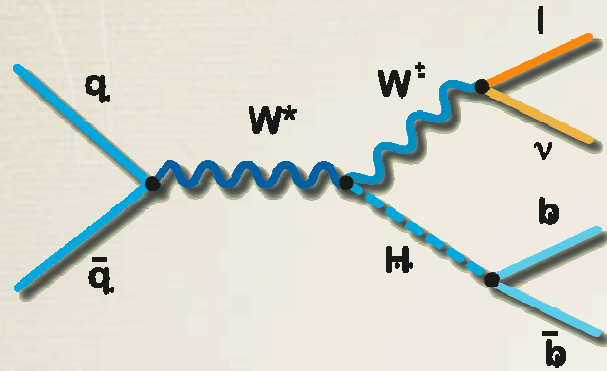


Most sensitive:  
Wh→lvbb

At high mass, all sensitivity from H→WW



# Wh → lvbb analysis



Basic acceptance cuts :

- $p_T^l > 20 \text{ GeV}$
- $\cancel{E}_T > 20 \text{ GeV}$
- 2-3 jets, 1-2 b-tags
- $p_T^j > 20 \text{ GeV}$

Process	1 tag	2 tags
All Pretag Cands.	50644.0 ± 0.0	57174.0 ± 0.0
WW	56.2 ± 6.2	0.4 ± 0.1
WZ	23.0 ± 1.7	4.8 ± 0.5
ZZ	0.8 ± 0.1	0.2 ± 0.0
TopLJ	121.3 ± 17.1	23.8 ± 3.9
TopDil	48.8 ± 6.8	14.1 ± 2.3
STopT	64.0 ± 9.3	1.8 ± 0.3
STopS	40.6 ± 5.7	12.8 ± 2.1
Z+jets	37.4 ± 5.5	2.1 ± 0.3
Total MC	392.0 ± 35.0	59.9 ± 7.5
Wbb	538.7 ± 162.5	70.3 ± 22.5
Wcc/Wc	489.1 ± 150.9	6.8 ± 2.3
Total HF	1027.8 ± 312.3	77.1 ± 24.7
Mistags	458.0 ± 57.9	2.2 ± 0.6
Non-W	135.5 ± 54.2	9.0 ± 3.6
Total Prediction	2013.3 ± 324.1	148.2 ± 26.1
WH100	9.5 ± 0.8	2.9 ± 0.3
WH105	8.6 ± 0.7	2.7 ± 0.3
WH110	7.6 ± 0.6	2.4 ± 0.3
WH115	6.3 ± 0.5	2.0 ± 0.2
WH120	4.9 ± 0.4	1.6 ± 0.2
WH125	4.0 ± 0.3	1.3 ± 0.2
WH130	3.1 ± 0.3	1.0 ± 0.1
WH135	2.3 ± 0.2	0.7 ± 0.1
WH140	1.5 ± 0.1	0.5 ± 0.1
WH145	1.0 ± 0.1	0.3 ± 0.0
WH150	0.7 ± 0.1	0.2 ± 0.0
Observed	1998.0 ± 0.0	156.0 ± 0.0

“Estimating the background contribution after applying the event selection to the WH candidate sample is an elaborate process”

W+jets: normalization from data; heavy-flavor fraction from ALPGEN for shape (tree-level)+data for norm.; Do also uses NLO to check

Combined theory +experiment error

From CDF, after event selection



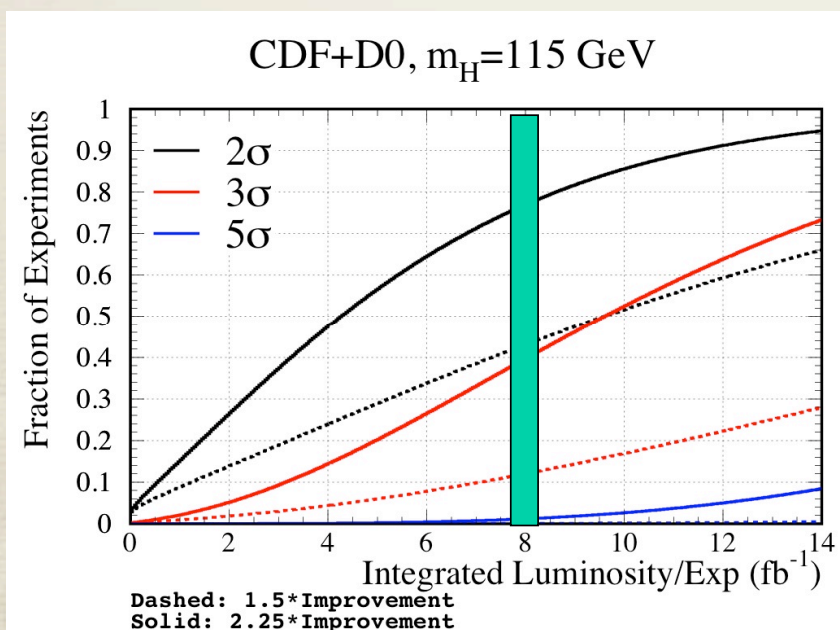
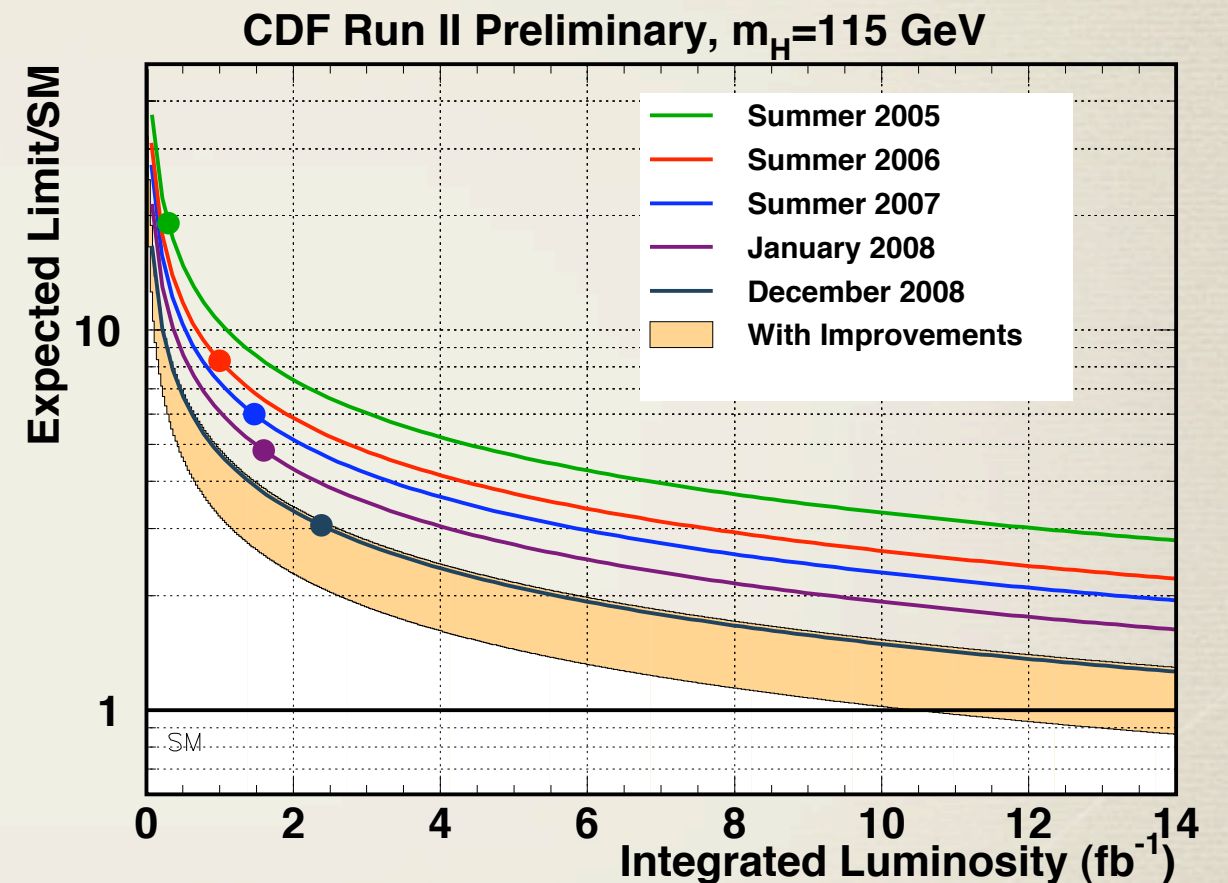
# Low-mass limits and projections

- \* Analysis improvements expected: better dijet mass resolution, increased acceptance

Results at  $m_H = 115\text{GeV}$ : 95%CL Limits/SM

Analysis	Lum ( $\text{fb}^{-1}$ )	Higgs Events	Exp. Limit	Obs. Limit
CDF NN+ME+BDT	2.7	8.4	4.8	5.8
DØ ME+NN <b>new</b>	2.7	13.3	6.7	6.4

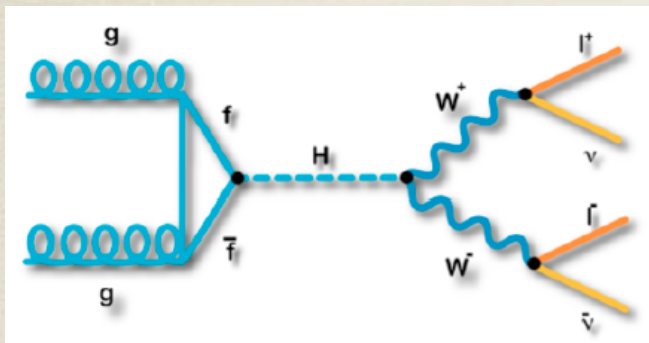
from M. Herndon, LoopFest 2009



Likely to have exclusion, possibility of  $3\sigma$  at low mass (depends on Nature...)



