Physics Beyond the Standard Model

— Signals at Colliders

Tao Han Univ. of Wisconsin - Madison

CTEQ Summer School, Puebla, Mexico (May 26, 27, 2005) Physics Beyond the Standard Model

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The Standard Model and the Need For Going Beyond Our "Theory Bank" New Physics Signals at Hadron Colliders Physics Beyond the Standard Model

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The Standard Model and the Need For Going Beyond Our "Theory Bank" New Physics Signals at Hadron Colliders

> Higgs bosons SUSY particles New gauge bosons New heavy fermions Extra dimensions

## The Standard Model

### as a Low-Energy Effective Theory

•  $SU_c(3)$  QCD as the theory of strong interactions:







QCD remarkably successfful: Perturbative QCD well tested and formed foundation for HEP; Significant progress in lattice gauge calculatioins. •  $SU_L(2) \otimes U_Y(1)$  EW theory and precision measurements:





•  $SU_L(2) \otimes U_Y(1)$  EW theory and precision measurements:



EW precision data:  $m_H < 251$  GeV at 95% CL with  $m_t = 178$  GeV.





All couplings  $g_{2,3}$ ,  $\sin^2 \theta_W$ ,  $g_f$  and masses  $\sim g_i v$  are in place. SM with a light H could be an *effective theory* to  $\Lambda \sim M_{pl}$ .

- a stable vacuum; non-trivial interactions;
- renormalizability ...

Q: Would you need physics beyond the Standard Model? A: ... ...



(The Garden of Aden)

## The Need For Going Beyond SM ?

Mass Spectrum in a Wide Range:



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### Mass Spectrum in a Wide Range:



EW scale:  $v \approx \mathcal{O}(1 \text{ TeV})$ ;  $m_{\nu} : 10^{-15} \text{ down } ? M_{pl} : 10^{15} \text{ up } ?.$ 

Vastly Separated Scales for Fundamental Interactions:

• QCD condensate:  $f_{\pi}$ 

At the scale  $\Lambda_{QCD}$ , the interaction becomes non-perturbative:

$$\begin{aligned} \alpha_s(Q^2) &= \frac{1}{b \ln(Q^2/\Lambda^2)} \Rightarrow \Lambda_{QCD} \sim \Lambda \, \exp(-\frac{1}{2b\alpha_s}), \\ f_\pi \propto \langle \bar{q}_L q_R \rangle_0^{1/3} \sim 100 \text{ MeV}. \end{aligned}$$

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Empirically (Fermi's weak interaction) and theoretically (EWSB):

$$v = \frac{1}{(\sqrt{2} \ G_F)^{1/2}} = \frac{2M_W}{g} \approx 250 \ \text{GeV}.$$

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• Quantum Gravity?

$$M_{Pl} = \hbar c / \sqrt{G}_N \approx 10^{19} \text{ GeV}.$$

We have NO clue about it ...

Three fermion generations; Quark small mixing; Neutrino masses and (nearly) maximal mixing; CP violation...

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Gravity and Planck scale physics;

Particle cosmology:

inflation; baryogenesis; dark matter; dark energy ...

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 $\implies$  All indicate the need for physics beyond the SM.

### Our "theory bank"

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(A). Supersymmetry:

Weak scale SUSY stabilizes the hierarchy  $M_W - M_{pl}$ 

$$\Delta m_{H}^{2} \sim (M_{SUSY}^{2} - M_{SM}^{2}) \frac{\lambda_{f}^{2}}{16\pi^{2}} \ln \left(\frac{\Lambda}{M_{SUSY}}\right).$$

if the "soft-SUSY breaking":  $M_{SUSY} \sim \mathcal{O}(M_{SM})$ .

Predict TeV scale new physics: light Higgs bosons  $H^0$ ,  $A^0$ ,  $H^{\pm}$ ; SUSY partners  $\tilde{W}^{\pm}..., \tilde{g}, \tilde{q}, \tilde{l}^{\pm}...$ 

Lead to rich physics at the electroweak scale at colliders; Accommodate SUSY GUTs  $M_{GUT} \sim 5 \times 10^{16}$  GeV.

