

# Heavy

## Quark Production

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# Statement of the Problem

## OUTLINE

- Statement of the problem
- Status report:
  - Comparison of Data & Theory
- How do we make heavy quarks
- B-Hadroproduction: A case study
- Single Top Production

CKM Quark Mixing Matrix

- Conclusions

- Coffee

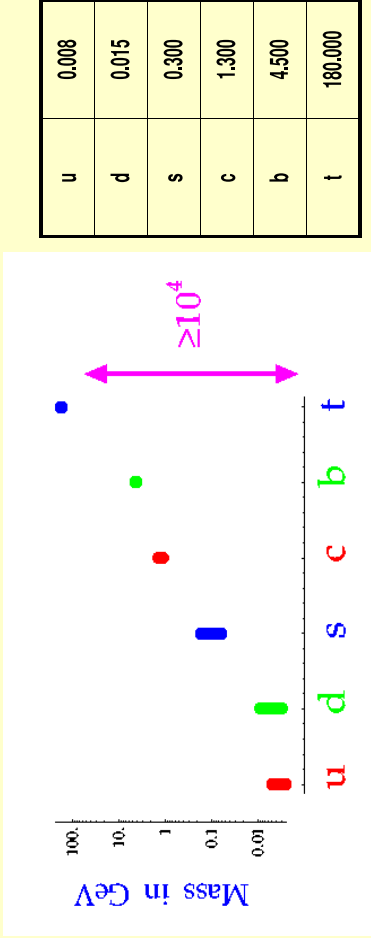
## A Thought Experiment:

What is the ideal way to learn about quark masses and their effects on a physical process?

As a theorist, I simply run my calculation over the full range of mass values from 0 to  $\infty$ , and study the behavior.

Wouldn't it be great if the experiments could do the same???

Quark Masses Span Wide Dynamical Range  $\sim 10^4$



We can't vary the quark mass continuously, but these "notches" on our control panel give us a lot of flexibility

Single-Scale Problem in Perturbation Theory:

$$\sigma = \sum_{N=1}^{\infty} (\alpha_s L)^N = \sum_{N=1}^{\infty} \left\{ \alpha_s(\mu) \log\left(\frac{E^2}{\mu^2}\right) \right\}^N$$

... where E is any relevant scale of the problem: Q, P<sub>T</sub>, E<sub>T</sub>, ...

Use RGE to solve this.  $\frac{d\sigma}{d\log\mu^2} = \dots$

Multi-Scale Problem in Perturbation Theory:

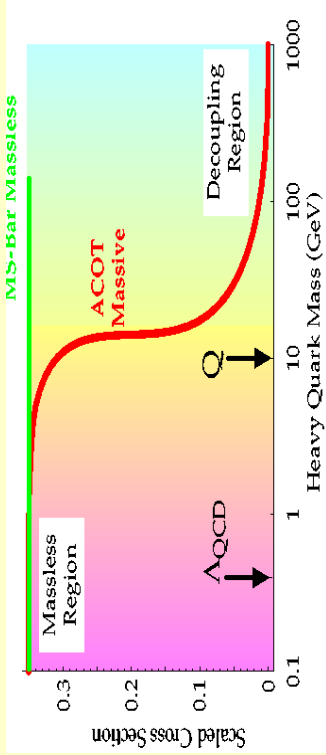
What do we do if we have 2 scales???

$$\log\left(\frac{E^2}{\mu^2}\right) \quad \log\left(\frac{M_H^2}{\mu^2}\right)$$

... life gets interesting.

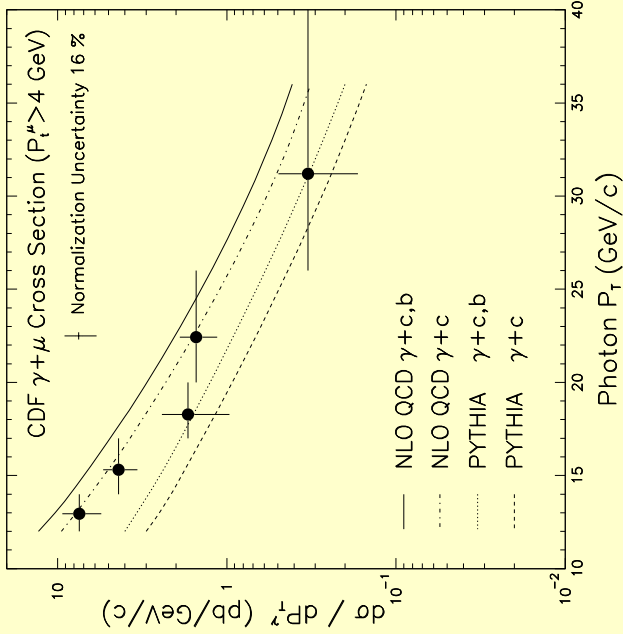
Theorists would much prefer that quark masses only come in 2 varieties:

- $m = 0$ : Massless case.  $m = \infty$ : Infinite case.
- Mass plays no dynamic role. Mass Decouples.
- Well understood. We can forget about this object



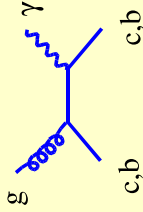
# Status Report:

# Comparison of Data & Theory



Comparison of Run I Data with NLO Theory

Reasonable agreement within theory uncertainty

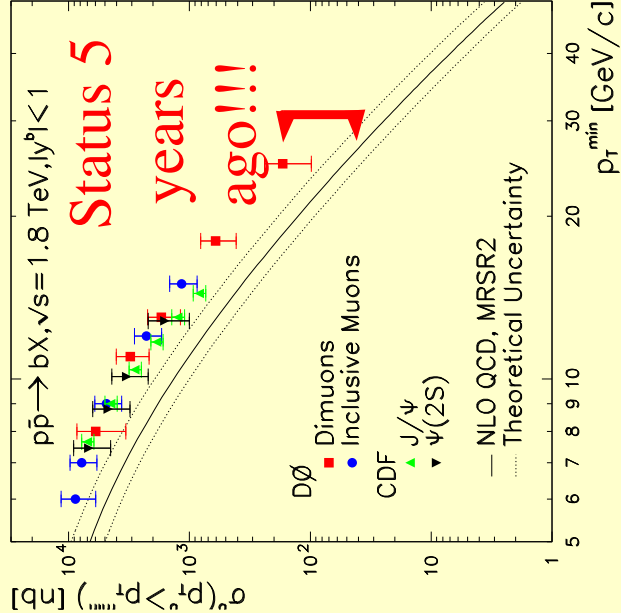
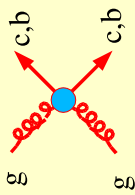