# $h \rightarrow WW \rightarrow l\nu l\nu$



from Do

	$ee$ pre-selection	$ee$ final	$e\mu$ pre-selection	$e\mu$ final
$Z \rightarrow ee$	$218695 \pm 704$	$108 \pm 14$	$280.6 \pm 3.3$	$0.0^{+0.1}_{-0.0}$
$Z \rightarrow \mu\mu$	—	—	$274.6 \pm 0.9$	$5.8 \pm 0.1$
$Z \rightarrow \tau\tau$	$1135 \pm 16$	$1.4 \pm 0.5$	$3260 \pm 3$	$7.3 \pm 0.1$
$t\bar{t}$	$131.4 \pm 1.4$	$39.9 \pm 0.8$	$272.0 \pm 0.3$	$82.5 \pm 0.2$
$W$ +jets	$241 \pm 5$	$98 \pm 3$	$183 \pm 4$	$78.6 \pm 2.8$
$WW$	$172.2 \pm 2.6$	$66.8 \pm 1.6$	$421.2 \pm 0.1$	$154.7 \pm 0.1$
$WZ$	$112.5 \pm 0.2$	$9.68 \pm 0.05$	$20.5 \pm 0.1$	$6.6 \pm 0.1$
$ZZ$	$98.2 \pm 0.2$	$7.68 \pm 0.07$	$5.3 \pm 0.1$	$0.60 \pm 0.01$
Multijet	$1351 \pm 55$	$1.7^{+2.0}_{-1.7}$	$279 \pm 168$	$1.1^{+9.6}_{-1.1}$
Signal ( $M_H = 165$ GeV)	$9.45 \pm 0.01$	$6.13 \pm 0.01$	$17.1 \pm 0.01$	$12.2 \pm 0.1$
Total Background	$221937 \pm 707$	$332 \pm 15$	$4995 \pm 168$	$337 \pm 10$
Data	221530	336	4995	329

Basic acceptance cuts (CDF) :

- $p_T^{l1} > 20$  GeV
- $p_T^{l2} > 10$  GeV
- $\cancel{E}_T > 15 - 25$  GeV  
(for various final states)
- Look separately at 0,1,2+ jet bins

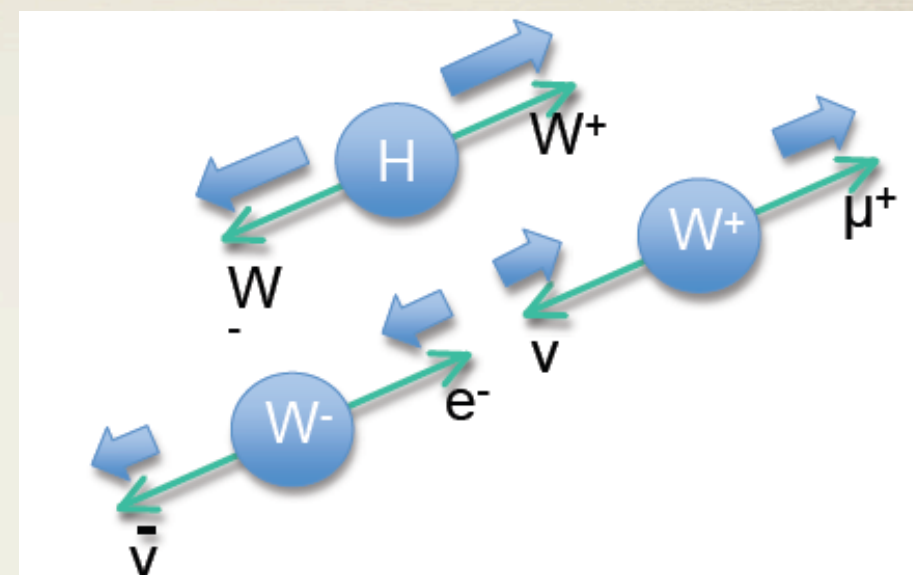
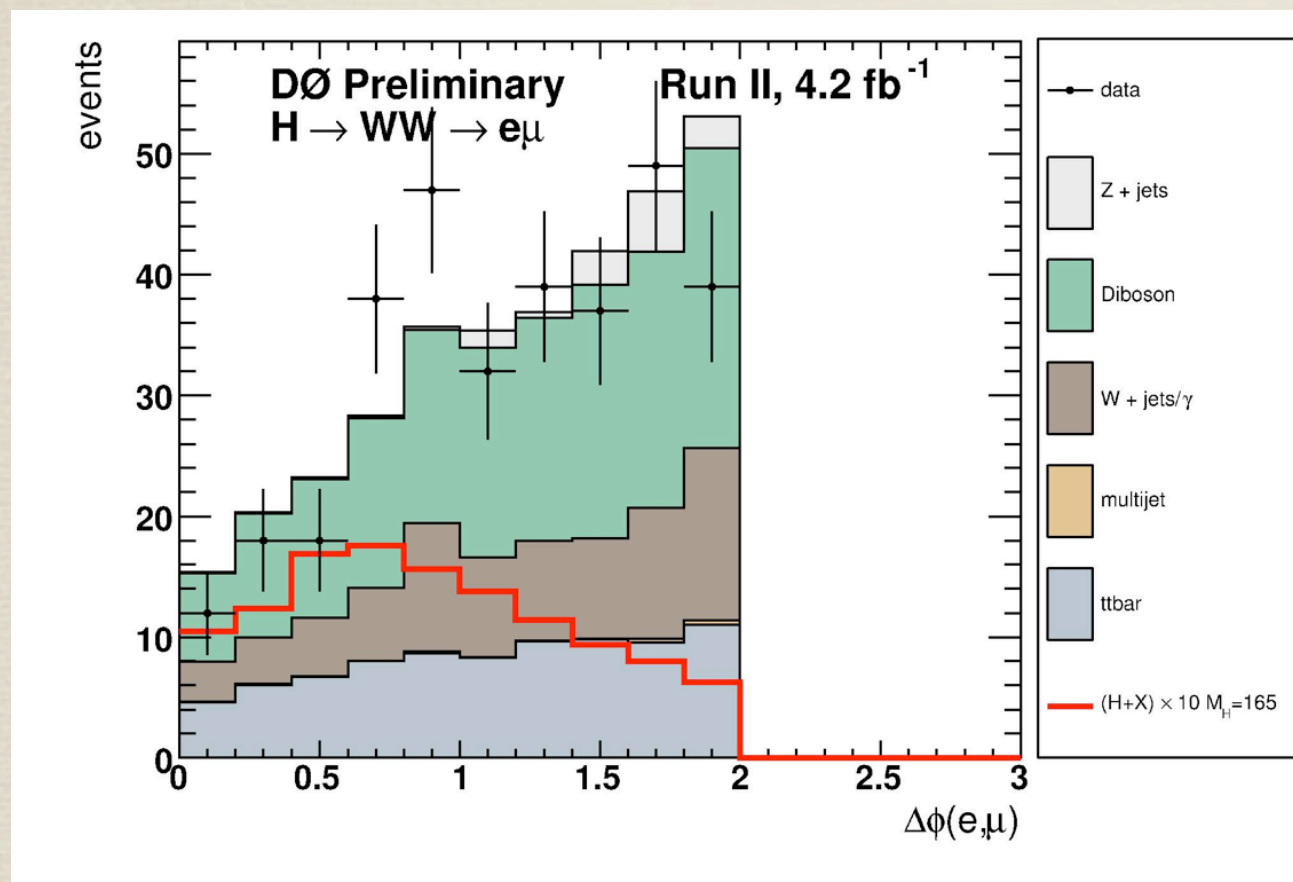
$t\bar{t}$ : affects 2-jet bin; taken from NLO calculations