(B). Dynamical approach for mass generation:

• Technicolor and alike: a lesson from QCD  $SU(N_{TC})$  gauge theory, TC fermions Q = U, D, ...EWSB by TC-fermion condendation at  $\Lambda_{TC}$ :  $v \sim \langle \overline{Q_L} Q_R \rangle^{1/3} \sim 246$  GeV.

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• "Topcolor/Top-seesaw": Top quark special ?  $m_t \approx v/\sqrt{2} = 174$  GeV.

Introducing an additional fermion pair  $\chi_L$ ,  $\chi_R$  to generate the condensation  $H \sim (\bar{\chi}_R t_L, \bar{\chi}_R b_L)$ 

Lead to a heavy Higgs  $m_H \sim 1$  TeV, a SM t, and a heavy state  $\chi$ ,  $M_{\chi} \approx 4$  TeV. (B). Dynamical approach for mass generation:

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  - A less ambitious approach: Little Higgs Models Accept the existence of a light Higgs; keep the Higgs boson "naturally" light (at 1-loop level).

Predicts new "partner particles":  $W, Z, B \leftrightarrow W_H, Z_H, B_H; \quad t \leftrightarrow T; \quad H \leftrightarrow \Phi.$ 

# (C). Extra-dimensions: A new approach to the hierarchy problem

• Large Extra-dimension Scenario; ADD\*

In a world with D = 4 + n dimensions, *n* of them compactified,



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the 4-dim Planck scale is related to the D-dim one  $M_D$  as  $M_{PL}^2 \sim M_D^{n+2} \int dx^n = M_D^{n+2} V_n.$ Thus the fundamental scale in the theory:  $M_D \sim (M_{pl}^2/V_n)^{1/n+2} \longrightarrow \mathcal{O}(1 \text{ TeV}).$ 

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If an extra dimension y becomes compact (a circle of radius R), then all fields (gravitational, electromagnetic etc.) in y-dimension are periodic functions :

$$F(x,y) = \sum_{n=-\infty}^{\infty} F^n(x) e^{in \cdot y/R}.$$

Equation of motion:

$$(\partial^{\mu}\partial_{\mu} - \partial^{y}\partial_{y})F(x,y) \Rightarrow (\partial^{\mu}\partial_{\mu} + \frac{n^{2}}{R^{2}})F^{n}(x)$$
  
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No  $\gamma_{KK}$ ,  $e_{KK}^-$ , ... found  $\Rightarrow R^{-1}$  large; or  $\gamma$ ,  $e^-$  ... don't go there.

• Graviton Interactions With SM Fields:

The rule: gravitons couple to ANYTHING (attach it on any legs or vertices in the SM)



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Although each graviton couples gravitationally  $\kappa^2 \sim G_N$ , the high-degeneracy leads to

$$\kappa^2 \rho(m) dm^2 \sim \kappa^2 R^n m^{n-2} dm^2 \sim E^n / M_S^{n+2}$$

Effective coupling  $\kappa^2 \sim \frac{1}{M_{pl}^2} \rightarrow \frac{1}{M_S^2}$  !

• The Randall-Sundrum Scenario

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The extra dimension y is "warped":

$$ds^2 = e^{2A(y)} \eta_{\mu\nu} dx^{\mu} dx^{\nu} - dy^2,$$

where the "warp" factor A(y) = -ky, with k the curvature scale in the 5<sup>th</sup>-dim.



So the masses of the KK states are not equally-spaced.

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Electroweak precision constraints;

K/B rare decays and CP violation:  $B \rightarrow X_s \gamma$ ;  $J/\psi K_S$ ,  $\phi K_S$ ,  $\eta' K_S$ ...;

Neutrino masses and mixing;

muon g-2;  $\mu \rightarrow e\gamma...$ ; neutron/electron EDMs;

Nucleon stability;
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Yet more to come:

Tevatron:  $(p\bar{p} \text{ at } 1.96 \text{ TeV}, \text{ current})$ 

EW, top sector, new particle searches, Higgs (?) ...

LHC: (pp at 14 TeV, 2007)

comprehensive Higgs studies, extensive new particle searches... ILC:  $(e^+e^- \text{ at } 500 \text{ GeV} - 1 \text{ TeV } ?)$ 

more on top sector, precision Higgs and new light particles...