## Hadroproduction of Beauty at Tevatron

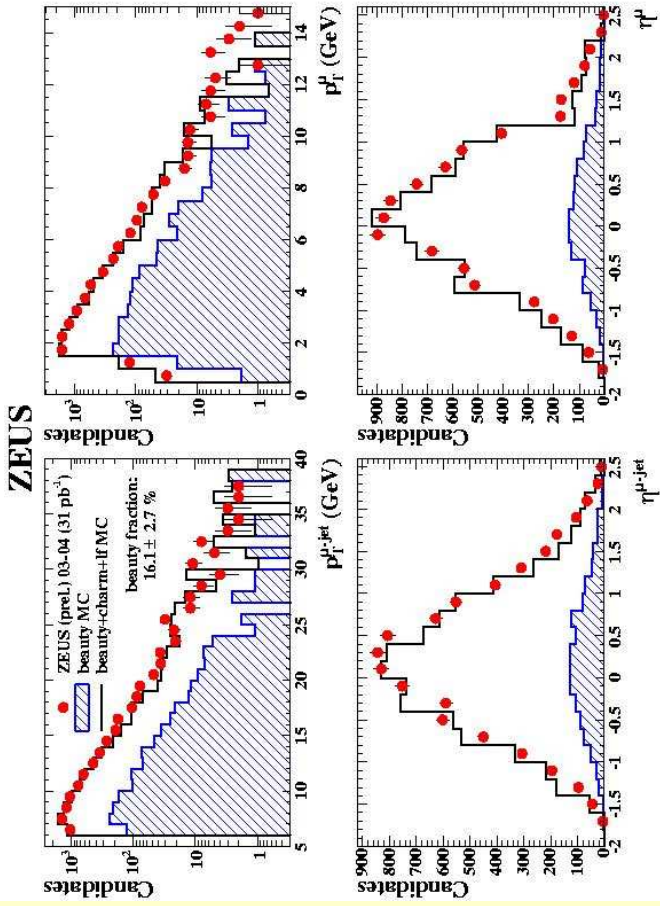
Comparison of Run I data with NLO Theory

Data is high by factor of 2x or 3x

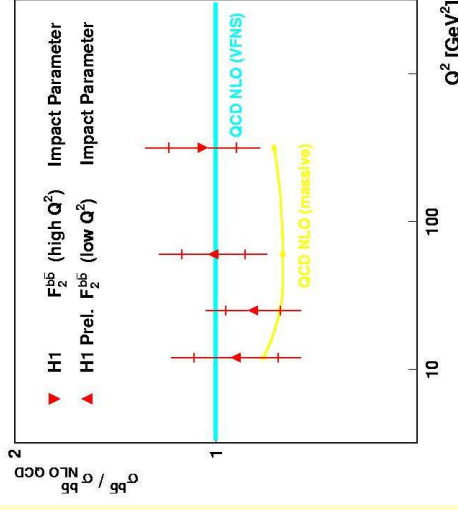
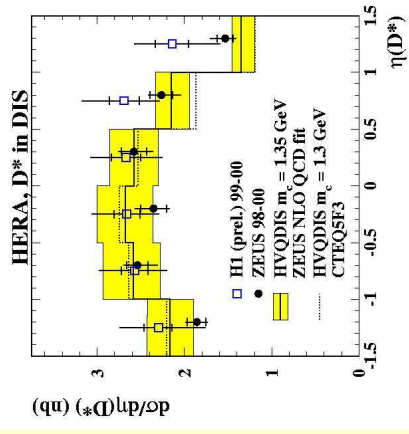
... even given  $\mu$  variation

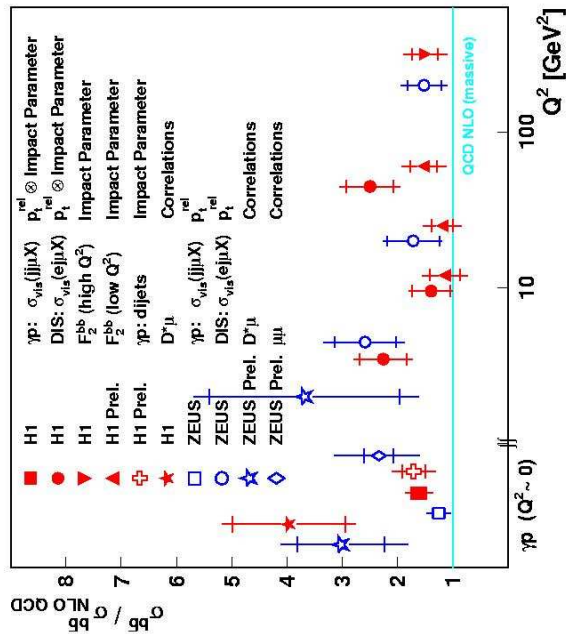


... we'll come back to this...

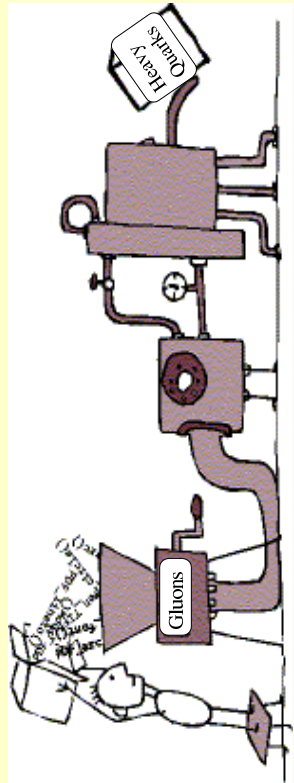


## Charm & Beauty Production at HERA





# How do we make heavy quarks



## The Dilemma

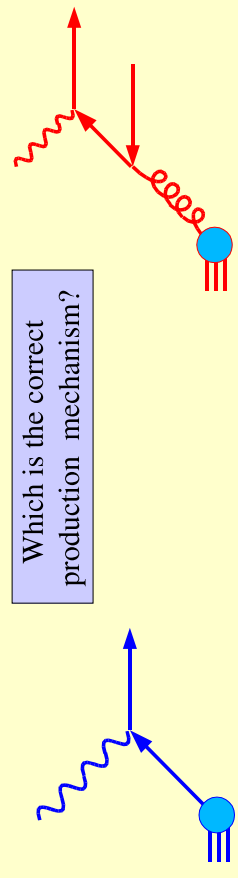
### General Trend:

Charm: in good shape  
Bottom: needs examination

### Should Bottom be a problem???

$m_b \approx 4.5 \text{ GeV}$        $m_c \approx 1.5 \text{ GeV}$   
 $\text{Log}[m_b/m_c] \approx \text{Log}[3] \approx \text{Not a big number!!!}$   
 $\alpha_s(m_b) < \alpha_s(m_c)$