$W$ +jets: jet fakes lepton; from data-driven methods

$WW$ : taken from NLO calculation

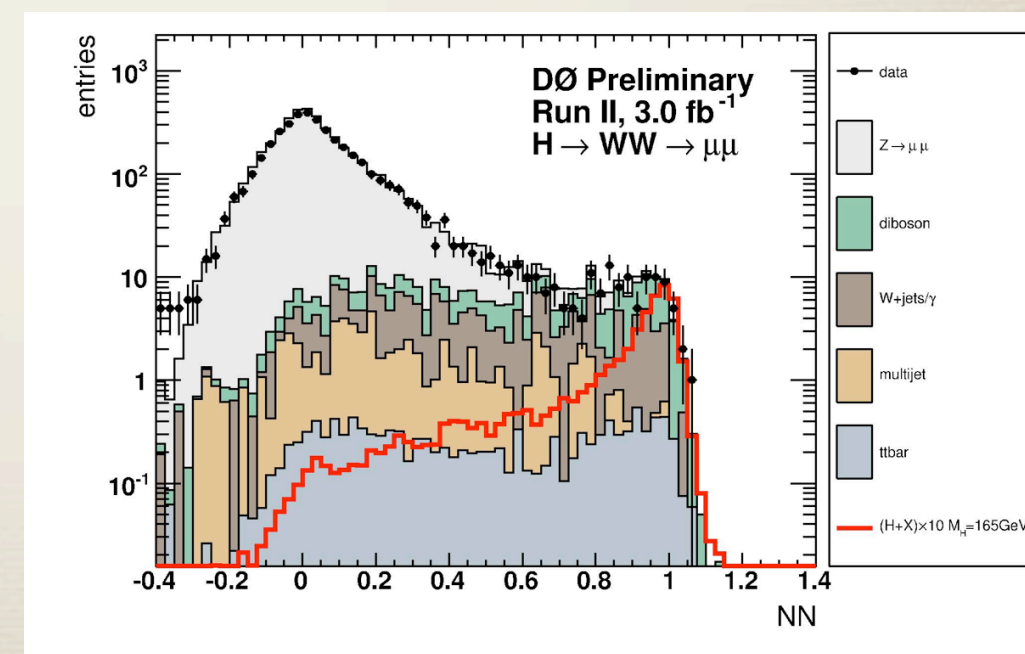


# Kinematic discriminants



A primary handle for o-jet bin:  $\Delta\phi_{ll}$   
Spin correlation: leptons in same direction

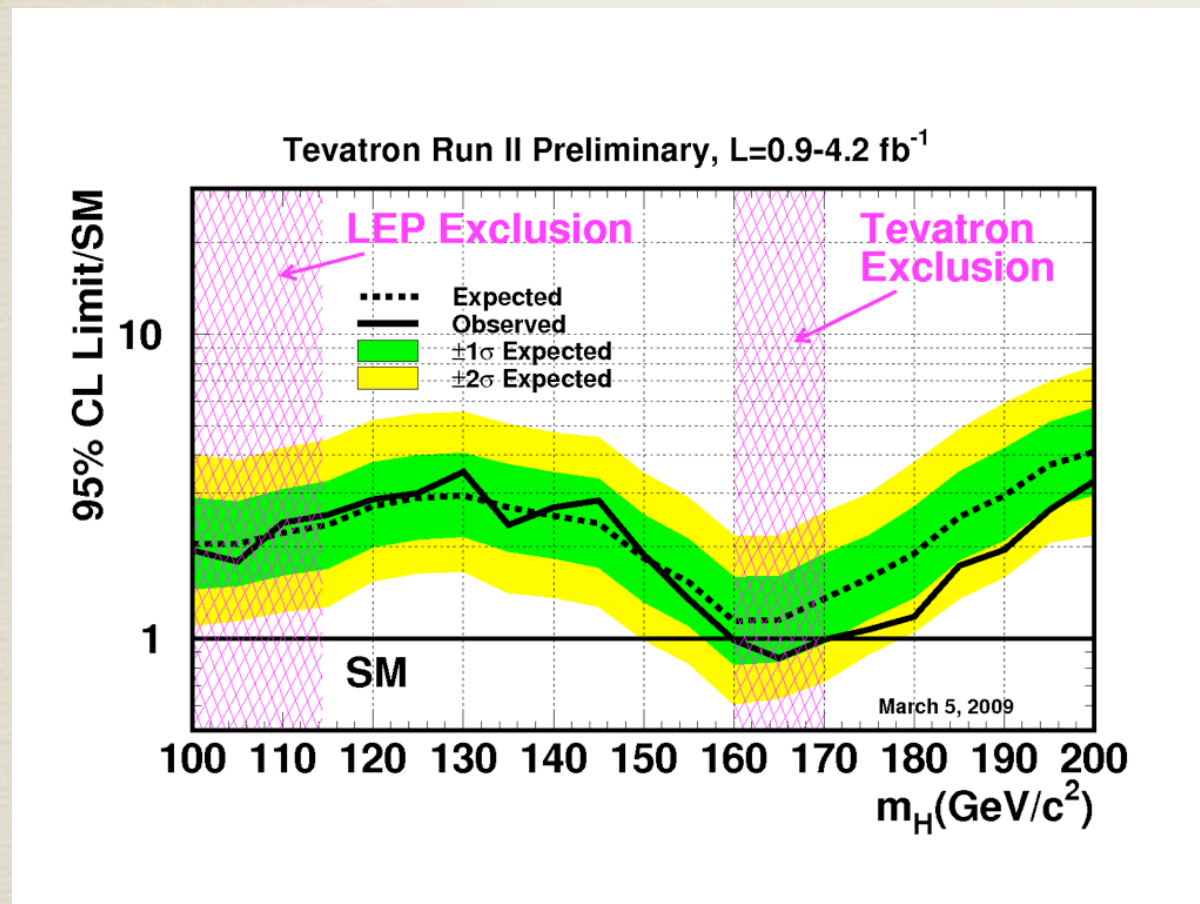
NN Analysis Variables	
$p_T$ of leading lepton	$p_T(\ell_1)$
$p_T$ of trailing lepton	$p_T(\ell_2)$
Minimum of both lepton qualities	$\min(q_{\ell_1}, q_{\ell_2})$
Vector sum of the transverse momenta of the leptons:	$p_T(\ell_1) + p_T(\ell_2)$
Scalar sum of the transverse momenta of the jets:	$H_T = \sum_i  p_T(\text{jet}_i) $
Invariant mass of both leptons	$M_{\text{inv}}(\ell_1, \ell_2)$
Minimal transverse mass of one lepton and $\cancel{E}_T$	$M_T^{\text{min}}$
Missing transverse energy	$\cancel{E}_T$
Scalar transverse energy	$E_T^{\text{scalar}}$
Azimuthal angle between selected leptons	$\Delta\phi(\ell_1, \ell_2)$
Solid angle between selected leptons ( $e\mu$ only)	$\Delta\Theta(\ell_1, \ell_2)$
$\Delta R$ between selected leptons ( $e\mu$ only)	$\Delta R(\ell_1, \ell_2)$
Azimuthal angle between leading lepton and $\cancel{E}_T$	$\Delta\phi(\cancel{E}_T, \ell_1)$
Azimuthal angle between trailing lepton and $\cancel{E}_T$	$\Delta\phi(\cancel{E}_T, \ell_2)$





# High-mass exclusion

\* Combine CDF+Do exclusion limits:  $160 \leq M_H \leq 170$  GeV at 95% CL



	95%CL Limits/SM				
M Higgs(GeV)	155	160	165	170	175
Method 1: Exp	1.5	1.1	1.1	1.4	1.6
Method 1: Obs	1.4	0.99	0.86	0.99	1.1
Method 2: Exp	1.5	1.1	1.1	1.3	1.6
Method 2: Obs	1.3	0.95	0.81	0.92	1.1

Solidly exclude SM at 165 GeV

0 Jet Uncertainties	$gg \rightarrow H$
<b>Cross Section</b>	
Scale	10.9%
PDF Model	5.1%
Total	12.0%

→ These are some of the largest systematics in the analysis; detailed QCD study crucial to perform this search!

