

The Unnatural (or Split) Composite Higgs

Tony Gherghetta
University of Minnesota

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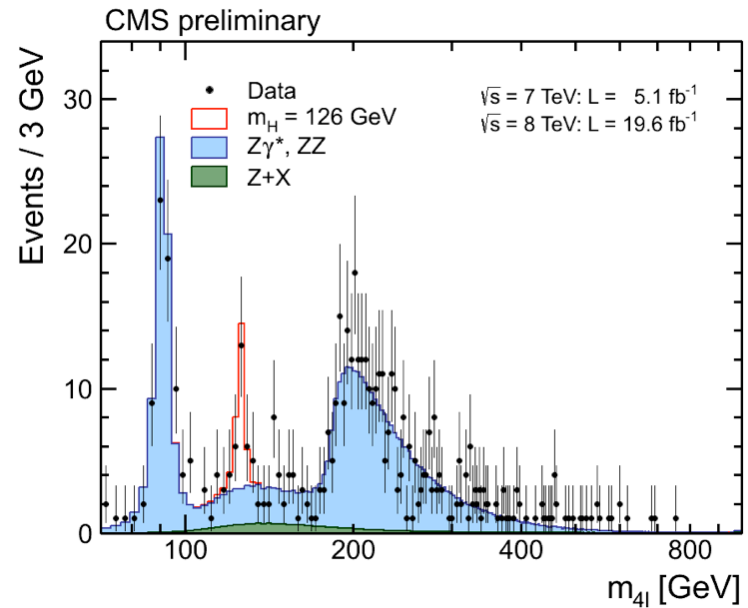
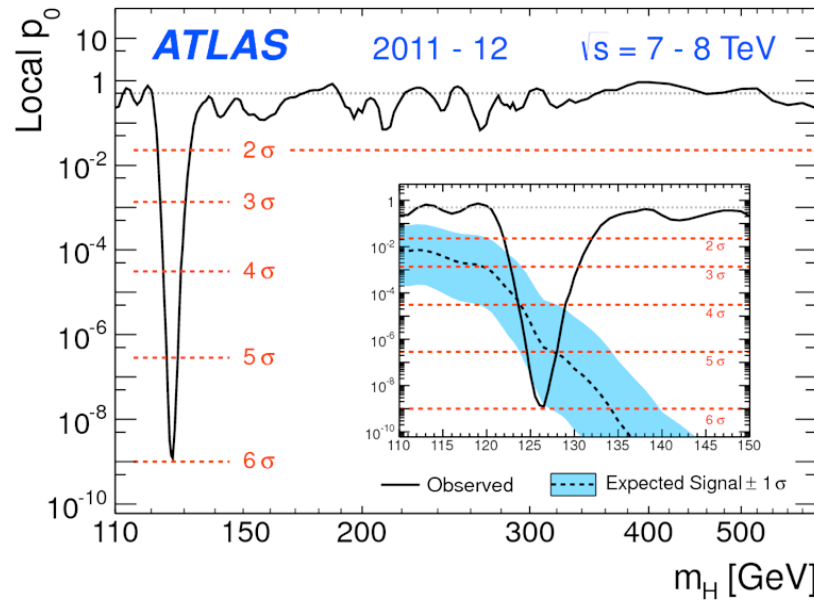
[James Barnard, TG, Tirtha Sankar Ray, Andrew Spray: 1409.7391]

[James Barnard, Peter Cox, TG, Andrew Spray: 1510.06405]

Outline

- Introduction and motivation
- The “unnatural” composite Higgs
- Experimental signals of unnaturalness
- Conclusion

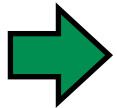
Higgs discovery - LHC Run I



Higgs potential: $V(h) = -\mu_h^2 |H|^2 + \lambda_h |H|^4$ $\langle H \rangle = \frac{1}{\sqrt{2}}(v + h)$

