

Cosmological Relaxation of the Electroweak Scale

with P. Graham and D. E. Kaplan

arXiv: 1504.07551

the Relaxion

The Hierarchy Problem

The Higgs mass in the standard model is sensitive to the ultraviolet.

Two approaches to explain:

- New symmetry or new dynamics realized at the electroweak scale. (SUSY, composite Higgs, EOFT)
- An anthropic explanation for fine tuning of ultraviolet parameters. (Multiverse)

We Propose: A **Dynamical** Solution

- Higgs mass-squared promoted to a field.
- The field evolves **in time** in the early universe.
- The mass-squared relaxes to a small negative value.
- The electroweak symmetry breaking stops the **time-dependence**.
- The small electroweak scale is fixed **until today**.

Elements of a Dynamical Solution



Initial Formation



State after millions of years of erosion

- Time evolution important
- Dissipation - eroded sand needs to go somewhere
- Every point along the way is stable - just that the flat surface is much more stable

Caveats

The solution:

- is only technically natural.
- requires large field excursions (larger than the scale that cuts off loops).
- requires a very long period of inflation.
- can only push the cutoff up to 10^8 GeV.

Simplest Model

Standard Model plus QCD axion

$$\mathcal{L} \supset (-M^2 + g\phi)|h|^2 \quad \dots + \frac{\phi}{32\pi^2 f} G^{\mu\nu} \tilde{G}_{\mu\nu}$$

M cuts off SM
loops.

Continuous shift symmetry
broken completely by g .

The axion here is non-compact.

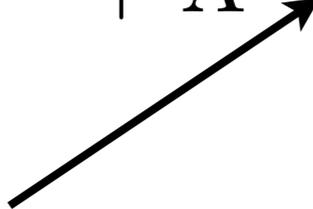
(The Abbott model with a coupling to the Higgs & QCD)

Simplest Model

Standard Model plus QCD axion

$$\mathcal{L} \supset (-M^2 + g\phi)|h|^2 + gM^2\phi + g^2\phi^2 + \dots + \Lambda^4 \cos \frac{\phi}{f}$$

Continuous shift symmetry
broken to discrete by non-
perturbative effects.