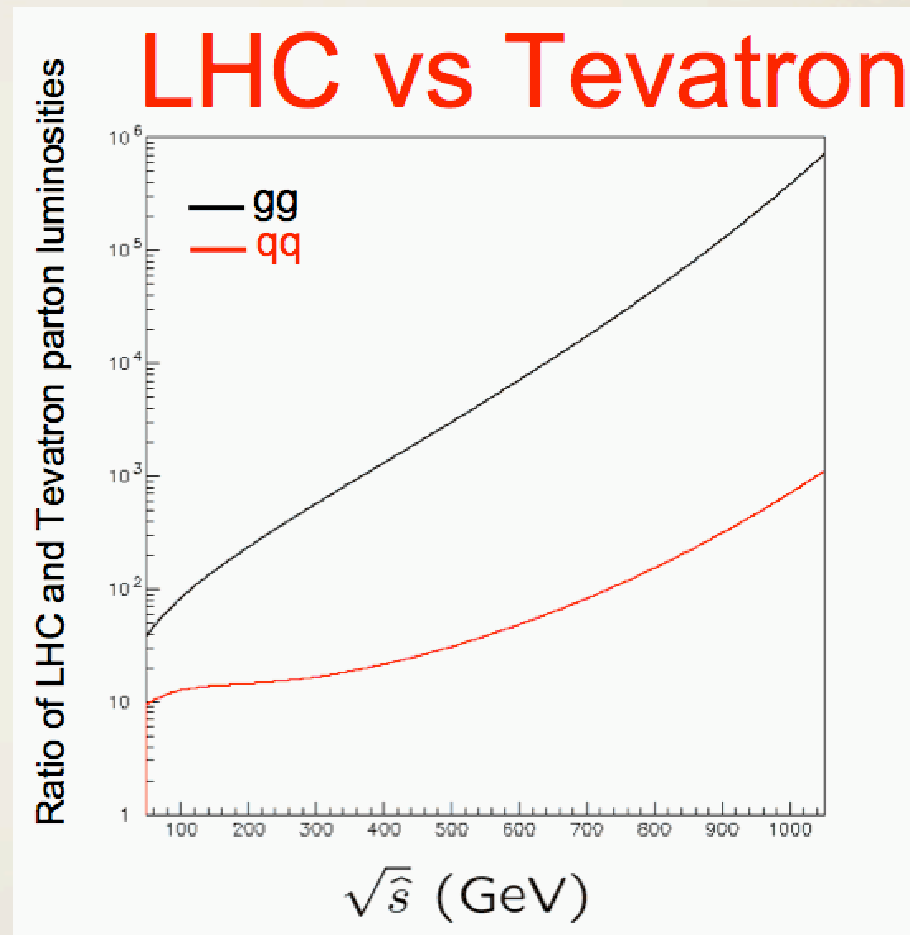
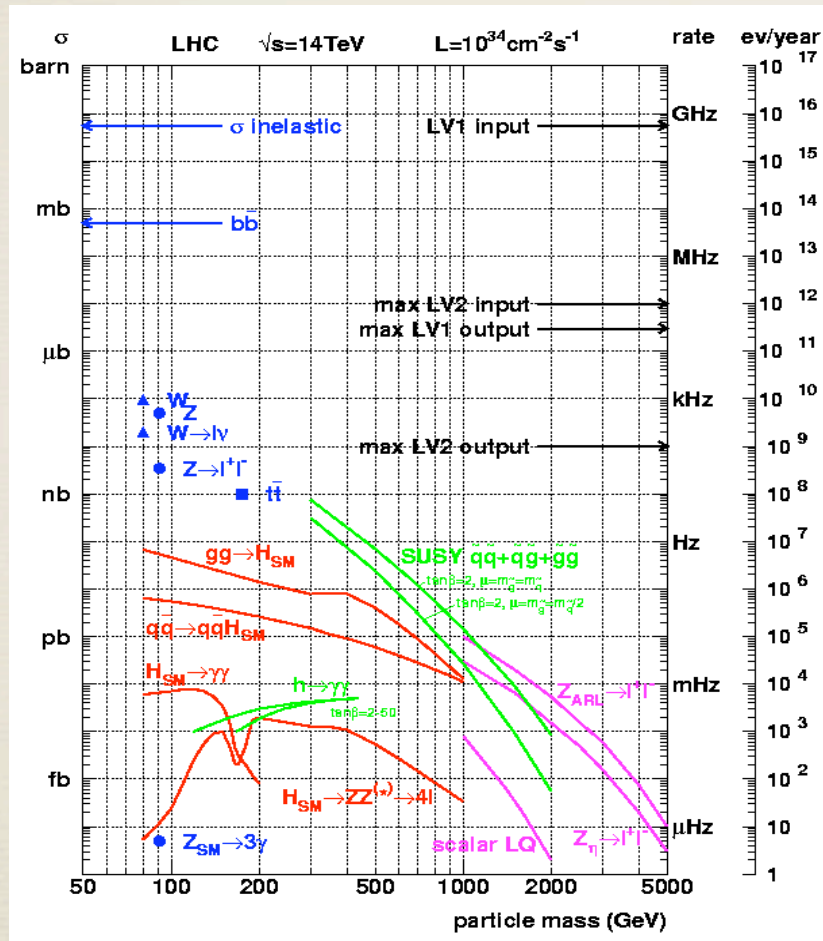


# LHC physics overview

\* Qualitative change; gluons now overwhelm scattering rate

Background

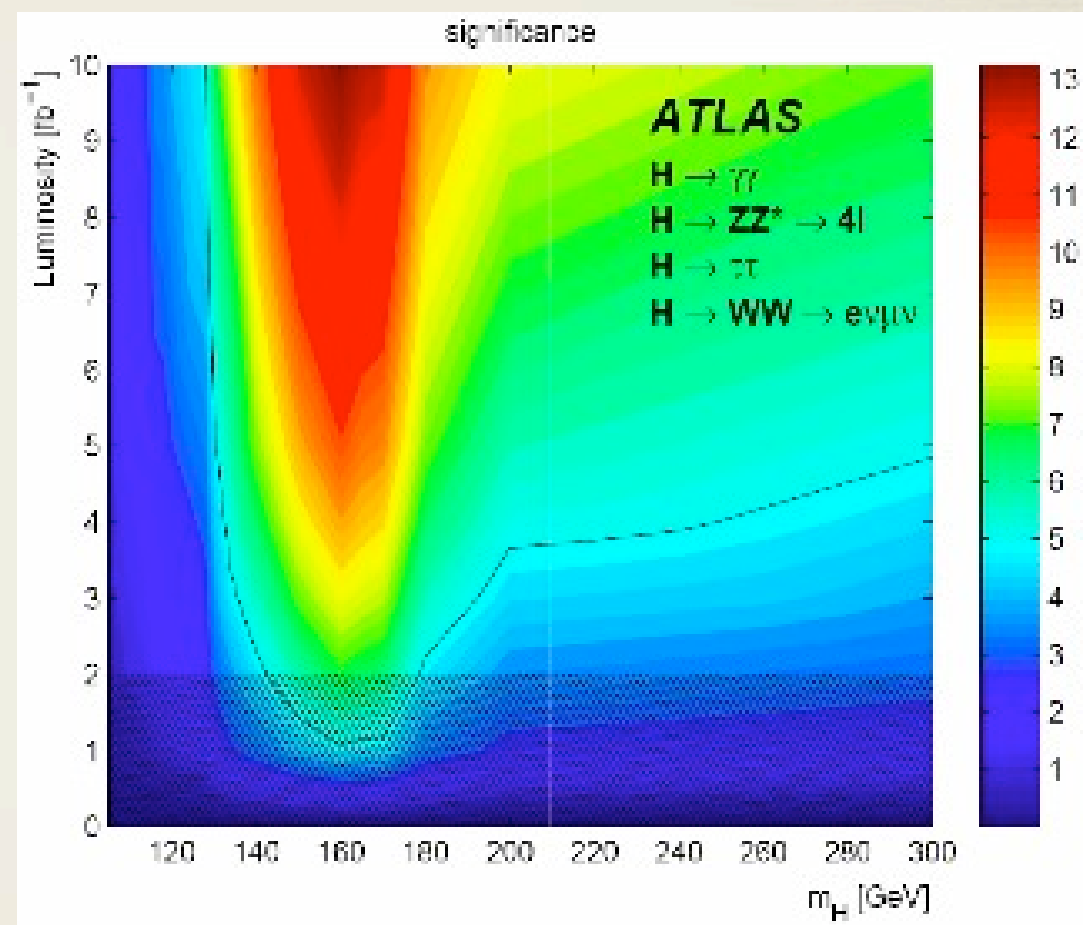
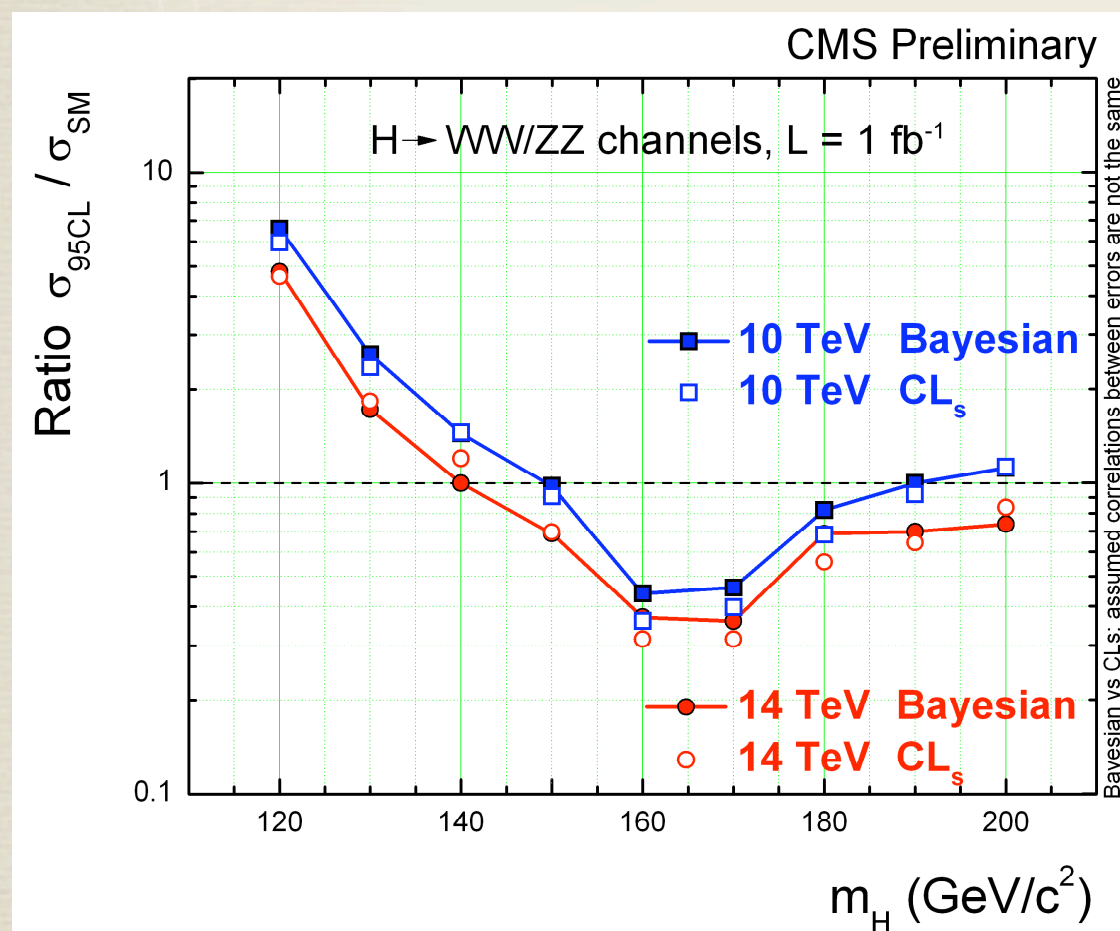
Higgs