New Physics Search at Hadron Colliders

In high-energy hadron collisions,



New Physics Search at Hadron Colliders

In high-energy hadron collisions,



- Higher energy threshold:  $M_{new} \sim \sqrt{s}$ .
- multiple (strong, electroweak) channels:  $q\bar{q}, gg, qg, b\bar{b}, WW$  ...

Scattering cross sections for various SM processes:



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- Rare events: once every 1,000,000, there may be one interesting ...
- challenge to dig signals out of the backgrounds...

How to search for new particles?

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Distinctive decay products: (in high  $p_T$ )



• invariant mass of two-body  $R \rightarrow ab$ :  $m_{ab}^2 = (p_a + p_b)^2 = M_R^2$ . Jacobian peak in transverse momentum:

$$rac{d\sigma(R
ightarrow ab)}{dp_T^2} \propto rac{1}{(m_{ab}^2-4p_T^2)^{1/2}}.$$

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• "transverse" mass of two-body  $W^- \rightarrow e^- \bar{\nu}_e$  :

$$m_{e\nu T}^{2} = (E_{eT} + E_{\nu T})^{2} - (\vec{p}_{eT} + \vec{p}_{\nu T})^{2}$$
  
=  $2E_{eT}E_{\nu T}(1 - \cos\phi) \leq M_{W}^{2}$ .

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• cluster transverse mass of multi-body  $H^0 \to W^+ W^- \to e^+ \nu_e \ e^- \overline{\nu}_e$ :

$$m_{WWT}^{2} = (E_{e1T} + E_{e2T} + E_{\nu 1T} + E_{\nu 2T})^{2} - (\vec{p}_{e1T} + \vec{p}_{e2T} + \vec{p}_{\nu 1T} + \vec{p}_{\nu 2T})^{2}$$
  
$$= (E_{e1T} + E_{e2T} + E_{T}^{miss})^{2} - (\vec{p}_{e1T} + \vec{p}_{e2T} + \vec{p}_{T}^{miss})^{2} \le M_{H}^{2}.$$
  
where  $\vec{p}_{T}^{miss} = -\sum_{obs} \vec{p}_{T}^{obs}.$ 

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YOU design an appropriate variable/observable for the search.

Higgs Searches at the Tevatron and the LHC:

The crucial features: Couplings proportional to masses.



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preferably to heavier particles.

## SM Higgs boson production rates:



#### SM Higgs boson production rates:



• At the Tevatron: hundreds of Higgs bosons may have been produced, for  $m_h \lesssim 200~{\rm GeV},~500~{\rm pb}^{-1}.$ 

• At the LHC: hundreds of thousand may be produce,

for  $m_h \lesssim 700$  GeV, 100 fb<sup>-1</sup>.

• Higgs first shot at the Tevatron:



### • SM Higgs fully covered at the LHC:



ATLAS report: combining multiple channels,  $10\sigma$  observation achievable.

• SUSY Higgs fully covered at the LHC:



#### Significance contours for SUSY Higgses

Regions of the MSSM parameter space ( $m_A$ ,  $tg\beta$ ) explorable through various SUSY Higgs channels

- 5  $\sigma$  significance contours
- two-loop / RGE-improved radiative corrections