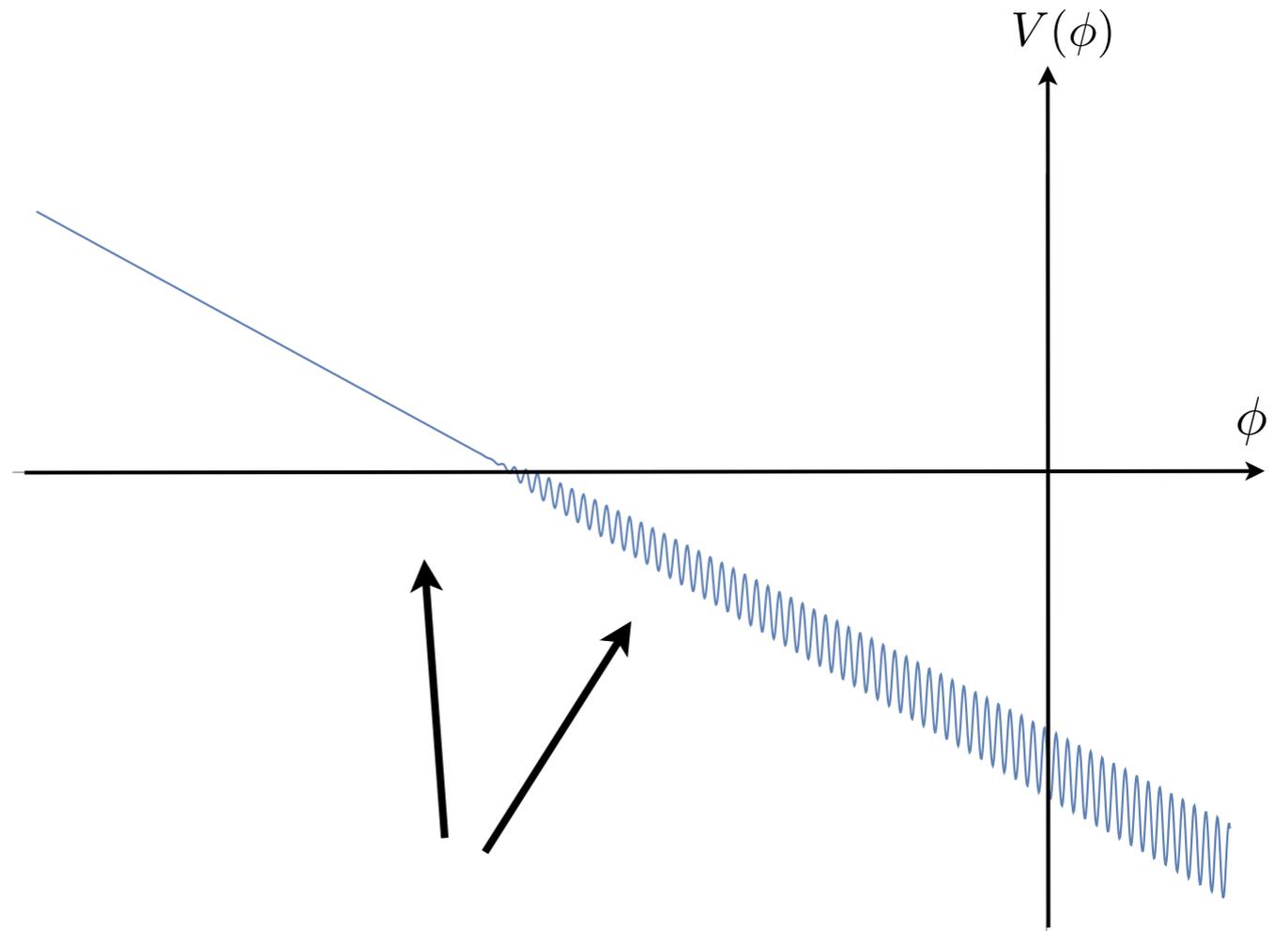


Conservative effective field theory regime: $\phi \lesssim \frac{M^2}{g}$

(Assuming expansion of $V(g\phi)$ in powers of $\left(\frac{g\phi}{M^2}\right)$)

Chronology

- Take initial ϕ value such that $m_h^2 > 0$
- During inflation, ϕ slow-rolls, scanning physical Higgs mass.
- ϕ hits value where $\sim m_h^2$ crosses zero.
- Barriers grow until rolling has stopped.



Key: Barriers grow because they depend on the Higgs vev.

Higgs vev and the Periodic Potential

Barrier height (axion potential) can be approximated in the chiral Lagrangian (2 flavors):

$$V_{\text{axion}} \left(\frac{\phi}{f} \right) \sim \Lambda^4 \cos \frac{\phi}{f}$$

Around the normal EW scale: $\Lambda^4 \sim f_\pi^2 m_\pi^2 \left(\frac{\min(m_u, m_d)}{m_u + m_d} \right)$

$$m_\pi^2 \propto (y_u + y_d) \langle h \rangle$$

Barrier height grows with the Higgs vev.

Parameter Requirements

ϕ stops rolling and Higgs vev stops growing when slope turns around:

$$\partial_{\phi}(gM^2\phi + \Lambda^4 \cos(\phi/f)) \sim 0$$

or

$$gM^2 f \sim \Lambda^4$$

$$\Lambda \sim 100 \text{ MeV}$$

fixed parameters

changes with Higgs vev

$$gM^2 f \sim f_{\pi}^2 \mu (y_u + y_d) \langle h \rangle$$

Parameter Requirements

1) Vacuum energy density during inflation $> M^4$

$$H_{\text{infl}} > \frac{M^2}{M_{\text{pl}}}$$

2) Classical rolling dominates: $\frac{\dot{\phi}}{H_{\text{infl}}} > H_{\text{infl}}$