# LHC summary: low $\text{fb}^{-1}$

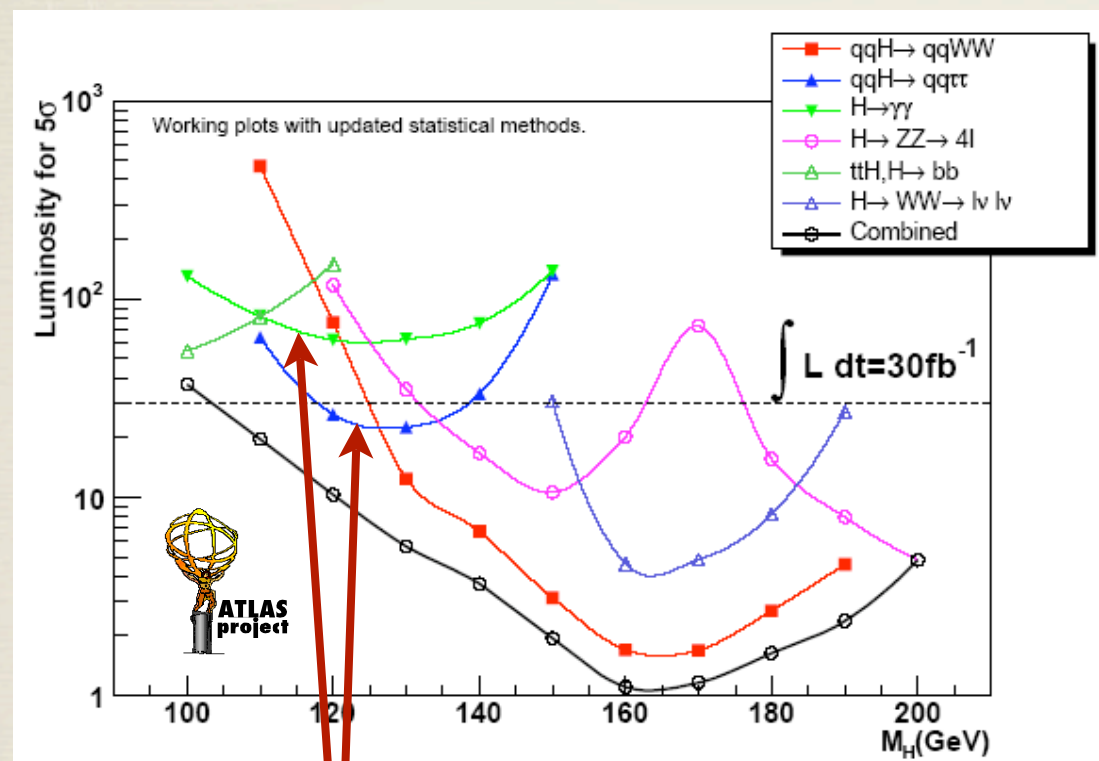
\* Will reproduce expected Tevatron exclusion with  $1 \text{ fb}^{-1}$





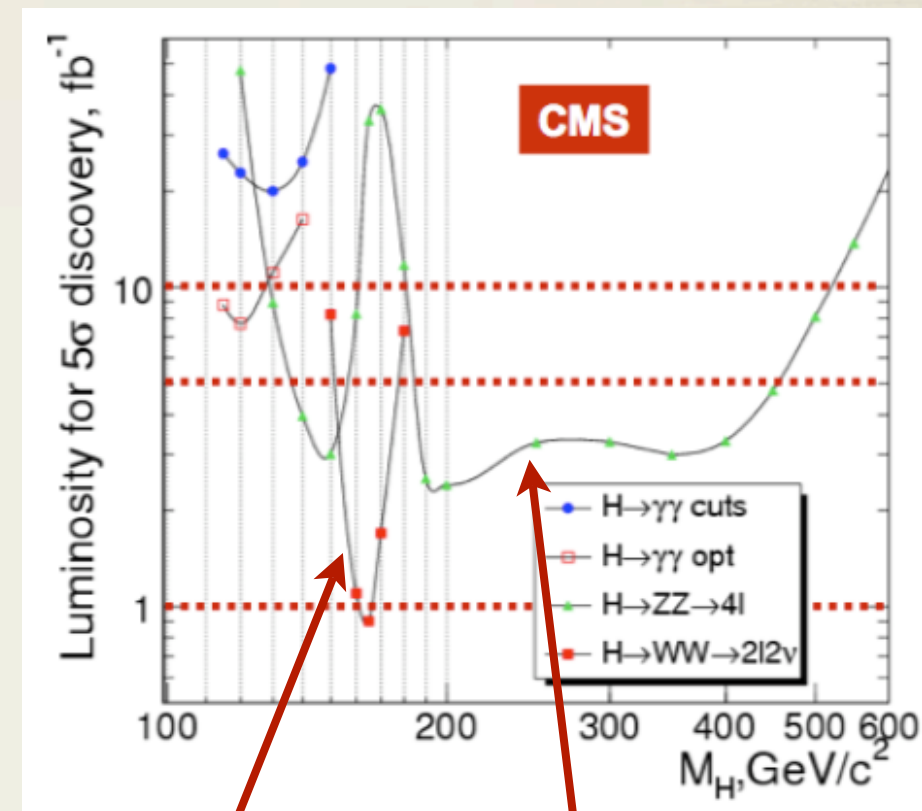
# LHC summary: high $\text{fb}^{-1}$

\* Entire mass range covered, much with multiple modes



$h \rightarrow \gamma\gamma$ , WBF  $h \rightarrow \tau\tau$  cover low mass range

$M_H > 200 \text{ GeV}$ : only few  $\text{fb}^{-1}$   
 $M_H < 120 \text{ GeV}$ : 20-30  $\text{fb}^{-1}$



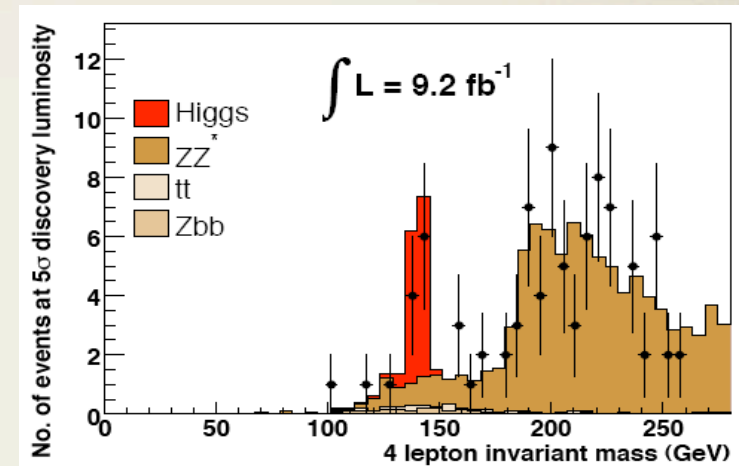
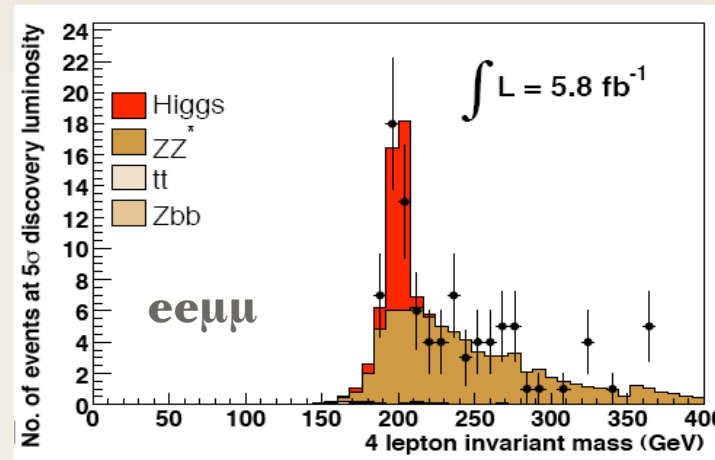
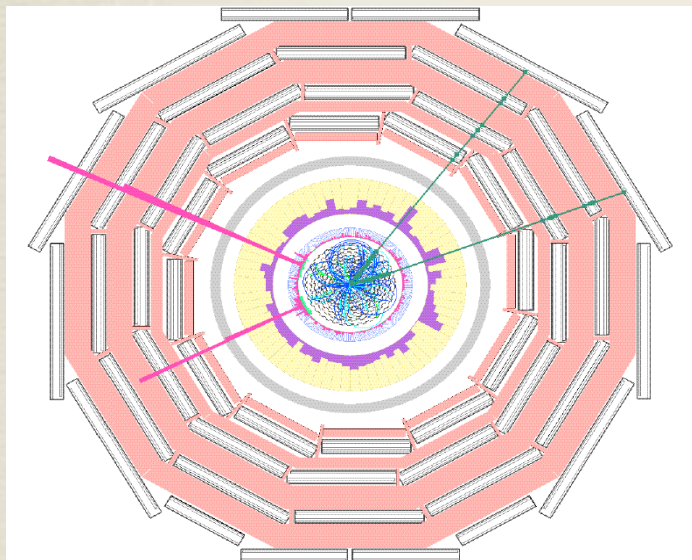
$h \rightarrow ZZ \rightarrow 4l$  assures discovery over entire high-mass range