$$v^2 = \frac{\mu_h^2}{\lambda_h} \simeq (246 \text{ GeV})^2$$

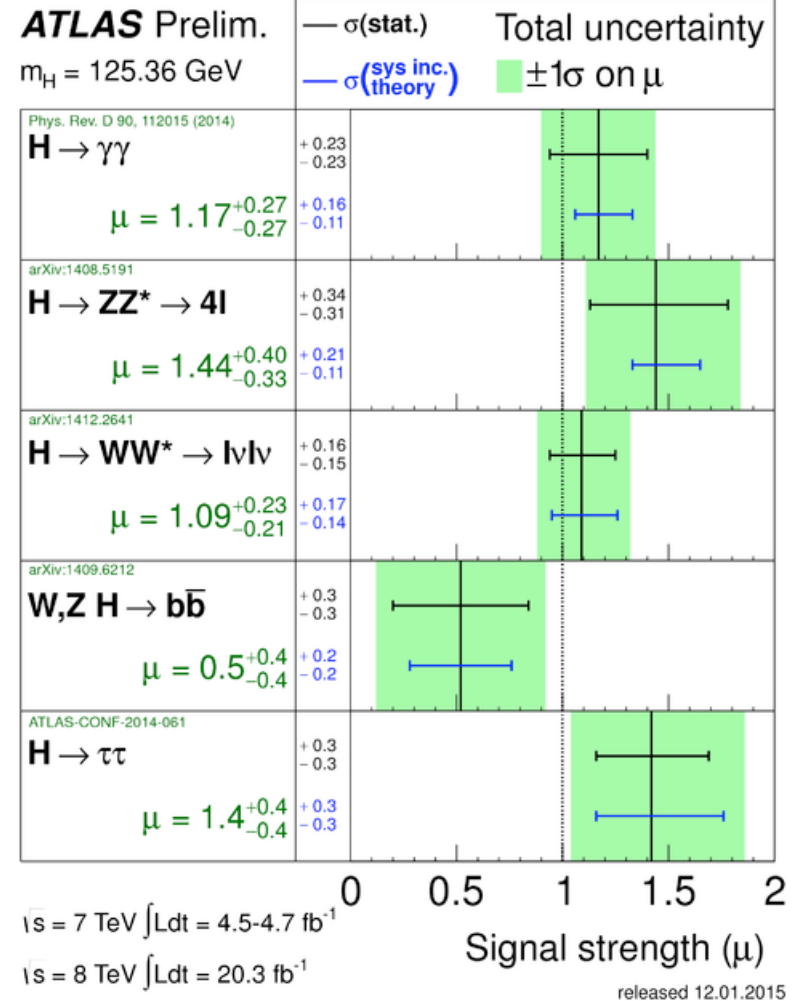
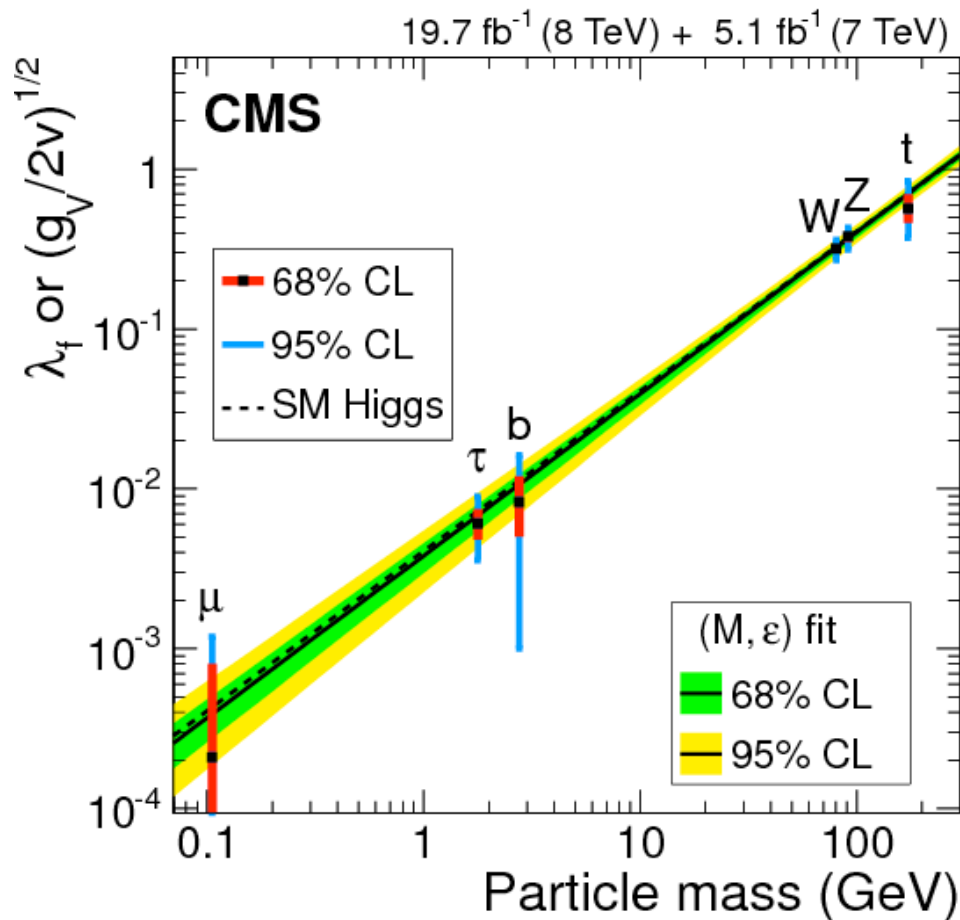
$$m_h^2 = 2\lambda_h v^2 \simeq (126 \text{ GeV})^2$$



$$\mu_h^2 \simeq (89 \text{ GeV})^2$$

$$\lambda_h \simeq 0.13$$

Higgs couplings



➡ Looks very much like a SM Higgs boson!