$$H_{\text{infl}}^3 < gM^2$$

Plugging in for g , and using 1) and 2):

$$M^6 < \frac{\Lambda^4 M_{\text{pl}}^3}{f}$$

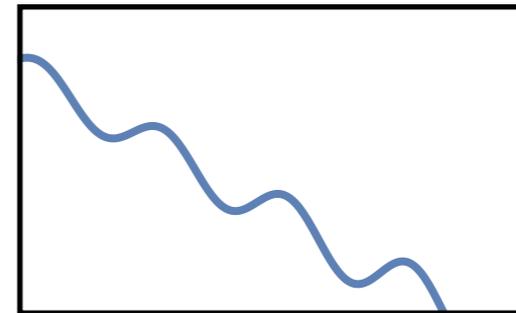
Bound on cutoff...

$$M < 10^7 \text{ GeV} \left(\frac{10^9 \text{ GeV}}{f} \right)^{1/6}$$

However,...

$$gM^2 f \sim \Lambda^4$$

$$\theta_{\text{QCD}} \simeq \pi/2$$



Prediction: $d_n \simeq \text{few} \times 10^{-16} e \text{ cm}$

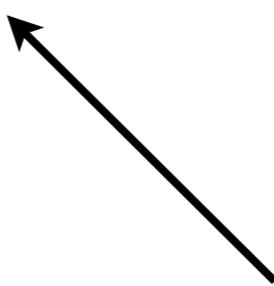
Solve Strong CP (1)

Usual solutions don't quite work.

Dynamical one -- Drop the slope:

$$\mathcal{L} \supset (-M^2 + g\phi)|h|^2 + \kappa\sigma^2\phi + gM^2\phi + \dots + \Lambda^4 \cos \frac{\phi}{f}$$

inflaton - drops at end of inflation



$$gM^2 \simeq \theta \times \kappa\sigma^2 \quad \longrightarrow \quad \begin{aligned} gM^2 f &\sim \theta \Lambda^4 \\ H_{\text{infl}} &> \theta^{-\frac{1}{2}} \frac{M^2}{M_{\text{pl}}} \\ H_{\text{infl}}^3 &< \theta^{-1} gM^2 \end{aligned}$$

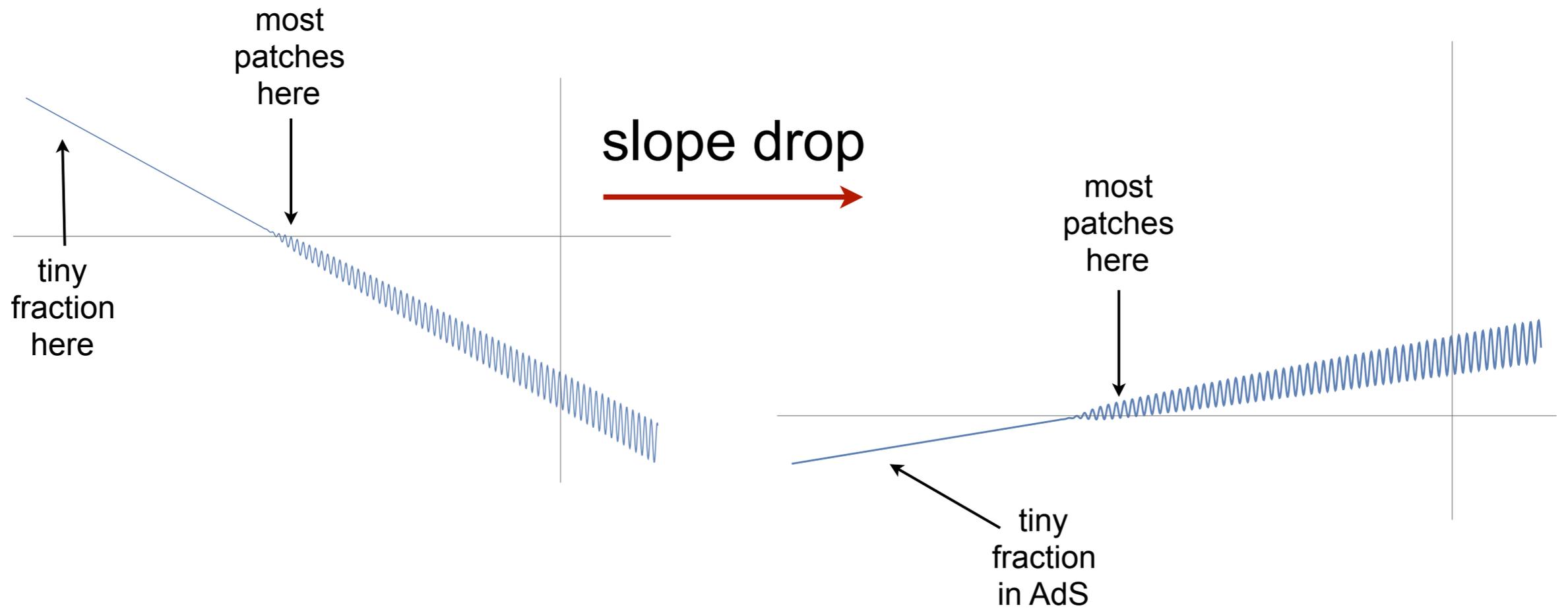
Bound on cutoff!