$h \rightarrow WW \rightarrow l\nu l\nu$  again important at LHC



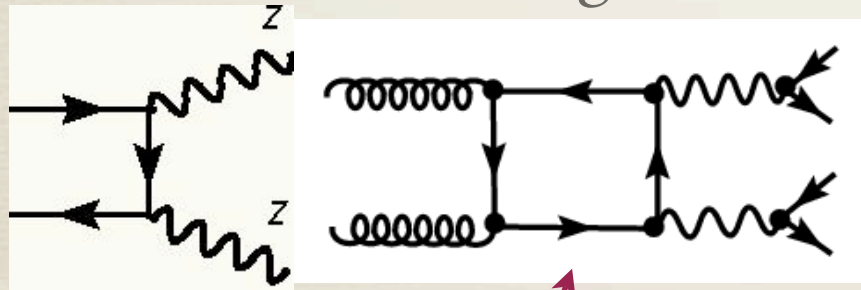
$$h \rightarrow ZZ \rightarrow l_1 l_1 l_2 l_2$$

- \* Trigger: one  $p_T > 20-25$  GeV or two  $p_T > 10-15$  GeV leptons
- Reconstruct: at least one  $Z \rightarrow ll$  decay

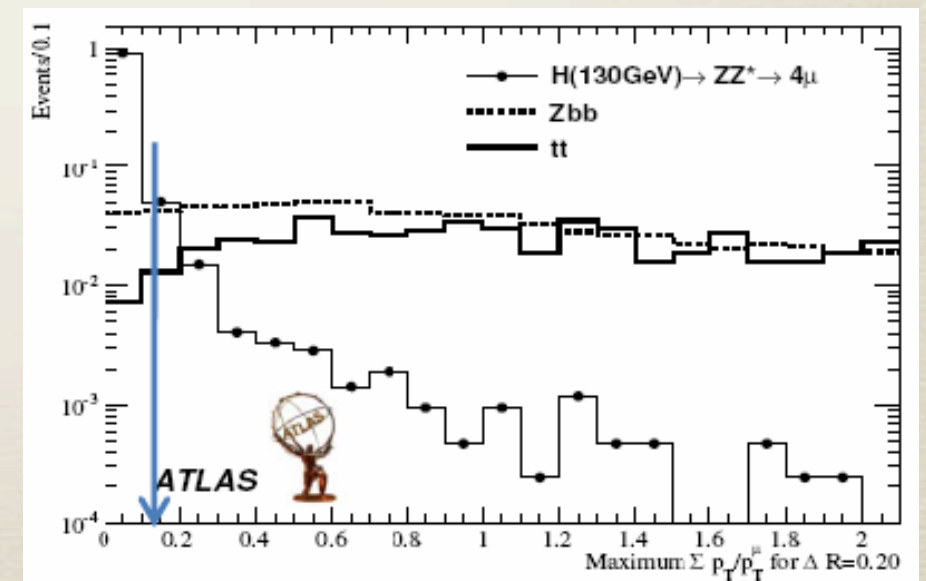
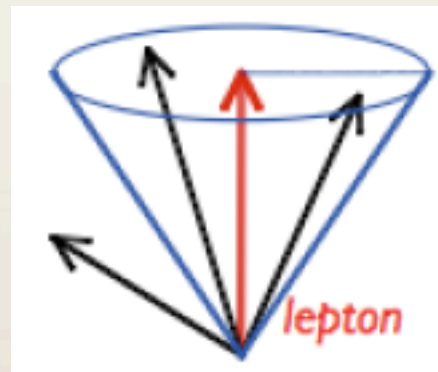


Reducible:  $tt \rightarrow ll\nu bb$ ,  $Zbb$  with semi-leptonic b-decay

Irreducible backgrounds:



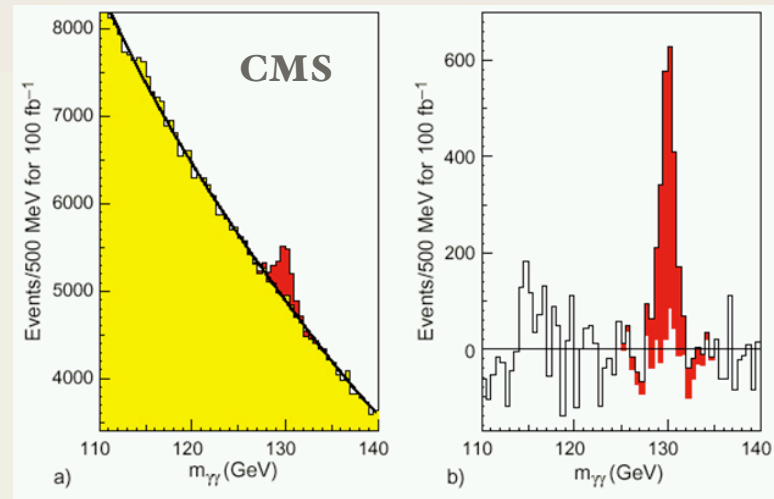
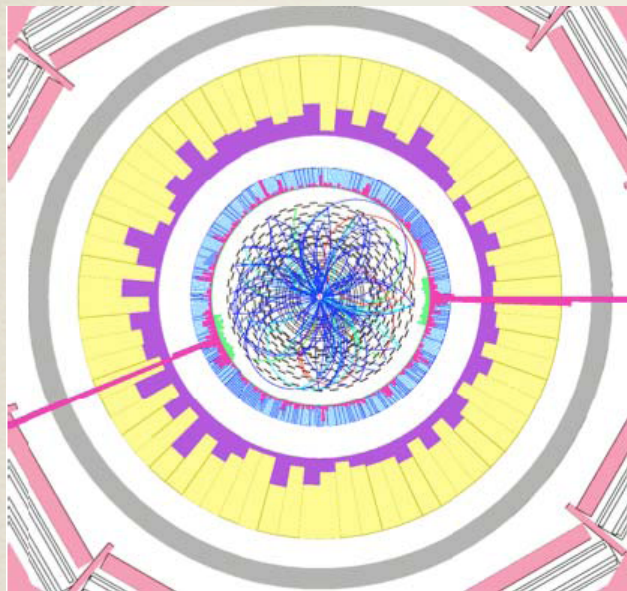
Formally NNLO, but enhanced by gg luminosity





$$h \rightarrow \gamma\gamma$$

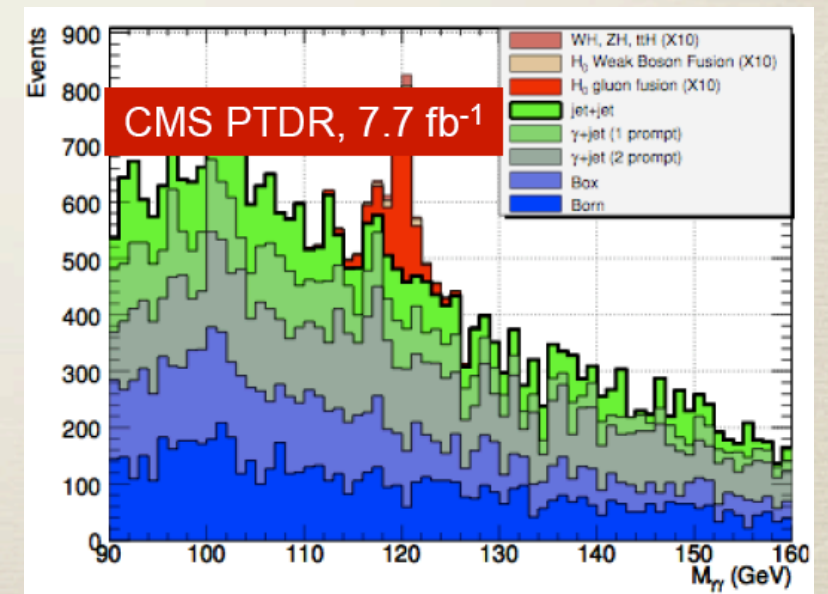
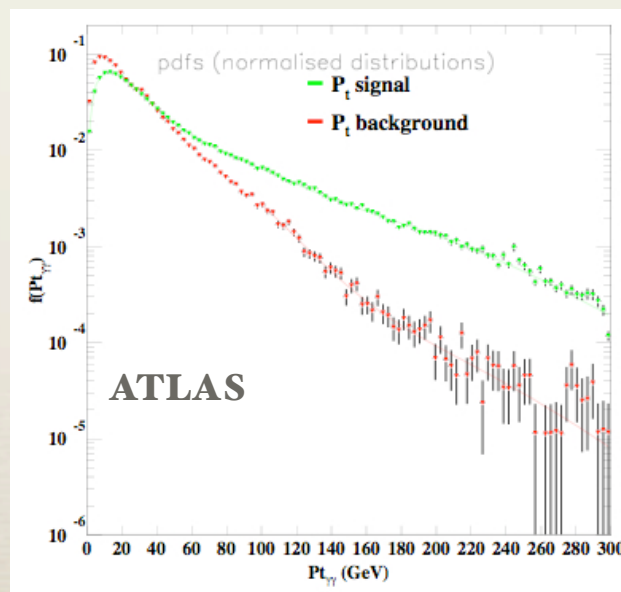
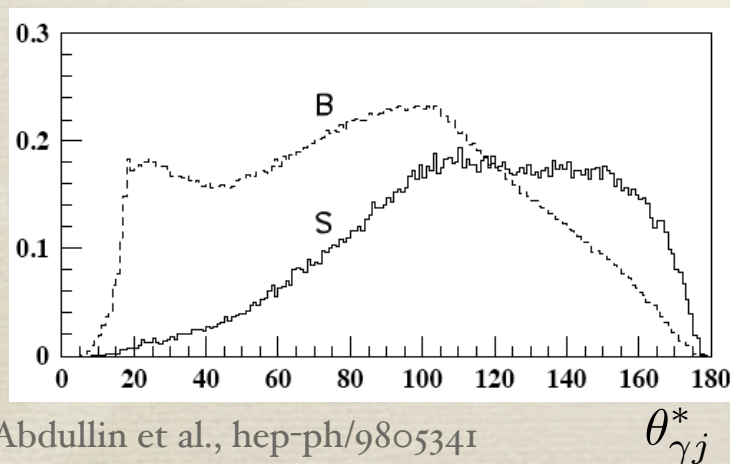
- \* Trigger: 1-2 photons; Reconstruct:  $p_T > 40$  GeV,  $p_T > 25$  GeV  
Excellent EM calorimeter resolution; calibrate with  $Z \rightarrow ee$