## Production of Heavy Quarks: The Problem



Heavy Excitation (HE)

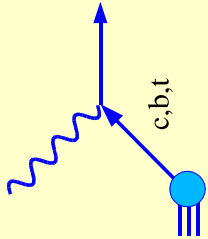
| Quark | Channel |
|-------|---------|
| s     | YES     |
| t     | NO      |
| c     | ???     |
| b     | ???     |

Heavy Creation (HC)

| Quark | Channel |
|-------|---------|
| s     | NO      |
| t     | YES     |
| c     | ???     |
| b     | ???     |

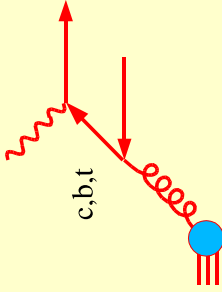
*If you can't beat 'em, join 'em.*

## How to Join without ``Double Counting''???

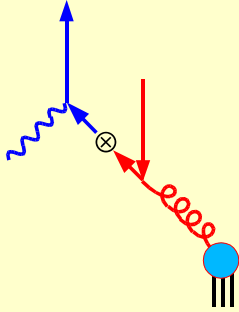


Heavy Excitation (HE)

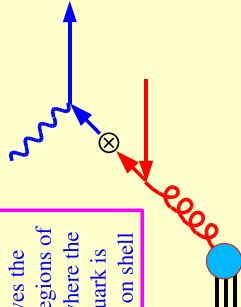
Wait a minute!  
Since the heavy quark originally came from a gluon splitting, these diagrams are **Double Counting**



Heavy Creation (HC)



Subtraction (SUB)

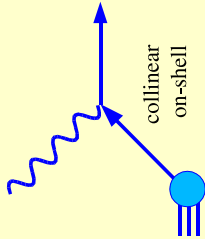


SUB removes the overlapping regions of phase space where the t-channel quark is collinear and on shell

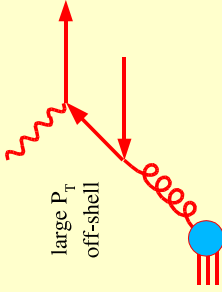
$$\text{TOT} = \text{HE} + (\text{HC} - \text{SUB})$$

Formally, NLO

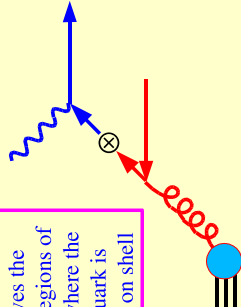
## How to Join without ``Double Counting''???



Heavy Excitation (HE)



Heavy Creation (HC)



SUB removes the overlapping regions of phase space where the t-channel quark is collinear and on shell

$$\text{TOT} = \text{HE} + (\text{HC} - \text{SUB})$$

Formally, NLO

## There is a rigorous factorization proof ...

### Ingredients of Factorization

Decompose into (t-channel) 2PI amplitudes:

$$\sigma = \sum_{N=1}^{\infty} C (K)^N T + \text{Non-leading}$$

Collins, Soper, Sterman, Perturbative QCD, World Scientific (1989), Collins in preparation

After reorganization of the infinite sum:

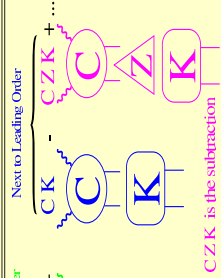
$$\sigma \approx \underbrace{C [1 - (1-Z)] K^1 J^1 T}_{\text{Wilson Coefficient (Hard Scat. G')}} + \underbrace{C [1 - (1-Z)] K^1 J^1 T}_{\text{Wilson Coefficient (Hard Scat. G')}} + \underbrace{C [1 - (1-Z)] K^1 J^1 T}_{\text{Wilson Coefficient (Hard Scat. G')}} + \underbrace{C [1 - (1-Z)] K^1 J^1 T}_{\text{Wilson Coefficient (Hard Scat. G')}} + \dots$$

Wilson Coefficient:

$$C [1 - (1-Z)] K^1 J^1 \approx$$

All orders result

Wilson Coefficient: IR safe, "hard" scattering cross section



CZK is the subtraction

A formal proof was constructed by numerous groups.

This proof was explicitly extended to the case of massive quarks

(Collins, 1998)

THOUGH

EXPERIMENT

To keep things simple, let's consider scattering off a parton target.

## Application of Factorization Formula at Leading Order (LO)

Basic Factorization Formula

$$\sigma = f \otimes \omega \otimes d + O(\Lambda^2/Q^2)$$

### At Zeroth Order:

$$\sigma^0 = f^0 \otimes \omega^0 \otimes d^0 + O(\Lambda^2/Q^2)$$

Use:  $f^0 = \delta$  and  $d^0 = \delta$  for a **parton** target.

Therefore:

$$\sigma^0 = f^0 \otimes \omega^0 \otimes d^0 = \delta \otimes \omega^0 \otimes \delta = \omega^0$$

$$\sigma^0 = \omega^0$$



$f^0$

$f^1$

for parton target

**Warning: This trivial result leads to many misconceptions at higher orders**

Basic Factorization Formula

$$\sigma = f \otimes \omega \otimes d + O(\Lambda^2/Q^2)$$

## At First Order:

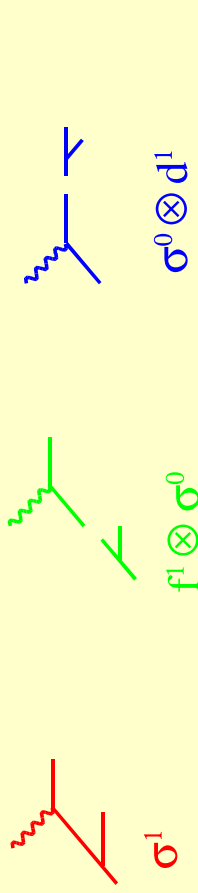
$$\sigma^1 = f^1 \otimes \omega^0 \otimes d^0 + f^0 \otimes \omega^1 \otimes d^0 + f^0 \otimes \omega^0 \otimes d^1$$

$$\sigma^1 = f^1 \otimes \sigma^0 + \omega^1 + \sigma^0 \otimes d^1$$

We used:  $f^0 = \delta$  and  $d^0 = \delta$  for a **parton** target.