$$M^6 < \theta^{\frac{3}{2}} \frac{\Lambda^4 M_{\text{pl}}^3}{f}$$

or

$$M < 30 \text{ TeV} \left(\frac{\theta}{10^{-10}} \right)^{\frac{1}{4}} \left(\frac{10^9 \text{ GeV}}{f} \right)^{\frac{1}{6}}$$

Quantum vs. Classical evolution



If we remove this constraint, upper bound on Hubble comes from requiring barriers to form:

$$H_{\text{infl}} < \Lambda$$

Weaker bound on cutoff!

$$M^2 < \theta^{\frac{1}{2}} \Lambda M_{\text{pl}}$$

or

$$M < 1000 \text{ TeV} \left(\frac{\theta}{10^{-10}} \right)^{\frac{1}{4}}$$

Solve Strong CP (2)

(Model 2)

Use a different strong group and couple ϕ to $G'^{\mu\nu} \tilde{G}'_{\mu\nu}$.

The Higgs must change the barrier heights: Add fermions

$$\begin{array}{cc} & \underline{SU(3)} \\ L, N & \square \\ L^c, N^c & \bar{\square} \end{array}$$

$$\mathcal{L} \supset m_L L L^c + m_N N N^c + y h L N^c + \tilde{y} h^\dagger L^c N$$

Require Higgs vev to be dominant contribution to m_N

Radiative naturalness $\Rightarrow m_L < 600$ GeV

$m_L > 250$ GeV from LHC

Bound on cutoff (Model 2)

$$M < (\Lambda^4 M_{\text{pl}}^3)^{\frac{1}{7}} \left(\frac{M}{f} \right)^{\frac{1}{7}}$$

or

$$M < 3 \times 10^8 \text{ GeV} \left(\frac{f_{\pi'}}{30 \text{ GeV}} \right)^{\frac{3}{7}} \left(\frac{y\tilde{y}}{10^{-2}} \right)^{\frac{1}{7}} \left(\frac{250 \text{ GeV}}{m_L} \right)^{\frac{1}{7}} \left(\frac{M}{f} \right)^{\frac{1}{7}}$$