# Weak Scale Supersymmetry

#### • SUSY partners

particles	symbol	spin	mass param.
gluino	$\widetilde{g}$	1/2	$M_{3}$
charginos	$ ilde{\chi}_1^\pm$ , $ ilde{\chi}_2^\pm$	1/2	$M_2$
neutralinos	$ ilde{\chi}^0_1$ , $ ilde{\chi}^{ar{0}}_2$ , $ ilde{\chi}^{ar{0}}_3$ , $ ilde{\chi}^0_4$	1/2	$M_1,\ \mu,\ B$
			$m_{H_u}^2,  m_{H_d}^2$
sleptons	$ ilde{e}_L$ , $ ilde{ u}_{e_L}$ , $ ilde{e}_R$	0	$m_{\ell L}^2$
	$ ilde{\mu}_L$ , $ ilde{ u}_{\mu_L}$ , $ ilde{\mu}_R$	0	
	$ ilde{ au}_1$ , $ ilde{ au}_2$ , $ ilde{ u}_{ au_L}$	0	$m^2_{\ell R}$
squarks	$ ilde{u}_L$ , $ ilde{d}_L$ , $ ilde{u}_R$ , $ ilde{d}_R$	0	$m_{q_L}^2$
	$ ilde{c}_L$ , $ ilde{s}_L$ , $ ilde{c}_R$ , $ ilde{s}_R$	0	1-
	$ ilde{t}_1$ , $ ilde{t}_2$ , $ ilde{b}_1$ , $ ilde{b}_2$	0	$m_{q_R}^2$
Higgs	$h^{0}, H^{0}, A^{0}, H^{\pm}$	0	$m_A^2,   an eta$

But where do they get their masses?

 $\Rightarrow$  "soft" SUSY breaking

(many parameters put in by hand)

Also general Yukawa couplings

 $A_{u,d,\ell}$ , that lead to Sfermion mixings; CP phases etc.

R-parity violation couplings ...

model	masses and mixing ang.	CP-viol. phases	TOTAL
SM	17	2	19
MSSM	79	45	124
(MSSM) <sub>BV</sub>	97	62	159
(MSSM) <sub>LV</sub>	157	122	279
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Guidance and Assumptions:

Based on observation:

\* Proton stability:

 $\Rightarrow$  *R*-parity conservation; or *B*, *L* not broken

simultaneously (in  $1^{st}, 2^{nd}$  generations).

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- \* No large CP-violation/FCNC:
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- Pure theoretical considerations:
- \* Gauge-coupling/Yukawa Unification:
- $\Rightarrow$  universal masses at the GUT scale
- \* radiative E.W.S.B.;
- \* LSP cold dark matter; ...

#### • Gauge coupling unification

$$\alpha_1 = \alpha_2 = \alpha_3 = \alpha_G$$
 at  $\mathcal{O}(10^{16} \text{ GeV})$ 



need the help of weak-scale SUSY threshold.

Hadron colliders can be a S-particle factory:

QCD production:  $q\bar{q}, gq, gg \rightarrow \tilde{q}\bar{\tilde{q}}, \tilde{q}\tilde{g}, \tilde{g}\tilde{g}$ . E.W. production:  $q\bar{q} \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^-, \tilde{\chi}_1^\pm \tilde{\chi}_1^0, \tilde{\chi}_1^\pm \tilde{\chi}_2^0$ .





 $\sigma(Tevatron) \approx \mathcal{O}(0.1 - 1 \text{ pb}); \ \sigma(LHC) \approx \mathcal{O}(10 - 100 \text{ pb}).$ 

New ball-game for signal searches:

The lightest SUSY particle (LSP  $\tilde{\chi}_1^0$ ) is stable (*R*-parity), and nearly non-interacting (in detectors),

 $\Rightarrow$  large missing energy is the characteristics; difficult to reconstruct a mass peak for the sparticle. New ball-game for signal searches:

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Details depend on the model...

• mSUGRA scenario: SUSY breaking near  $M_{GUT}$ . Supergravity as messenger to transmit SUSY breaking effects.

 $m_0, m_{1/2}, A, \tan\beta, \text{and } sign(\mu)$ 



Sparticle decays:

 $\tilde{\chi}_1^+ \to \tilde{\chi}_1^0 \ell^+ \nu, \quad \tilde{\chi}_1^0 q \bar{q}'$ 

$$\begin{split} &\tilde{\chi}_2^0 \to \tilde{\chi}_1^0 \ell^+ \ell^-, \quad \tilde{\chi}_1^0 q \bar{q} \\ &\tilde{g} \to \tilde{\chi}_2^0 q \bar{q}, \quad \tilde{g} \to \tilde{\chi}_1^+ \bar{q} q, \quad \tilde{g} \to \tilde{q} \bar{q}, \\ &\tilde{t}_1 \to \tilde{\chi}_1^0 t, \quad \tilde{t}_1 \to \tilde{\chi}_2^0 t, \quad \tilde{t}_1 \to \tilde{\chi}_1^+ b. \end{split}$$