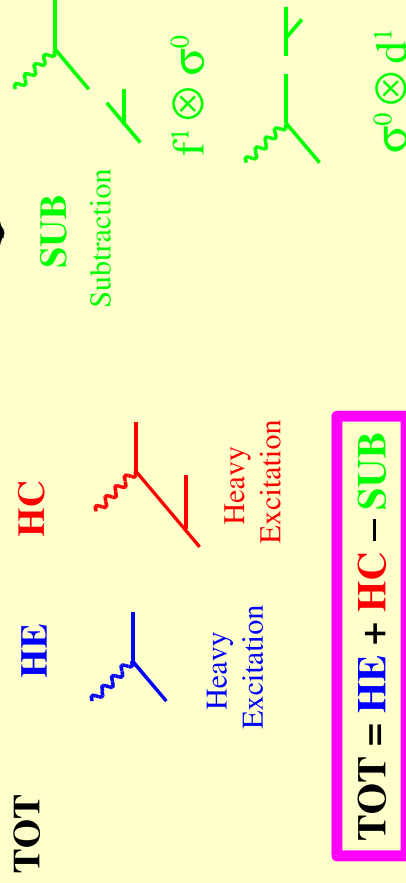
Therefore:

$$\omega^1 = \sigma^1 - f^1 \otimes \sigma^0 - \sigma^0 \otimes d^1$$



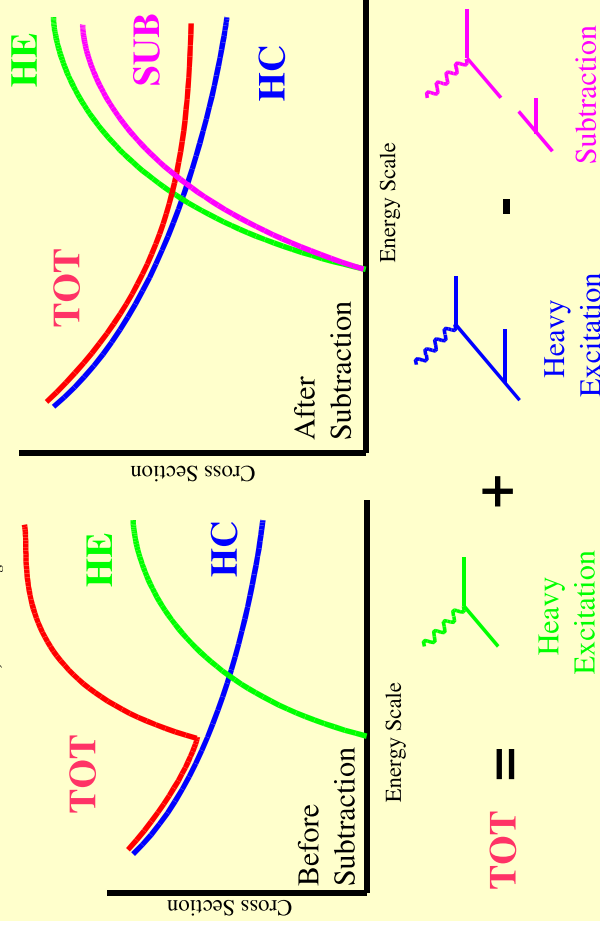
## Combined Result:

$$\omega^0 + \omega^1 = \sigma^0 + \sigma^1 - \left\{ f^1 \otimes \sigma^0 + \sigma^0 \otimes d^1 \right\}$$



$$\text{TOT} = \text{HE} + \text{HC} - \text{SUB}$$

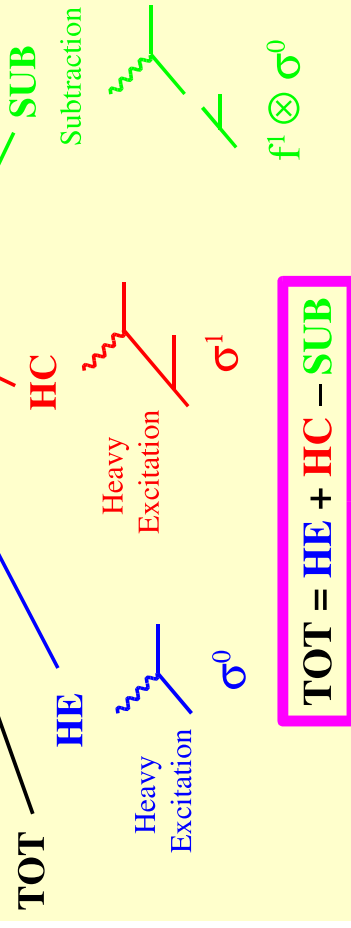
Note, we'll see this again ...



Expand  $f(x)=x$  in Taylor Series about  $x_0$ .

$$\text{For } x_0=0: f(\epsilon) = 0 + (\epsilon - 0) + \dots = \epsilon$$

$$\text{For } x_0=1: f(\epsilon) = 1 + (\epsilon - 1) + \dots = \epsilon$$



$$\text{TOT} = \text{HE} + \text{HC} - \text{SUB}$$

**It doesn't matter which expansion point you use;  
QCD will compensate (if you go to high enough order).**

*In practice ...*

**we are often limited to low-order calculations,  
so it is wise to choose your expansion point carefully.**

Part 1) Show these 3 definitions are equivalent; work out the limits of integration.

$$\begin{aligned} f \otimes g &= \int f(x)g(y)\delta(z - x * y)dx dy \\ f \otimes g &= \int f(x)g\left(\frac{z}{x}\right)\frac{dx}{x} \\ f \otimes g &= \int f\left(\frac{z}{y}\right)g(y)\frac{dy}{y} \end{aligned}$$

Part 2) Show convolutions are the ``natural'' way to multiply probabilities.

If  $f$  represents the heads/tails probability distribution for a single coin flip, show that the distribution of 2 coins is  $f \oplus f$  and 3 coins is  $f \oplus f \oplus f$ .

$$\begin{aligned} f \oplus g &= \int f(x)g(y)\delta(z - (x + y))dx dy \\ f(x) &= \frac{1}{2}(\delta(1 - x) + \delta(1 + x)) \end{aligned}$$

*BONUS: How many processes can you think of that don't factorize?*

Use the Basic Factorization Formula

$$\sigma = f \otimes \omega \otimes d + O(\Lambda^2/Q^2)$$

**At Second Order:**

$$\sigma^2 = f^2 \otimes \omega^0 \otimes d^0 + \dots$$

$$f^1 \otimes \omega^1 \otimes d^0 + \dots$$

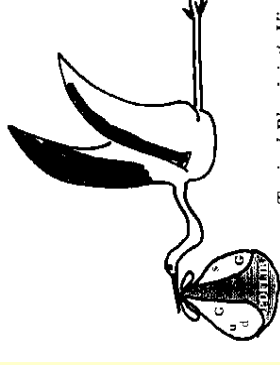
Therefore:

$$\omega^2 = ???$$

- Compute  $\omega^2$  at second order.
- Make a diagrammatic representation of each term.