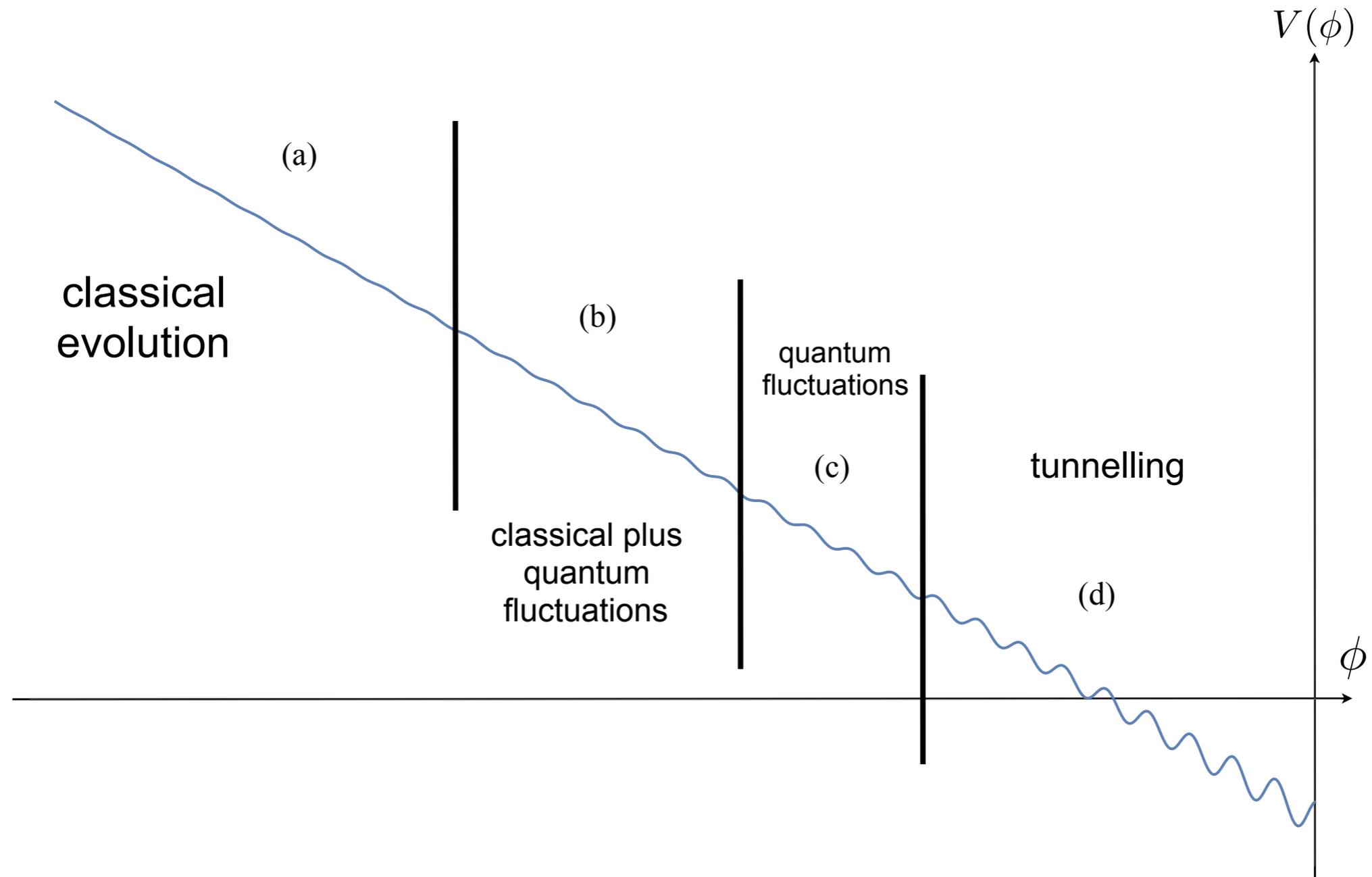


Bounds from Higgs decays, EWP



Constraints weaker due to loops

End of Roll



Need to end up in vacua that
lives longer than the age of the
universe since reheating

Inflation

To achieved the relaxed value,
inflation has to last long enough:

$$\Delta\phi \sim \frac{\dot{\phi}}{H_{\text{infl}}} N \sim \frac{\partial_{\phi} V}{H_{\text{infl}}^2} N \sim \frac{gM^2}{H_{\text{infl}}^2} N$$

We require:

$$\Delta\phi \gtrsim \left(\frac{M^2}{g} \right)$$

$$N \gtrsim \frac{H_{\text{infl}}^2}{g^2} \sim 10^{48}, 10^{37} \quad (\text{Model 1,2 saturated})$$