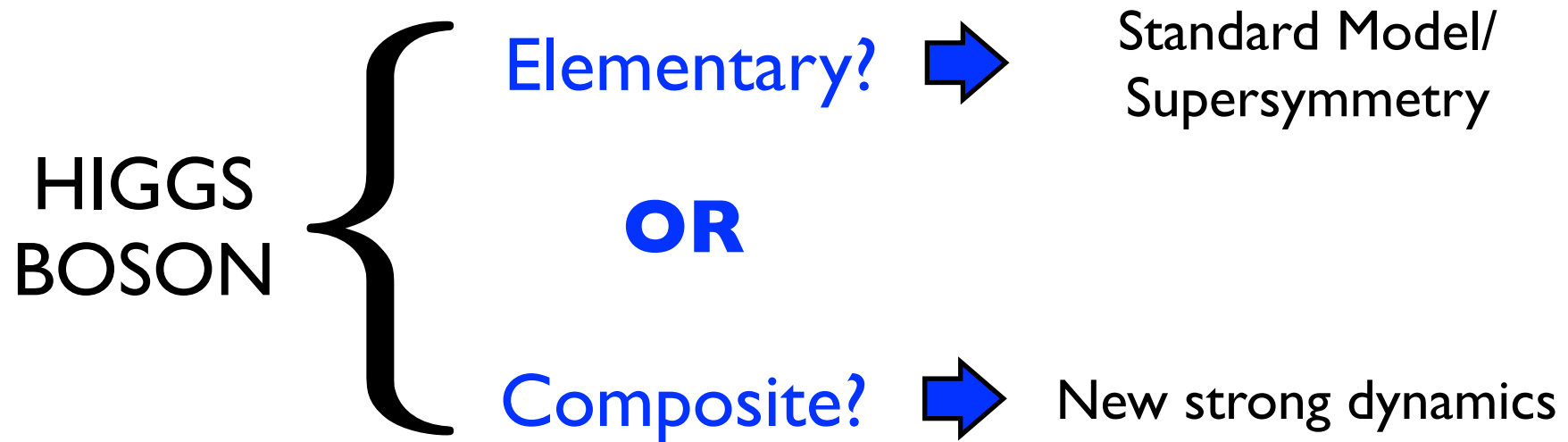
However, SM is **not** a complete theory of Nature!

Questions:

- Planck/weak scale hierarchy? ($m_h \ll M_p$)
- Fermion mass hierarchy? Neutrino masses?
- GUTS? 3 fermion generations?
- Dark matter?
- Baryon asymmetry?
- Strong CP problem?
- Inflaton? Cosmological constant?
- UV completion of gravity?



What is the nature of the Higgs boson?

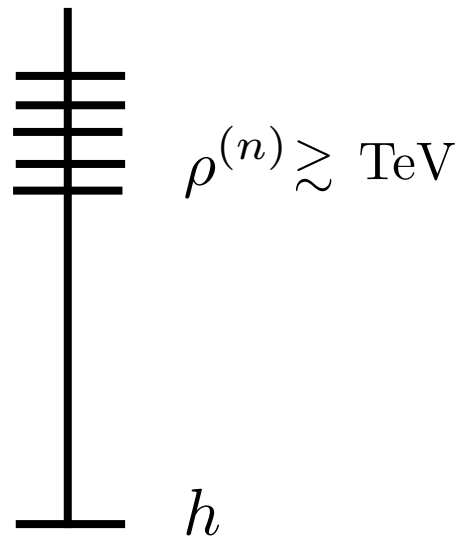


Understanding why $m_h \ll M_p$ can help
address shortcomings in the SM

Composite Higgs

Higgs as a pseudo Nambu-Goldstone boson [Georgi, Kaplan '84]