# B-Hadronproduction: A Case Study

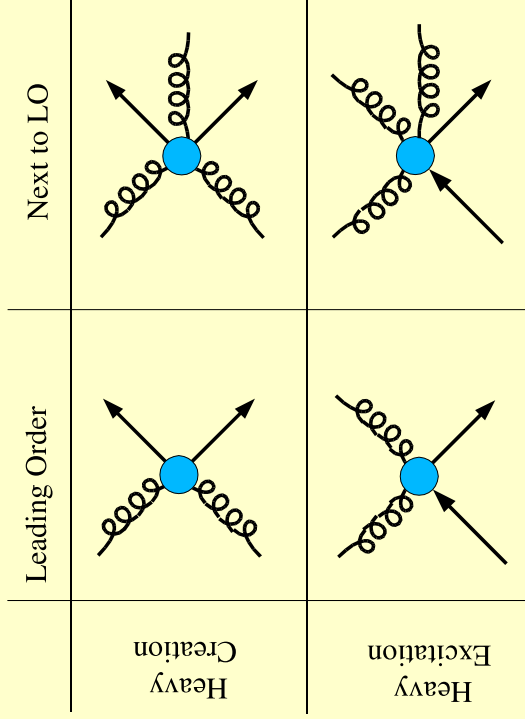
Where do PDF's come from???



*Typical Physicist's View*

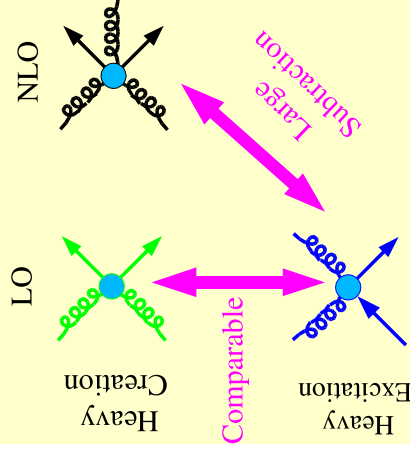
Drawing by Heidi Schellman

## The Basic Contributions to Heavy Flavor Production



Fixed-Flavor Scheme  
Variable-Flavor Scheme

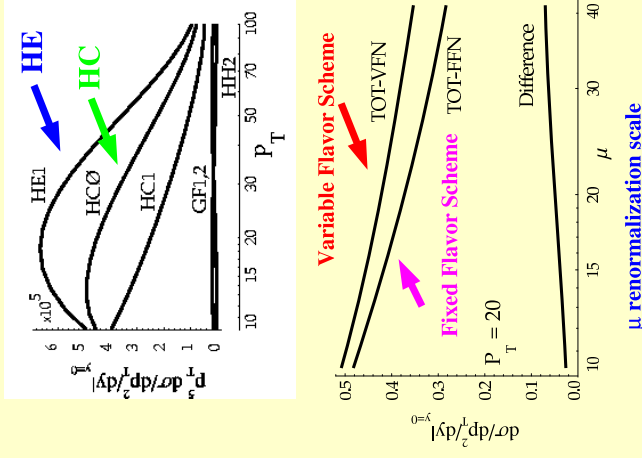
## NLO Variable Flavor Scheme



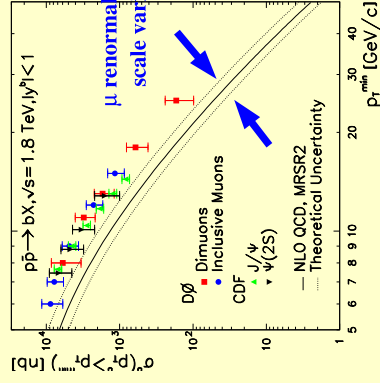
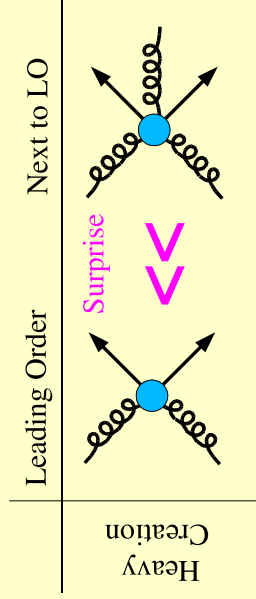
Net result:

- Reduction of  $\mu$ -dependence
- 30% to 50% increase in  $\sigma$

Alvarez, Collins, Olness, Tung  
Olness, Sealise, Tung



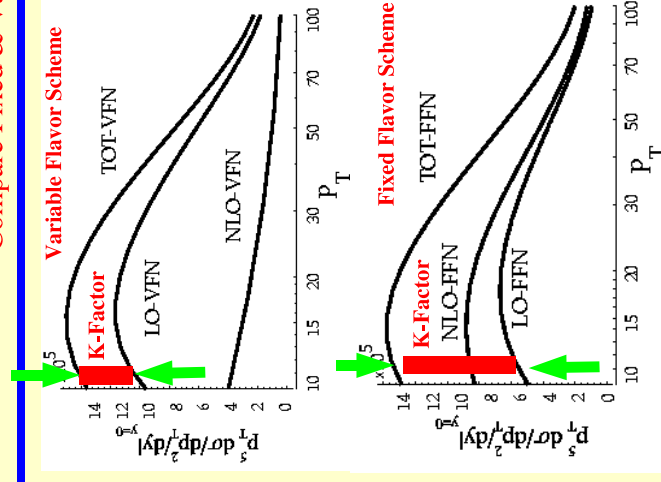
## NLO Fixed-Flavor Scheme



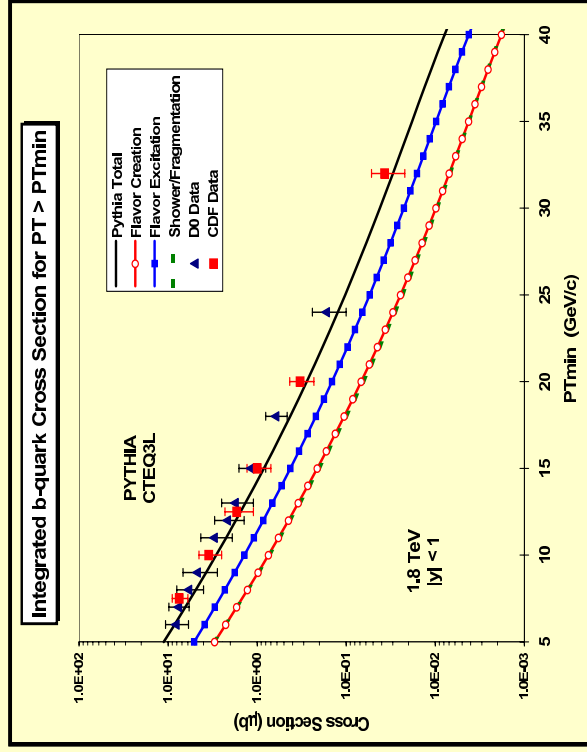
Surprise: NLO / LO ~ 2  
But, theory still below data

Nason, Dawson, Ellis  
Beenakker, Kuijf, Van Neerven, Smith

## Compare Fixed & Variable Flavor Scheme



- To NLO, different schemes are comparable.
- K-Factor very different.
- Suggestion: VFS may provide more efficient organization of perturbation series than FFS.
- Recall: Choice of expansion point  $x_0$  in Taylor series.