Inflation

Single field: $V(\Phi) = m^2 \Phi^2$

$$N = \int H dt \sim \int \frac{H^2}{\partial_\Phi V} d\Phi \sim \frac{\Phi_i^2}{M_{\text{pl}}^2}$$

Classical rolling:

$$\frac{\dot{\Phi}}{H_{\text{infl}}} < H_{\text{infl}} \longrightarrow \frac{m\Phi_i^2}{M_{\text{pl}}^3} < 1 \longrightarrow V(\Phi_i) < \frac{M_{\text{pl}}^4}{N}$$

$$\longrightarrow N < \left(\frac{M_{\text{pl}}}{M}\right)^4 (\times \theta)$$

$$N \gtrsim \frac{H_{\text{infl}}^2}{g^2} \longrightarrow M < 10^5, 10^{8.75} \text{ GeV}$$

Reheating requires additional dynamics (e.g., hybrid)

Observables

QCD model: Small parameter space

- (Rel)axion: May be dark matter, **with different abundance prediction from vacuum misalignment.**
- Observable neutron EDM favored.
- **Coupling to the Higgs:** (tiny)
 - New force experiments
 - Background oscillations of SM mass scales (if DM)
- Low-scale inflation (no primordial tensor modes in the CMB)

Low energy precision
measurements to test this solution
to the hierarchy problem!

Observables

non-QCD model: weak-scale physics

- (Rel)Axion: Still be dark matter, with different abundance prediction from vacuum misalignment, **as well as mass prediction/couplings**
- **Fermions with electroweak quantum numbers**
- Coupling to the Higgs:
 - **New force experiments**
 - **Oscillations of SM mass scales, e.g. m_e (if DM)**
- Low-scale inflation (no primordial tensor modes in the CMB)

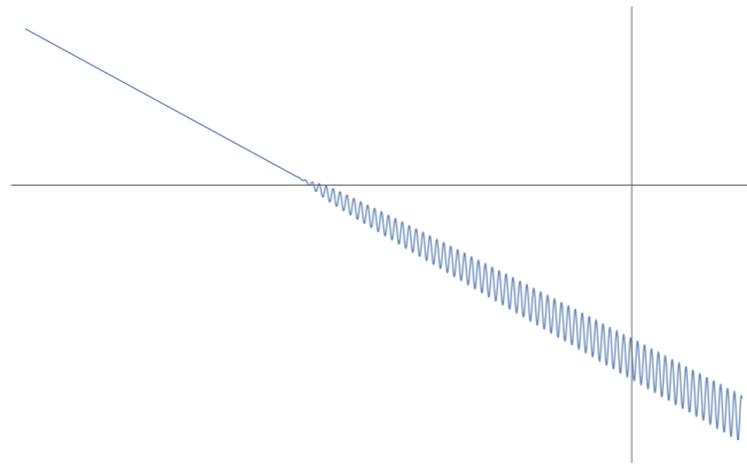
Low energy precision
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Relaxion Conditions

$$\mathcal{L} \supset (-M^2 + g\phi)|h|^2 + gM^2\phi + g^2\phi^2 + \dots + \Lambda^4 \cos \frac{\phi}{f}$$

Self-organized criticality?

- Dissipation - Dynamical evolution of Higgs mass (field) must stop. **Hubble friction.**
- Self-similarity - Cutoff-dependent quantum corrections will choose an arbitrary point where the Higgs mass is cancelled. **Periodic axion.**



- Higgs back-reaction - EWSB must stop the evolution at the appropriate value. **Yukawa couplings.**
- Long time period - There must be a sufficiently long time period during the early universe for scanning. **Inflation.**

To Do

- Phenomenology:
 - Dark matter / cosmological predictions
 - Collider predictions
 - New forces
- New low-energy experimental ideas (CASPEr)
- UV completion (axion monodromy?)
- Better Inflation models
- Better models/higher cutoff