Global symmetry G spontaneously broken to subgroup H at scale f



Resonance mass: $m_\rho \sim g_\rho f$ $1 \lesssim g_\rho \lesssim 4\pi$

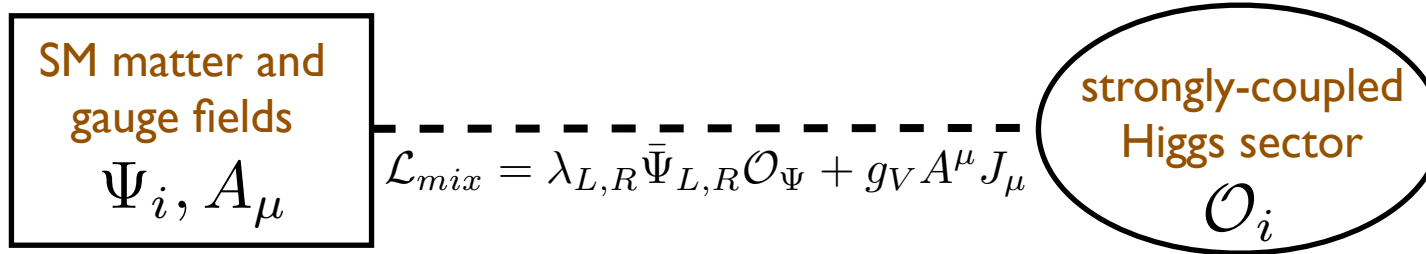
coset $G/H \supset h$

Higgs mass protected by shift symmetry
-- like pions in QCD

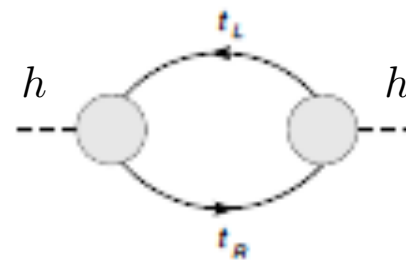
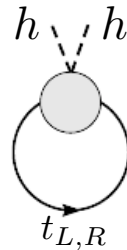
BUT global symmetry must be explicitly broken to generate $V(h) \neq 0$

Global symmetry broken by mixing with elementary sector

[Contino, Nomura, Pomarol '03; Agashe, Contino, Pomarol '04]



Higgs potential:



$$V(h) = -\mu_h^2 |H|^2 + \lambda_h |H|^4 \quad \text{where} \quad \mu_h^2 \sim \frac{g_{SM}^2}{16\pi^2} g_\rho^2 f^2 \quad \lambda_h \sim \frac{g_{SM}^2}{16\pi^2} g_\rho^2$$

$$\text{EWSB} \left(\langle H \rangle = \frac{v}{\sqrt{2}} \right) \quad v^2 = \frac{\mu_h^2}{\lambda_h} \quad \Rightarrow \quad \text{Prefers: } f \sim v$$

Higgs mass: $m_h^2 \simeq \frac{N_c}{\pi^2} m_t^2 \frac{m_Q^2}{f^2} = g_Q^2$



m_Q = fermion resonance mass

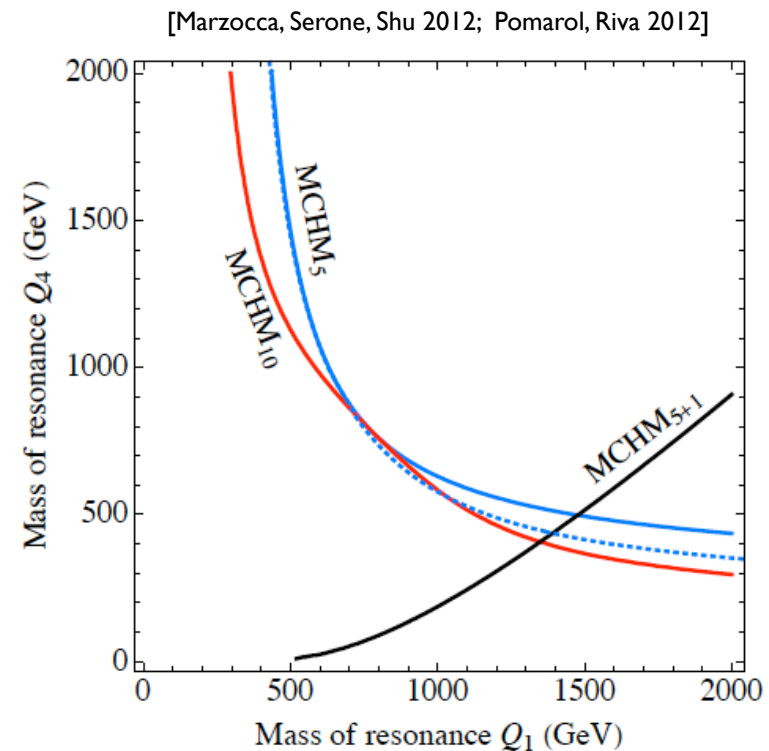
$m_Q \sim m_\rho \gtrsim 2.5 \text{ TeV} \quad (g_Q \sim g_\rho \gtrsim 3) \quad \Rightarrow \quad m_h \gtrsim m_t$

But, no need for $m_Q \sim m_\rho$

$m_h \sim 125 \text{ GeV}$

$\Rightarrow m_Q < m_\rho$

light fermion resonances!



HOWEVER, precision electroweak, flavor constraints

EWPT: $\frac{s}{16\pi^2 v^2} H^\dagger \tau^a H B^{\mu\nu} W_{a\mu\nu} \quad S = \frac{s}{2\pi} \sim \frac{m_W^2}{m_\rho^2} \quad \Rightarrow \quad f \gtrsim \frac{2.5 \text{ TeV}}{g_\rho}$

$\frac{-t}{16\pi^2 v^2} ((D^\mu H)^\dagger H)(H^\dagger D_\mu H) \quad T = \frac{t}{8\pi e^2} \sim \frac{v^2}{f^2} \quad \Rightarrow \quad f \gtrsim 5.5 \text{ TeV}$

e.g. FCNC $\epsilon_q^i \epsilon_q^j \epsilon_q^k \epsilon_q^l \frac{g_\rho^2}{m_\rho^2} \bar{q}^i q^j \bar{q}^k q^l \quad \epsilon_q^i \sim \frac{g_i}{g_\rho} \quad \Rightarrow \quad f \gtrsim 10 \text{ TeV}$