Flavor Creation  
Flavor Excitation

R. Field, hep-ph/0201112

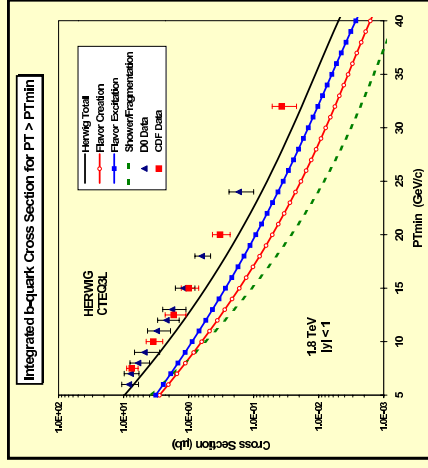
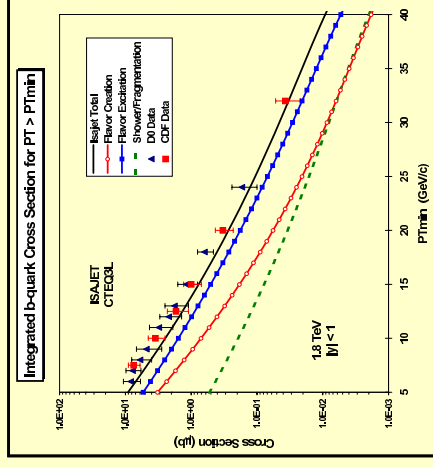
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2005 CTEQ School

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Flavor Creation

Flavor Excitation



R. Field, hep-ph/0201112

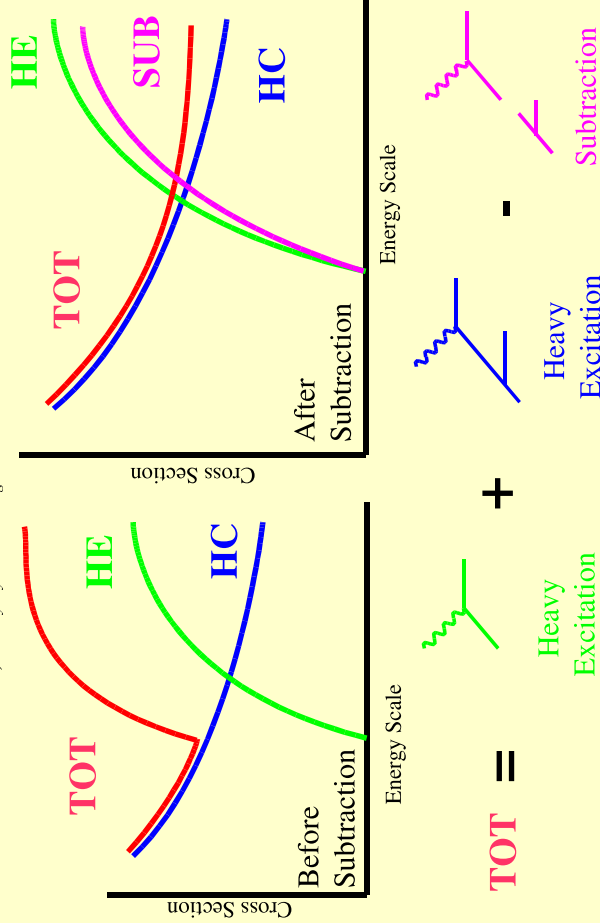
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## Recall

Note, we told you you'll see this again ...

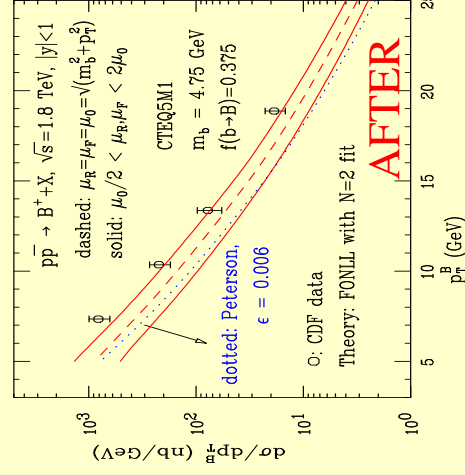
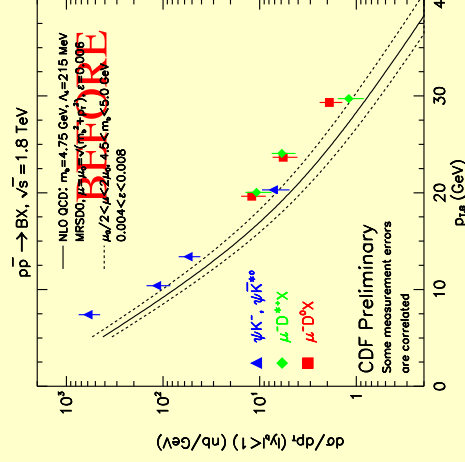


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## B production with modified fragmentation function



Cacciari & Nason, hep-ph/0304025  
Cacciari, Greco, Nason, JHEP 9805:007, 1998  
Cacciari & Greco, Nucl.Ph.B421:530, 1994

The effect of modifying the bottom fragmentation function raises theory predictions in the range of data.  
Note, we observe b-hadron, not b-quark!!!