Huge  $\pi^0 \rightarrow \gamma\gamma$  background; measure from sideband

$5\sigma$ : 20-30  $\text{fb}^{-1}$  for  $M_H < 140$  GeV

Additional handles with jets; consider  $\gamma\gamma + j, 2j$

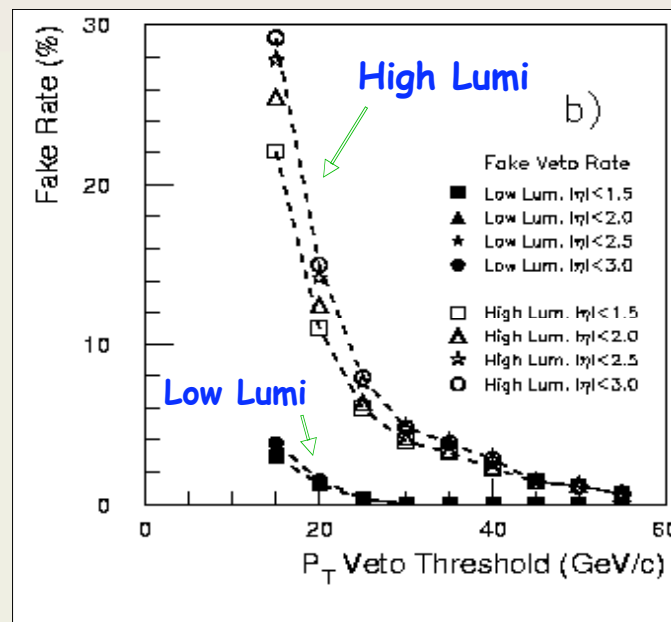
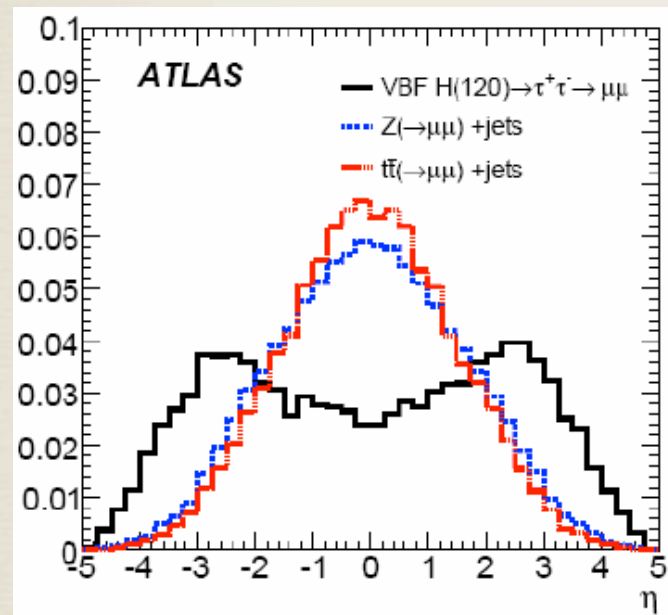


Nisati, KITP '08



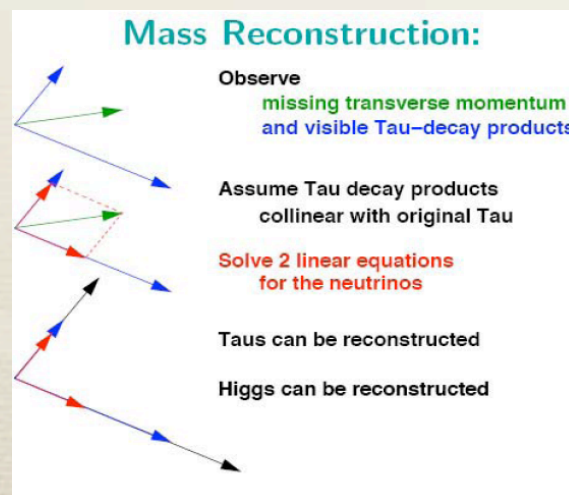
# WBF $h \rightarrow \tau\tau$

- \* Two tagging jets:  $E_T > 40$  GeV,  $\eta_{jj} > 4$ ,  $M_{jj} > 500-1000$  GeV
- Higgs decay products between tagging jets; central-jet veto
- $\tau\tau \rightarrow ll$ ,  $lh$  modes possible

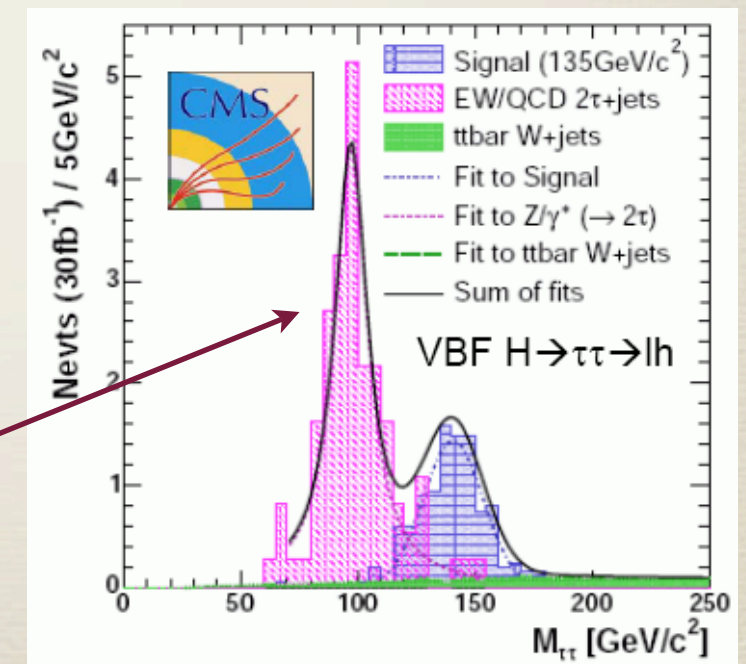


Central-jet veto a concern at high luminosities

Collinear approximation for  $\tau$ 's (highly boosted):



Data-driven techniques to control  $Z \rightarrow \tau\tau$  line-shape





# Global analysis of couplings

- \* Observe Higgs in many modes: gluon-fusion, WBF, W/Z+h (not discovery at LHC, but after  $M_H$  known Butterworth et al., 0802.2470

$$\sigma_p \times BR(h \rightarrow xx) = \underbrace{\left(\frac{\sigma_p}{\Gamma_p}\right)_{SM}}_{\text{NP effects cancel, calculate}} \times \underbrace{\frac{\Gamma_p \Gamma_x}{\Gamma}}_{\text{measure}}$$