Generically,  $\tilde{\chi}_1^0$  leads to missing energy signal: "missing  $\not\!\!\!E_T$  plus jets":  $\not\!\!\!E_T$ +jets "dilepton plus missing  $\not\!\!\!E_T$ "  $\ell\ell + \not\!\!\!E_T$  (±± or +-) "trilepton plus missing  $\not\!\!\!E_T$ "  $\ell\ell\ell + \not\!\!\!E_T$ 



LHC:  $m_0 > 4000 \text{ GeV}, m_{1/2} > 1400 \text{ GeV}, \tan \beta \gtrsim 45.$ 

• Gauge mediation scenario: SUSY breaking at  $\Lambda \sim 10 - 100$  TeV, Gauge interactions as messengers to mediate SUSY breaking effects.  $\Lambda$ , M, tan $\beta$ , and  $N_M$ 



Squarks and gluinos are typically heavier; Gravitino  $\tilde{G}$  LSP.



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The NLSP dominates phenomenology: 
$$\frac{\tilde{x}}{1/F}$$

NLSP	Decay to the $\widetilde{G}$
Bino-like Neutralino	$\widetilde{\chi}_1^0 \to \gamma \ \widetilde{G}$
Higgsino-like Neutralino	$\widetilde{\chi}_1^{\bar{0}}  ightarrow (h, Z, \gamma) \widetilde{G}$
Stau	$\widetilde{ au} \to  au \ \widetilde{G}$
Slepton Co-NLSP	${\tilde \ell}  o \ell  {\widetilde G}$
Squark	${ ilde q}  o (q,q'W)  { ilde G}$
Gluino	${ ilde g}  o g  {\widetilde G}$

$$c\tau(\tilde{x} \to x\tilde{G}) \approx 100 \ \mu \mathrm{m} \left(\frac{100 \ \mathrm{GeV}}{m_{\tilde{x}}}\right)^5 \left(\frac{\sqrt{F}}{100 \ \mathrm{TeV}}\right)^4.$$

could lead to a displaced vertex in decay, or quasi-stable charged track.

LHC reach:



New gauge bosons and heavy fermions
#### New gauge bosons and heavy fermions

Little Higgs models as an example In the Littlest Higgs model:\*



\*Arkani-Hamed, Cohen, Katz, Nelson, hep-ph/0206021.

$\tan\theta = \frac{s}{c} = \frac{g_2}{g_1}$	New $SU(2)$ gauge coupling (or equivalently mixing angle $\theta$ )
$\tan\theta' = \frac{s'}{c'} = \frac{g_2'}{g_1'}$	New $U(1)$ gauge coupling (or equivalently mixing angle $\theta'$ )
f	Symmetry breaking scale $\mathcal{O}(TeV)$
v'	Triplet $\phi$ vacuum expectation value, $v'/v \lesssim v/4f$
$m_H$	Regular SM Higgs mass
$M_T$	Heavy vector top mass, we trade $\lambda_2$ for $M_T$

• New gauge bosons in DY process:

Recall CDF searches for a  $Z' \rightarrow \mu^+ \mu^-$ : [PRL 79, (1997)]



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including:

 $A_H$  should be the lightest new state; • large DY production  $A_H \rightarrow \ell^+ \ell^-$  ( $\ell = e, \mu$ )



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Tevatron:  $M_{A_H} > 0.5$  TeV or f > 3 TeV; LHC:  $M_{A_H} \sim 3$  TeV or  $f \sim 18$  TeV.

•  $Z_H/W_H$  rebust new state • DY production rate large



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Tevatron: not quite accessible (except for  $A_H$ ); LHC:  $M_{Z_H} \sim 5$  TeV or  $f \sim 8$  TeV. ATLAS simulations for  $Z \rightarrow \ell^+ \ell^-$ :



Reach  $M_{Z_H} \sim \text{several TeV for } \cot \theta > 0.1$ :

ATLAS simulations for  $Z \rightarrow \ell^+ \ell^-$ :