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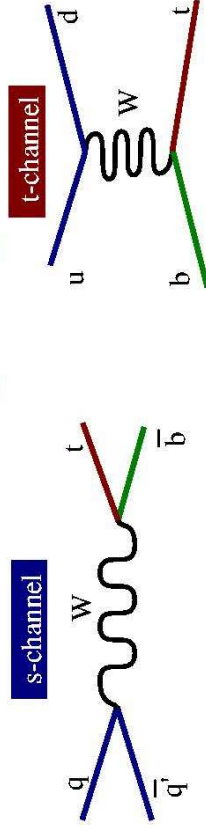
2005 CTEQ School

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# Single Top Production

# The CKM Quark Mixing Matrix

## Tevatron Single Top Goals



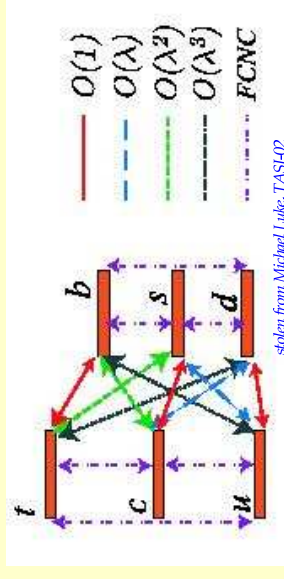
- Observe single top quark production
  - Separately in the s-channel and t-channel
- Measure production cross sections
  - CKM matrix element  $V_{tb}$
- Look for physics beyond the Standard Model
- Study top quark spin correlations – probe V-A
- Irreducible background to associated Higgs production



## The CKM Quark Mixing Matrix

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$$\begin{pmatrix} 0.97 & 0.22 & 0.003 \\ 0.22 & 0.97 & 0.04 \\ 0.003 & 0.04 & 0.999 \end{pmatrix}$$



$$\begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

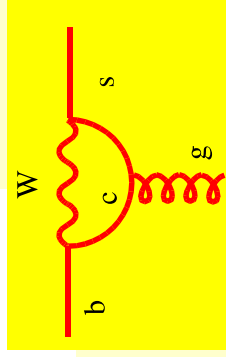
3-Generations;  
4 real parameters;  
 $\eta$  controls Im part  
 $\Rightarrow$   
CP-violation

## First Measurement of the Rate for the Inclusive Radiative Penguin Decay $b \rightarrow s\gamma$

M.S. Alam,<sup>1</sup> I.J. Kim,<sup>1</sup> Z. Ling,<sup>1</sup> A.H. Mahmood,<sup>1</sup> J.J. O'Neill,<sup>1</sup> H. Severini,<sup>1</sup> C.R. Sun,<sup>1</sup>  
F. Wappler,<sup>1</sup> G. Crawford,<sup>2</sup> C. M. Daubenmier,<sup>2</sup> R. Fulton,<sup>2</sup> D. Fujino,<sup>2</sup> K.K. Gan,<sup>2</sup>  
A. Wolf,<sup>2</sup>  
A. Wood<sup>3</sup> M

We have measured the inclusive  $b \rightarrow s\gamma$  branching ratio to be  $(2.32 \pm 0.57 \pm 0.35) \times 10^{-4}$ , where the first error is statistical and the second is systematic. Upper and lower limits on the branching ratio, each at 95% CL, are  $\mathcal{B}(b \rightarrow s\gamma) < 4.2 \times 10^{-4}$  and  $\mathcal{B}(b \rightarrow s\gamma) > 1.0 \times 10^{-4}$ . These limits restrict the parameters of extensions of the Standard Model.

PACS numbers: 13.25Hw, 14.40.Nd

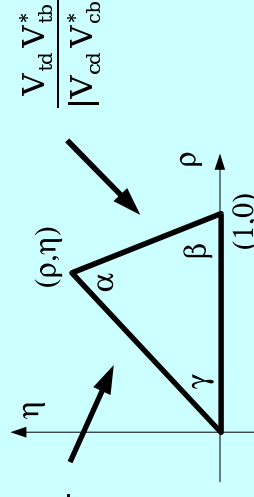


$$\text{Br}(b \rightarrow s\gamma) = 2.32 \pm 0.57 \pm 0.35 \times 10^{-4}$$

## From Theory to Certainty. BaBar announces new result on Charge Parity violation

At the International Conference on High Energy Physics in Amsterdam on July 25, the BaBar collaboration working at the Department of Energy's Stanford Linear Accelerator Center (SLAC) announced their new measurement of a parameter known as sine two beta, that expresses the degree of asymmetry between matter and antimatter. This result is the product of three years of intense research and is a classic example of how understanding of our universe advances through high energy physics research.

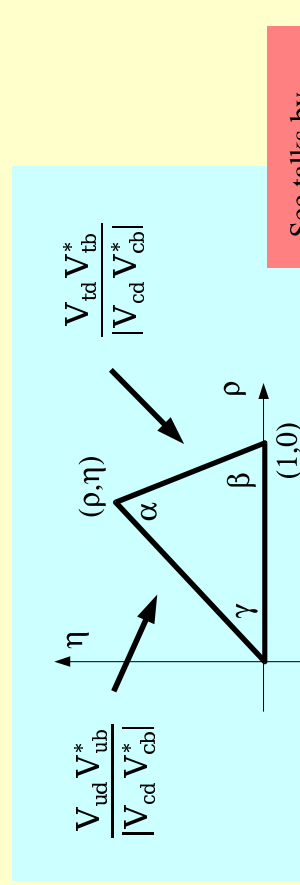
if  $\eta$  (or  $\beta$ ) is zero, no  
CP-violation  
 $\sin(2\beta) = 0.59 \pm 0.14 \pm 0.05$



## CP Violation in the CKM Mixing Matrix

$$\begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho + i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

stolen from Michael Luke, TASI-02



See talks by  
V. Sharma,  
M. Neubert

if  $\eta$  (or  $\beta$ ) is zero, no CP-violation

## The Mixing Matrix

Neutrino

$$U = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \times \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \times \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

**Atmospheric**      **Cross-Mixing**      **Solar**

$$c_{ij} \equiv \cos \theta_{ij}$$

$$s_{ij} \equiv \sin \theta_{ij}$$

$$\begin{bmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

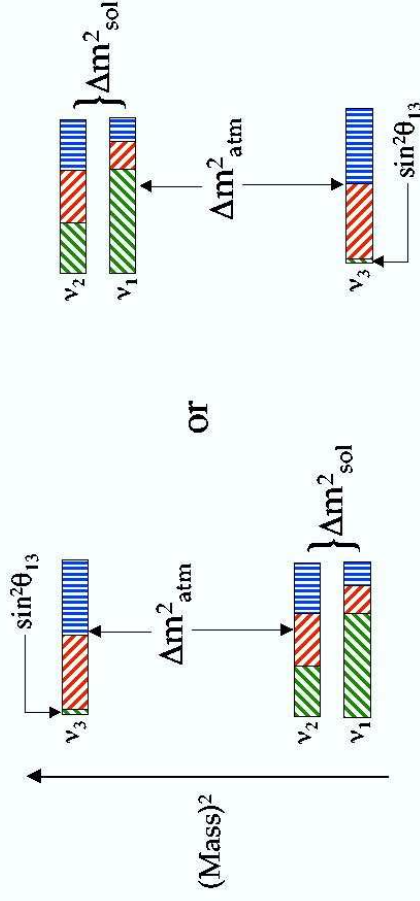
**Majorana CP phases**

$\theta_{12} \approx \theta_{\text{sol}} \approx 33^\circ$ ,  $\theta_{23} \approx \theta_{\text{atm}} \approx 37-53^\circ$ ,  $\theta_{13} < 12^\circ$

$\delta$  would lead to  $P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta) \neq P(\nu_\alpha \rightarrow \nu_\beta)$ . CP

But note the crucial role of  $s_{13} \equiv \sin \theta_{13}$ .