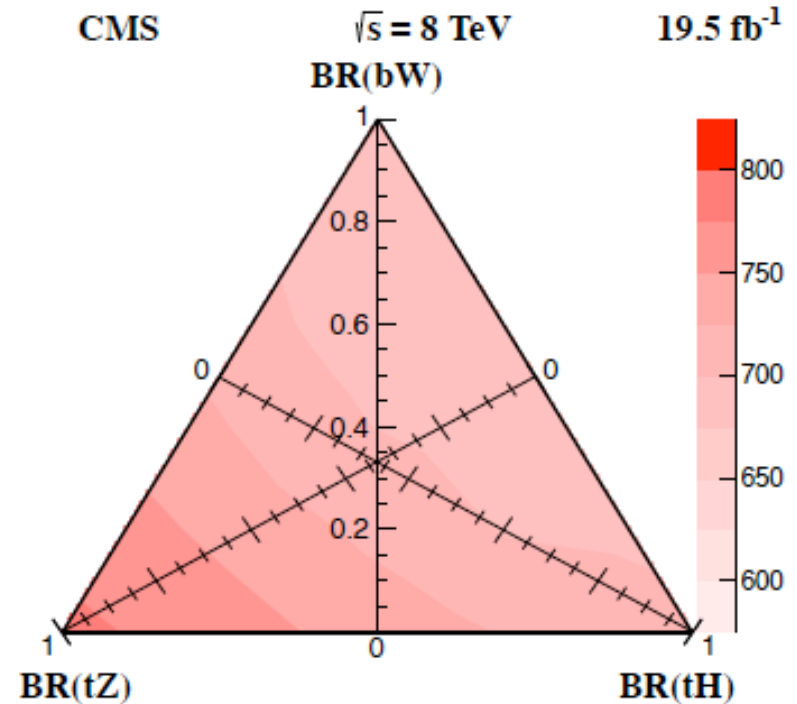
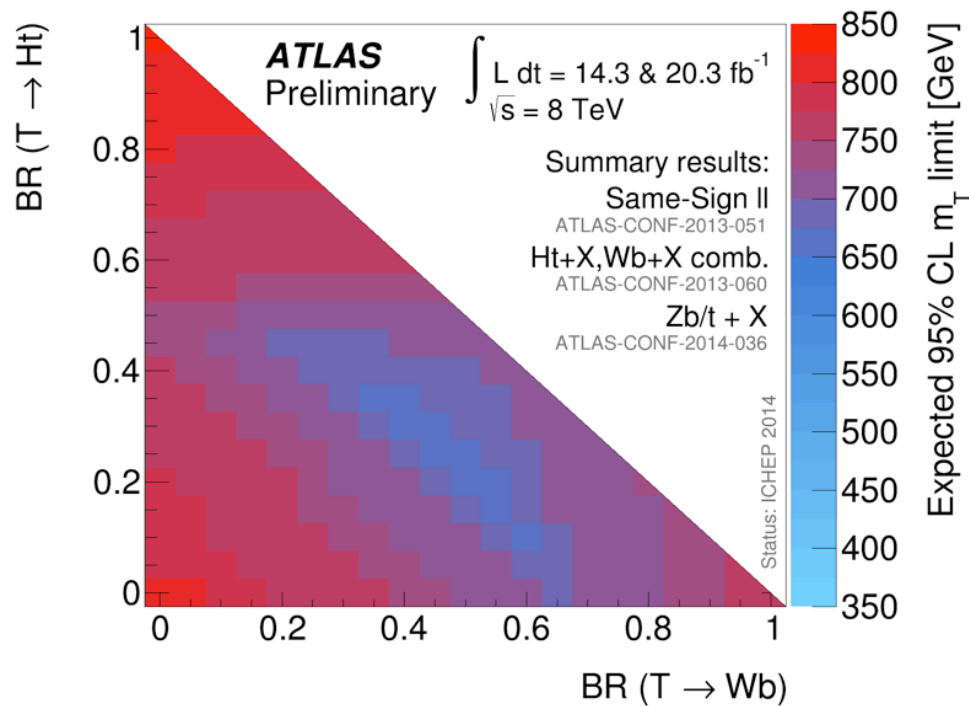
[Bellazzini, Csaki, Serra 1401.2457]
[Panico, Wulzer 1506.01961]