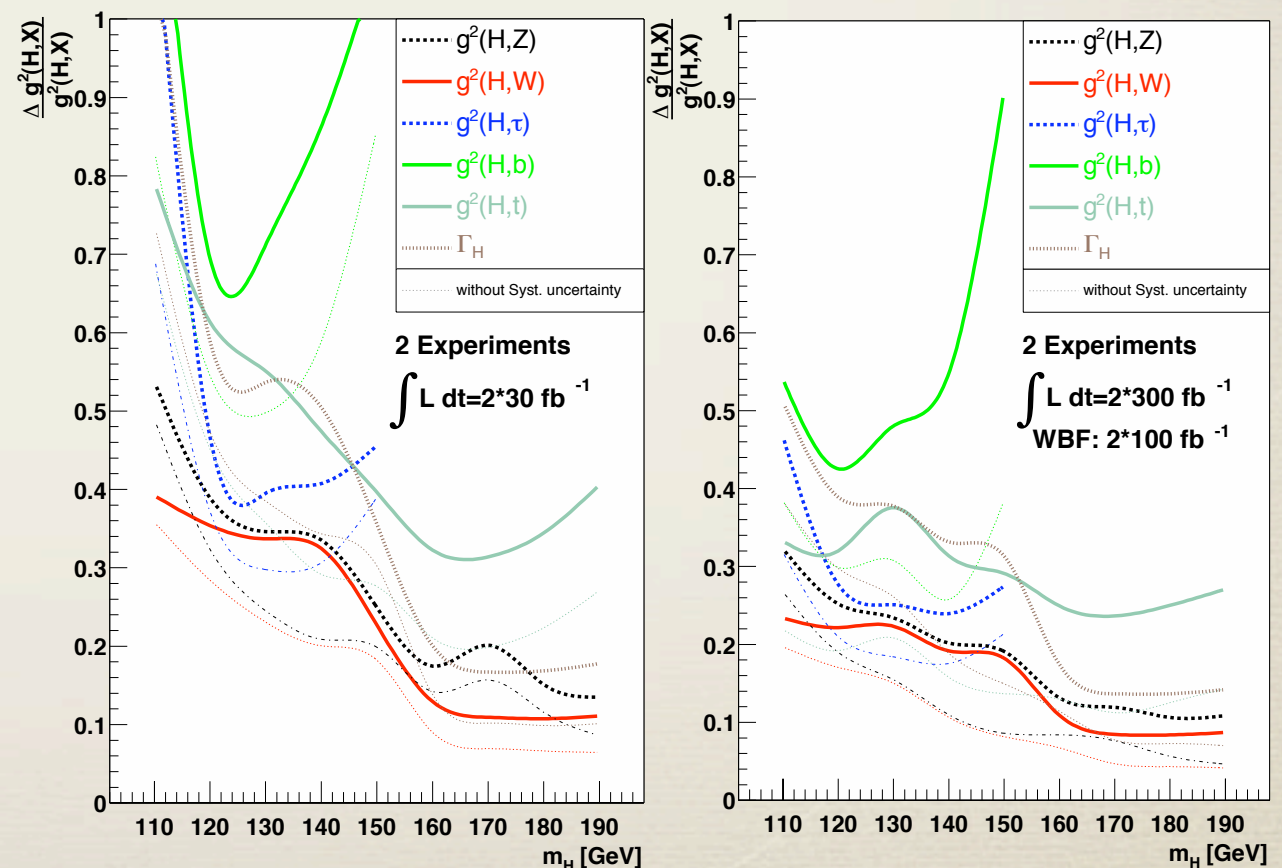
Scaling degeneracy if total width unknown:

$$\Gamma_i \rightarrow f \Gamma_i, \Gamma \rightarrow f^2 \Gamma$$

Mild assumption:  $g_{hVV}^2 < 1.05 \times g_{hVV,SM}^2$

Allows any # of scalar doublets, new particles in loops, small contributions of scalar triplets

⇒ Assumption+VBF measurement of  $(\Gamma_V)^2/\Gamma$  breaks degeneracy





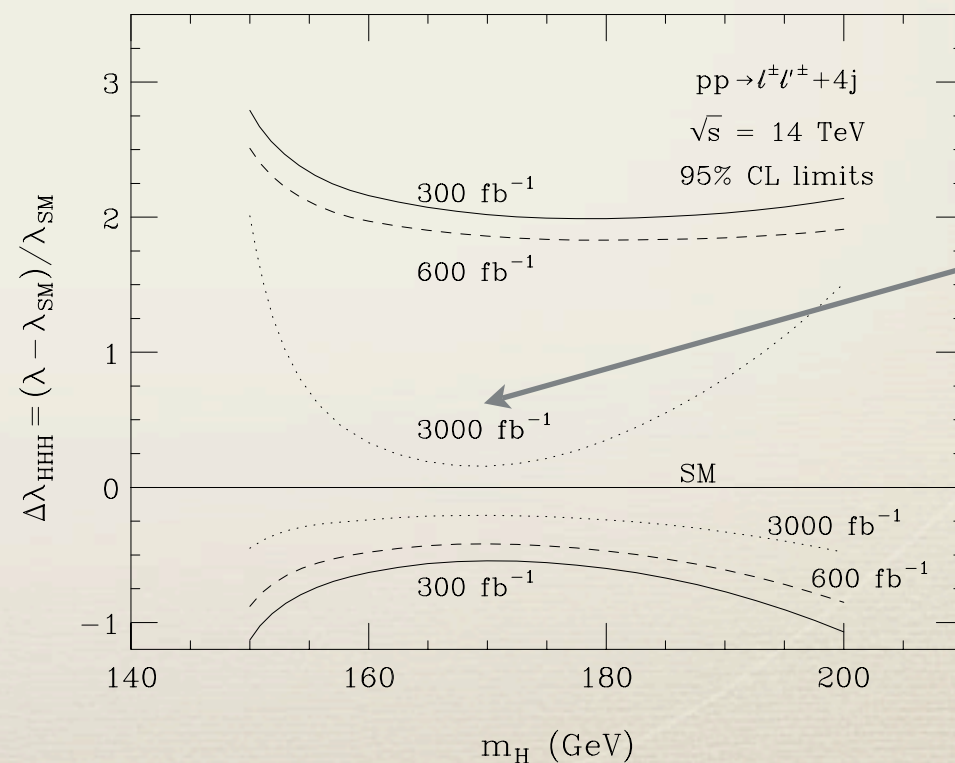
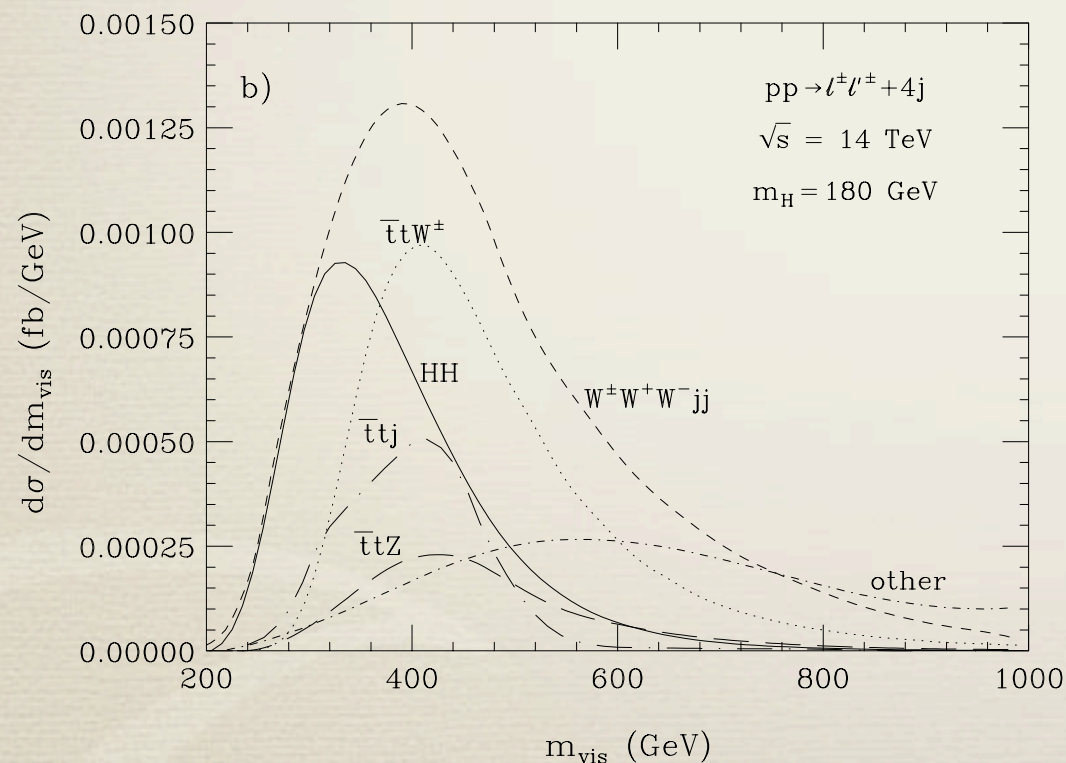
# Measuring the Higgs potential

\* Form of SM Higgs potential makes definite predictions

$$V(H) = \lambda \left( H^\dagger H - \frac{v^2}{2} \right)^2$$

$$\Rightarrow g_{hhh} = 3M_H^2/v$$

Probe in  $gg \rightarrow hh \rightarrow W^+W^-W^+W^- \rightarrow l+l'+4j + \text{missing } p_T$   
(one possible final state)



super-LHC  
luminosity  
upgrade  
required



# Conclusions

- \* We must find a Higgs boson or something else which consistently breaks EW symmetry
- \* Phenomenology of Higgs intricate and highly dependent on its mass; detailed experimental program needed to find it
- \* Very sensitive to quantum effects; better have a good handle on QCD!
- \* Tevatron beginning to reach into allowed SM mass region; LHC will pick up the search later this year
- \* Potential to determine whether the Higgs is SM or not with LHC measurements