The spectrum, showing its approximate flavor content, is



Normal

Inverted

$$\nu_e [ |U_{e1}|^2 ]$$

$$\nu_\mu [ |U_{\mu 1}|^2 ]$$

$$\nu_\tau [ |U_{\tau 1}|^2 ]$$

... not very diagonal

stolen from Boris Kayser, Phenon 2005

## Conclusions

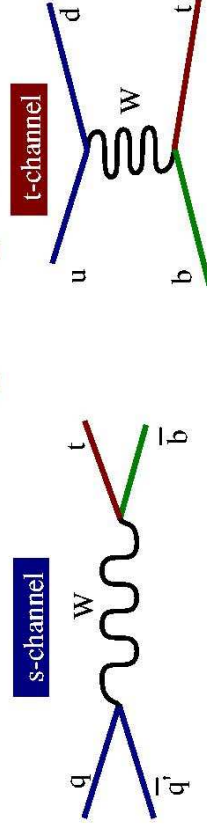
- DØ Run II single top analysis with  $230\text{pb}^{-1}$  completed
  - Detector, trigger, software etc working and understood
  - 95% CL cross section limits of  $\sigma_s < 6.4\text{ pb}$ ,  $\sigma_t < 5.0\text{ pb}$
  - Factor 2 improvement over previous limits
  - Reaching sensitivity to new physics
  - Could discover SM single top with this method with  $\sim 3\text{fb}^{-1}$
- Single Top is an exciting opportunity for Run II
  - New and old (SM) physics
- This is just the beginning
  - Expect x3 dataset by end of year
  - Improve all aspects of the analysis

*Dawn of Run II Discoveries*



Reinhard Schwienhorst, Michigan State University

## Tevatron Single Top Goals



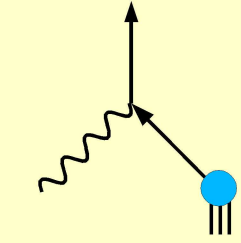
- Observe single top quark production
  - Separately in the s-channel and t-channel
- Measure production cross sections
  - CKM matrix element  $V_{tb}$
- Look for physics beyond the Standard Model
- Study top quark spin correlations – probe V-A
- Irreducible background to associated Higgs production



Reinhard Schwienhorst, Michigan State University

# Mass-Independent Evolution.

# Why is it valid?



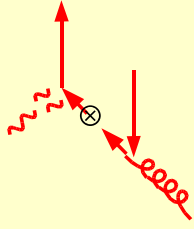
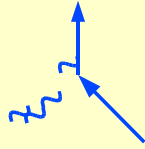
DGLAP equation  
Resums iterative  
splittings inside  
the proton

$$\text{HE} = \int f(P \rightarrow a) \otimes \sigma(a \rightarrow c)$$

$$\frac{df_i}{d \log \mu^2} = \frac{\alpha_s}{2\pi} {}^1P_{j \rightarrow i} \otimes f_j + \dots$$

Splitting Function

$${}^1P_{g \rightarrow q} = \frac{1}{2} [x^2 + (1-x)^2] + \left( \frac{M_H^2}{\mu^2} \right) [x(1-x)]$$



$$\text{HE} = \int \underbrace{f(P \rightarrow a) \otimes \sigma(a \rightarrow c)}$$

$$\approx f(P \rightarrow g) \otimes {}^1P(g \rightarrow a)$$

valid near threshold ( $M_H \sim Q$ )

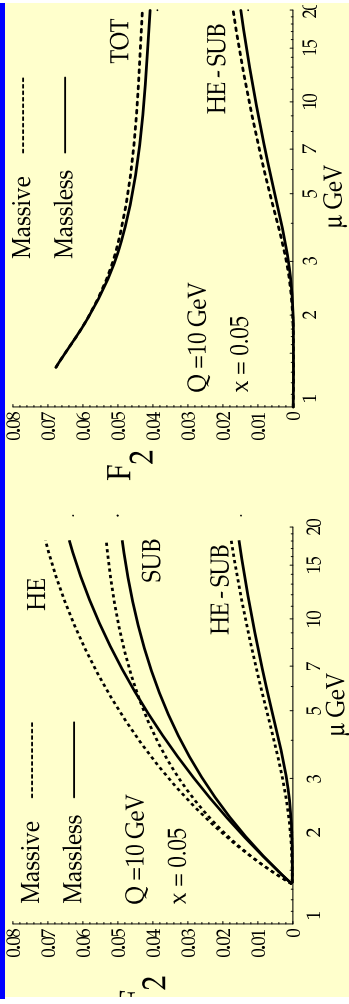
$$\text{SUB} = \int f(P \rightarrow g) \otimes {}^1P(g \rightarrow a) \otimes \sigma(a \rightarrow c)$$

${}^1P$  splittings must match

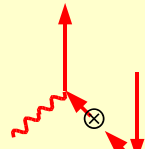
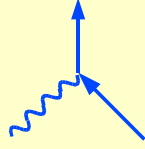
In Summary:

Near threshold ( $M_H \sim Q$ ), mass effects cancel between HE and SUB

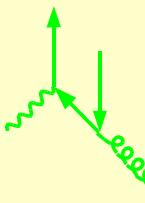
Above threshold ( $M_H \ll Q$ ), mass effects can be ignored



$$\text{HE} = \int f(P \rightarrow a) \otimes \sigma(a \rightarrow c)$$



$$\text{HC} = \int f(P \rightarrow g) \otimes \sigma(g \rightarrow c)$$



$$\text{SUB} = \int f(P \rightarrow g) \otimes {}^1P(g \rightarrow a) \otimes \sigma(a \rightarrow c)$$

# Conclusions

... or, coffee is just around the corner

## An **interesting** subject because:

- Lots of data at present; more in near future
- Theoretical issues of multi-scale problem

## A **fascinating** subject because:

- Theory & data often not consistent
- This should be a region we can compute



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