

Basic Formalism: Cross section



Basic Formalism: Structure Functions











Parton Model results on Structure Functions

$$F_{\lambda}(x,Q^2) \sim \int_0^1 \frac{d\xi}{\xi} \sum_a f_A^a(\xi) \ \widehat{F}_{\lambda}^a(x/\xi,Q^2) + \mathcal{O}(\frac{m}{Q}).$$

where $\hat{F}^a_{\lambda}(z,Q^2)$ is the "partonic structure function" for DIS on the parton target a.

The Feynman diagram contributing to this elementary quantity and the result of a straightforward calculation are (for electro-magnetic coupling case):

 \implies the simple scaling parton model results:

 $\begin{array}{rcl} F_T(x,Q^2) &=& \sum_a \ Q_a^2 \ f_A^a \left(x \right) & (\mathsf{Bj.} \Leftrightarrow \mathsf{Feynman}) \\ F_L(x,Q^2) &=& 0 & (\mathsf{Callan} \Leftrightarrow \mathsf{Gross}) \end{array}$

continued

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Consequences on CC Cross sections (parton model level):

$$\frac{d\sigma^{\nu/\bar{\nu}}}{dxdy} \propto W \cdot L \propto F_{\nu/\bar{\nu}} \left(\frac{1 \pm \cosh\psi}{2}\right)^2$$
$$\cosh\psi = \frac{2-y}{y} \longrightarrow \frac{1 \pm \cosh\psi}{2} \propto \left\{\begin{array}{c}1\\1-y\\\end{array}\right.$$
$$\frac{\sigma^{\bar{\nu}}}{\sigma^{\nu}} = \int dy \frac{d\sigma^{\bar{\nu}}}{dy} / \int dy \frac{d\sigma^{\nu}}{dy} \approx \frac{1}{3}$$

These qualitative features were verified in early (bubble chamber) high energy neutrino scattering experiments. Gargamelle (CERN)

Refined measurements reveal QCD corrections to the approximate naïve parton model results. These are embodies in all modern "QCD fits" and "global analyses". ₃₁



Features of the DIS structure

functions due to SM couplings



At HERA, the γ -Z interference term also contribute, giving rise to more complicated patterns for the "angular" (y) distribution.

Features of the partonic interactions revealed by DIS experiments have firmly established that the lepton probes interact primarily with spin ½ quark partons inside the nucleons with couplings of the SM.

Structure functions: Quark Parton Model Quark parton model (QPM) NC SFs for proton target: $[F_{2}^{\gamma}, F_{2}^{\gamma Z}, F_{2}^{Z}] = x \sum [e_{q}^{2}, 2e_{q}v_{q}, v_{q}^{2} + a_{q}^{2}] \{q + \overline{q}\}$ $[xF_3^{\gamma Z}, xF_3^Z] = 2x \sum_{q} [e_q a_q, v_q a_q] \{q - \overline{q}\} = 2x \sum_{q=u,d} [e_q a_q, v_q a_q] q_v$ QPM CC SFs for proton targets: $xF_{2,W_{\perp}}^{CC} = x\{\overline{u} + \overline{c} + d + s\}, \qquad xF_{3,W_{\perp}}^{CC} = x\{d + s - (\overline{u} + \overline{c})\}$ $xF_{2W}^{CC} = x\{u + c + (\overline{d} + \overline{s})\}, \quad xF_{3W}^{CC} = x\{u + c - (\overline{d} + \overline{s})\}$ For neutron targets, invoke (flavor) isospin symmetry: $u \Leftrightarrow d$ and $\overline{u} \Leftrightarrow \overline{d}$

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Comparing NC and CC Xsec's at HERA: EW Unification H1 e*p NC 94-00 prelim A HI ep NC NC cross section sharply ZEUS e*p NC 99-00 prelim decreases with decreasing ZEUS e p NC 98-99 prelim 1 SM e⁺p NC (CTEO5D) Q^2 (dominant γ exchange): Mein NC (CTEO5D) 10 ~ 1/Q⁴ 10 10 CC cross section approaches H1 e*p CC 94-00 prel H1 ep CC ZEUS e*p CC 99-00 prelim a constant at low Q² ZEUS e'p CC 98-99 prelim. 10 SM e*p CC (CTEQ5D)

dơ/dQ² (pb/GeV²)

10

10

v < 0.9

SM e'n CC (CTEO5D)

10

104

Q² (GeV²)

Dramatic confirmation of the unification of the electromagnetic and weak interactions of the SM in Deep Inelastic Scattering.

 $\sim [M^2_{W}/(Q^2+M^2_{W})]^2$

0.8 10 10 10 10 Q^2 /GeV²



High-Q2 CC cross section from HERA





QCD evolution

Cf. Introductory course

Evolution performed in terms of (1/2/3) non-singlet, singlet and gluon densities:

$$\frac{\partial}{\partial \ln \mu_{t_{i}}^{2}} q_{ns}^{4} = P_{ns}^{4} \otimes q_{ns}^{4}$$

$$\frac{\partial}{\partial \ln \mu_{t_{i}}^{2}} \left\{ \sum_{B}^{A} = \left\{ P_{ns}^{B} - P_{ns}^{A} \right\} \otimes \left\{ \sum_{B}^{D} = P \otimes q \right\}$$
Where
$$P(x) = a_{i}P^{m}(x) + a_{i}^{2} \left[P^{m}(x) - \beta_{i} \ln \frac{\mu_{i}^{2}}{\mu_{i}^{4}} P^{m}(x) \right] \quad \text{with} \quad a_{i} = \frac{\alpha_{i}(\mu_{i}^{2})}{4\pi}$$

$$\frac{da_{i}}{d \ln \mu_{e}^{4}} = \beta(a_{i}) = \sum_{a}^{a_{i}^{*}} \beta_{i}^{*} \approx a_{i}^{2} \beta_{i} + a_{i}^{2} \beta_{i} \quad \text{where} \quad \beta_{i} = 112 - \frac{3}{3} N_{i}$$
and $\beta_{i} = 102 - \frac{38}{3} N_{i}$

$$\frac{da_{i}}{d \ln \mu_{e}^{4}} = \beta(a_{i}) = \sum_{a}^{a_{i}^{*}} \beta_{i}^{*} \approx a_{i}^{2} \beta_{i} + a_{i}^{2} \beta_{i} \quad \text{where} \quad \beta_{i} = 112 - \frac{3}{3} N_{i}$$

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Parton Distribution Functions (PDF):

most significant physical results derived from DIS

(with help from other hard scattering processes)