$\Rightarrow \quad f \gg v \quad \text{“Little” hierarchy}$

Tension partly alleviated by complicating minimal models

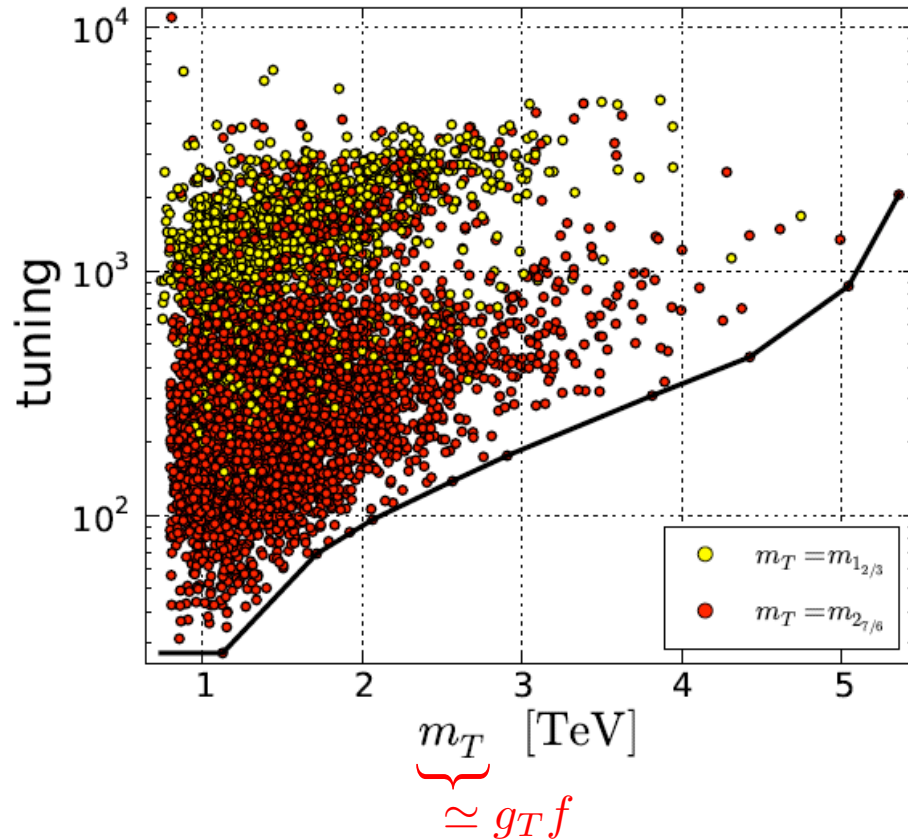
e.g. custodial symmetry, flavor symmetry....

LHC Limits: *The Missing Resonances Problem*

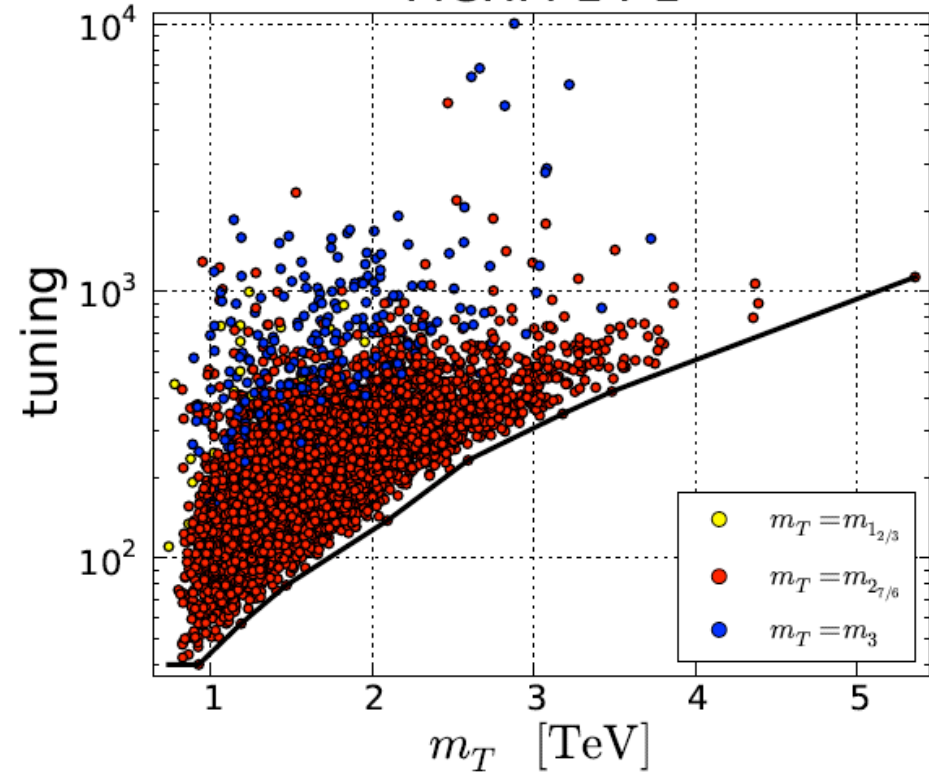


➡ $m_T \gtrsim 600 - 800 \text{ GeV}$

MCHM 5-5



MCHM 14-1



“Natural” models increasingly elaborate

and tuned: $\Delta^{-1} \sim \frac{v^2}{f^2} \lesssim 5\%$

Simple solution:

Assume

$$f \gtrsim 10 \text{ TeV}$$

– no need for custodial or flavor symmetries!