 $\begin{array}{l} \mbox{Reach } M_{Z_H} \sim \mbox{several TeV for } \cot \theta > 0.1: \\ \mbox{Cross-sectiions measure } \cot \theta : \ N(\ell^+ \ell^-) \ \mbox{versus } N(Zh). \\ \mbox{Mass peak } M_{Z_H} \ \mbox{determines } f. \end{array}$ 

Significant differences for FB asymmetry among Z's:

$$A_{FB}^{i,f} = \frac{3}{4}A_iA_f, \quad A_i = \frac{g_L^2 - g_R^2}{g_L^2 + g_R^2}.$$
$$A_{FB}^{had} = \frac{\int dx_1 \sum_{q=u,d} A_{FB}^{qe} \left(F_q(x_1)F_{\bar{q}}(x_2) - F_{\bar{q}}(x_1)F_q(x_2)\right) \operatorname{sign}(x_1 - x_2)}{\int dx_1 \sum_{q=u,d,s,c} \left(F_q(x_1)F_{\bar{q}}(x_2) + F_{\bar{q}}(x_1)F_q(x_2)\right)},$$



## • Heavy quark signals:

Recall the top-quark searches at hadron colliders The leading production channels:

> $q\bar{q} \rightarrow t\bar{t}$ , Tevatron 90%; LHC 10%  $gg \rightarrow t\bar{t}$ , Tevatron 10%; LHC 90% with  $t\bar{t} \rightarrow W^+ b \ W^- \bar{b} \rightarrow ...$

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measure  $V_{tb}$  and test  $tbW_L$  coupling  $\leftarrow$  surely new at the Tevatron.



 $gg \rightarrow T\overline{T}$  phase-space suppression;  $qb \rightarrow q'T$  via *t*-channel  $W_Lb \rightarrow T$ .

ATLAS simulations for  $T \rightarrow tZ$ , bW:



Reach  $M_T \sim 1$  (2) TeV for  $x_{\lambda} = 1$  (2).

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Cross-sections measure coupling  $x_{\lambda}$ . Mass peak  $M_T$  determines  $f: v/f = m_t/M_T(x_{\lambda} + x_{\lambda}^{-1})$  $\implies$  check consistency with f from  $M_{Z_H}$ . If there is either a *U*-type or *D*-type heavy quark, must observe  $W^+d \rightarrow U$  or  $W^-u \rightarrow D$ :



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Interesting to note:

- $\sigma_U \approx 10 \sigma_{\bar{U}}; \quad \sigma_D \approx 10 \sigma_{\bar{D}};$
- $U \rightarrow d\ell^+ \nu^- \Rightarrow$  sequential fermion embedding;

 $D \rightarrow u \ell^- \bar{\nu} \Rightarrow$  anomaly-free fermion embedding.

Kinematical features:  $W^+d \rightarrow U \rightarrow \ell^+\nu j$ :



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Deep into extra-dimensions at the LHC:

- Observable signatures for extra-dim models:
- ▷ At "low" energies
  - † "very low":  $E \ll 1/R, M_D$ :
  - 4d effective theory: as the Standard Model; weak effects from gravity.

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> Intermediate energy regime  $E \sim M_D$ : stringy states significant: s-channel poles as resonances:

$$\mathcal{M}(s,t) \sim \frac{t}{s - M_n^2}, \quad M_n = \sqrt{n} M_S.$$

▷ At "trans Planckian" energies  $E > M_D, M_S$ : (4 + n)-dim physics directly probed; gravity dominant: black hole production\*

 $\sqrt{s} = M_{BH} > M_D$  for  $b < r_{bh}$ .

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$$r_{bh} = \frac{1}{\sqrt{\pi}M_D} \left[ \frac{M_{BH}}{M_D} \left( \frac{8\Gamma\left(\frac{n+3}{2}\right)}{n+2} \right) \right]^{\frac{1}{n+1}} \to M_{BH}/M_{pl}^2 \text{ in 4d}$$
  
$$\sigma = \pi r_{bh}^2.$$



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• Collider Searches for Extra Dimensions:

A. Collider Signals I (ADD)

Real KK Emission: Missing Energy Signature a.  $e^+e^- \rightarrow \gamma + KK$  ( $\gamma$ +missing energy)



 $\begin{array}{ll} {\rm n-dim:} & {\rm at \; LEP2} \\ {\rm n=4} & M_S > 730 \; {\rm (GeV)} \\ {\rm n=6} & M_S > 520 \; {\rm (GeV)} \end{array}$ 

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b.  $p\bar{p} \rightarrow jet + KK$  (mono-jet+missing energy)

n – dim :	at Tevatron	at LHC
<i>n</i> <b>= 4</b>	$M_S>$ 900 (GeV)	3400
n = 6	$M_S>$ 810 (GeV)	3300

B. Collider Signals II (ADD)

Virtual KK Graviton Effects

On four-particle contact interactions:



Sum over virtual KK exchanges:

$$i\mathcal{M} \sim \overline{f}\mathcal{O}_i f \ \overline{f}\mathcal{O}_j f \int_0^\infty \frac{dm_{\vec{n}}^2 \ \kappa^2 \rho(m_{\vec{n}})}{s - m_{\vec{n}}^2 + i\epsilon}$$
  
 $\sim \frac{s^2}{M_S^4} \ \overline{f}\mathcal{O}_i f \ \overline{f}\mathcal{O}_j f.$ 

Again, effective coupling  $\kappa^2 \sim \frac{1}{M_{pl}^2} \rightarrow \frac{1}{M_S^2}$  !

Qualitative differences for signal/background distributions, due to the spin-2 exchange:



*LR* asymmetry for  $e^+e^- \rightarrow b\overline{b}$  at  $\sqrt{s} = 500$  GeV. Solid: SM; "data" points for  $\lambda = \pm 1$  with = 75  $fb^{-1}$ .

C. KK Resonant States at Colliders: (RS) If the SM fields (photons, electrons,  $Z, W, H^0...$ ) also propagate in extra dimensions, then they have KK excitations. Direct search bounds:

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Resonant production at the LHC:



D. Stringy States at Colliders
Future colliders may reach the TeV string threshold thus directly produce the "stringy" resonant states.
Amplitude factor near the resonance

$$\mathcal{M}(s,t) \sim \frac{t}{s - nM_S^2}$$
, its mass  $M_n = \sqrt{n}M_S$ .

# D. Stringy States at Colliders Future colliders may reach the TeV string threshold thus directly produce the "stringy" resonant states. Amplitude factor near the resonance

 $\mathcal{M}(s,t) \sim \frac{t}{s - nM_S^2}$ , its mass  $M_n = \sqrt{n}M_S$ .



where T is an unkown gauge factor (Chan-Simon factor), typically 1-4.

#### Very rich structure of angular distributions:


LHC 95% C.L. sensitivity from  $\ell^+\ell^-$  mode:



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With 300  $fb^{-1}$ , if no signal seen, we expect to reach bounds for

 $M_S > 8$  (10) TeV for T = 1 - 4.

### E. Black Hole Production at Colliders For a black hole of mass $M_{BH}$ , its size is

$$r_{bh} \approx \frac{1}{M_D} \left( \frac{M_{BH}}{M_D} \right)^{\frac{1}{n+1}} \rightarrow \frac{M_{BH}}{M_{pl}^2} \text{ in 4d.}$$

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At higher energies and shorter distances (impact parameter)

 $E_{cm} > M_{BH} > M_D, \quad b_{impact} < r_{bh},$ 

black holes formation is the dominant

quantum gravity phenomena.



Black holes copiously produced at the LHC energies,

$M_{BH}$	<i>n</i> = 4	n = 6
5 TeV 7 TeV 10 TeV	$1.6 imes 10^5~{ m fb}\ 6.1 imes 10^3~{ m fb}\ 6.9~{ m fb}$	$2.4  imes 10^5$ fb $8.9  imes 10^3$ fb 10 fb

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3-brane

Black holes "decay" via Hawking radiation:  $\gamma, \nu, e^{\pm}, hadrons, \dots W^{\pm}, Z \dots, gravitons$ 

Spectacular events:

- very luminous in the detector!
- lepton-number/baryon-number violation (?)
- spherical/angular momentum orientation (?) ... ...

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Realize the Tevatron potential, go for the LHC! Major breakthrough ahead of us!