Tuned Higgs potential

$$V \sim c_2 f^2 |H|^2 + c_4 |H|^4$$

tuning $\frac{v^2}{f^2} \lesssim 10^{-4}$

This compares to $\sim 10^{-28}$ in SM!

e.g. QCD - sensitivity in neutron, proton mass $\frac{m_{u,d}}{m_{nucleon}} \sim 10^{-3}$

Is there a motivated upper bound for f ?

Yes!



Partial compositeness:

$$\mathcal{L} = \lambda_L \psi_L \mathcal{O}_R + \lambda_R \psi_R \mathcal{O}_L$$

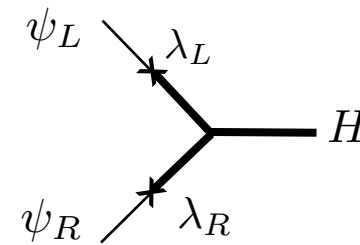
Explains the fermion mass hierarchy

[Kaplan 91; TG, Pomarol 00]

$$m_f \sim \lambda_L \lambda_R v$$

where

$$\lambda_{L,R} \sim \left(\frac{\Lambda}{\Lambda_{UV}} \right)^{\dim \mathcal{O}_{L,R} - \frac{5}{2}}$$



- Light fermions are mostly elementary $\Rightarrow \dim \mathcal{O}_{L,R} > \frac{5}{2}$
- Top quark is mostly composite! $\Rightarrow \dim \mathcal{O}_{L,R} \sim \frac{5}{2}$

Gauge coupling unification

[Agashe, Contino, Sundrum '05]

Assume composite t_R and coset $\mathcal{G}/\mathcal{H}$

$(t_R, \chi^c) =$ complete $\mathcal{H}$ multiplet

Decoupled with top “companions” χ Dirac mass: $m_\chi \sim \lambda_\chi f$

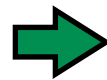
New contribution to the running of SM gauge couplings

$$\alpha_i(\mu) - \alpha_j(\mu) = \text{SM} - \underbrace{\{H, t^c\}}_{\text{composite Higgs, top}} \overset{\text{top “companions” contribution}}{\bar{t}^c}$$

One-loop beta function coefficients:

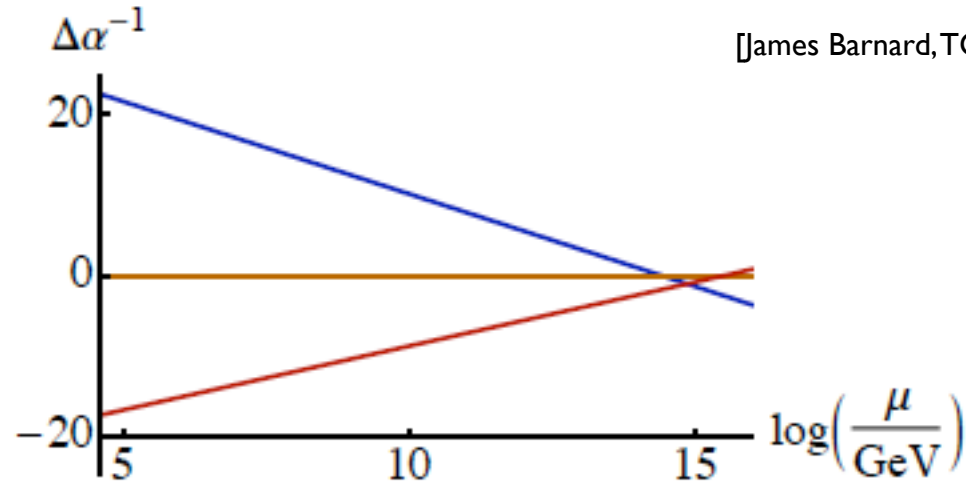
$$b_1 - b_2 = \frac{94}{15}$$

$$b_2 - b_3 = \frac{13}{3}$$

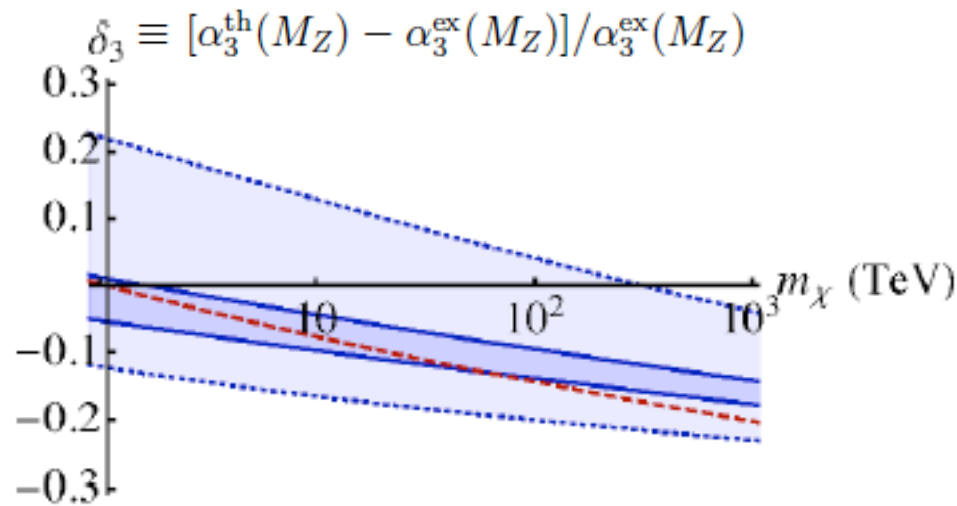


$$\frac{b_2 - b_3}{b_1 - b_2} \simeq 0.69$$

c.f. MSSM value = 0.71



$$\frac{d}{d\ln\mu} \left(\frac{1}{\alpha_i} \right) = \frac{b_i}{2\pi} + \frac{B_{ij}}{2\pi} \frac{\alpha_j}{4\pi} + \frac{C_{i\alpha}}{2\pi} \frac{\lambda_\alpha^2}{16\pi^2}$$

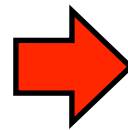


$$B_{\text{strong}} \sim 9b_{\text{strong}}$$

$$C \sim 3\lambda_\chi b_{\text{strong}}$$

$$b_{\text{strong}} = 1, 5$$

Requiring $\delta_3 = 0$
($b_{\text{strong}} = 5$)



$$f \lesssim 500 \text{ TeV}$$

Minimal Coset: $SU(7)/SU(6) \times U(1)$

[James Barnard, TG, Tirtha Sankar Ray, Andrew Spray: 1409.7391]

- contains $SU(5)$ --universal corrections to running
- scalar singlet dark matter [Frigerio, Pomarol, Riva, Urbano 1204.2808]

$$w = e^{i\Pi} \begin{pmatrix} 0_{(6)} \\ 1 \end{pmatrix} = \frac{1}{f} \begin{pmatrix} H \\ S \\ \sqrt{f^2 - |H|^2 - |S|^2} \end{pmatrix}$$

12 Nambu-Goldstone bosons

$$= \underbrace{\mathbf{5}}_{\text{Higgs doublet, D}} \text{ of } SU(5) + \underbrace{\mathbf{1}}_{=S} \text{ singlet}$$

H = Higgs doublet, D + $SU(3)$ triplet, T

Matter embeddings

SM matter embedding under $SU(5) \times U(1)_L \times U(1)_B$

$$q \in \mathbf{10}_{0, \frac{1}{3}} \quad u^c \in \mathbf{10}_{0, -\frac{1}{3}} \quad d^c \in \bar{\mathbf{5}}_{0, -\frac{1}{3}} \quad e^c \in \mathbf{10}_{-1, 0} \quad l \in \bar{\mathbf{5}}_{1, 0}$$

Composite top $t_R \subset \mathbf{15}$ of $SU(6)$

➡ Top companions $\chi \subset \bar{\mathbf{15}}$

$$\chi \equiv \tilde{q}^c \oplus \tilde{e} \oplus \tilde{d}^c \oplus \tilde{l} = (\bar{\mathbf{3}}, \mathbf{2})_{-\frac{1}{6}} \oplus (\mathbf{1}, \mathbf{1})_{-1} \oplus (\bar{\mathbf{3}}, \mathbf{1})_{\frac{1}{3}} \oplus (\mathbf{1}, \mathbf{2})_{-\frac{1}{2}}$$

Mixing Lagrangian

$$\begin{aligned} \mathcal{L} \supset & (\tilde{q}^c, \tilde{e}) \lambda_\chi^{\mathbf{10}} \mathcal{O}_t^{\mathbf{35}} + (\tilde{d}^c, \tilde{l}) \lambda_\chi^{\mathbf{5}} \mathcal{O}_t^{\mathbf{35}} + q \lambda_t \mathcal{O}_t^{\mathbf{35}} + q \lambda_b \mathcal{O}_b^{\bar{\mathbf{35}}} + b^c \lambda_{b^c} \mathcal{O}_{b^c}^{\mathbf{35}} \\ & + l \lambda_\nu \mathcal{O}_\nu^{\mathbf{21}} + l \lambda_\tau \mathcal{O}_\tau^{\mathbf{21}} + N^c \lambda_{N^c} \mathcal{O}_{N^c}^{\bar{\mathbf{21}}} + \tau^c \lambda_{\tau^c} \mathcal{O}_{\tau^c}^{\bar{\mathbf{21}}} + m_N N^c N^c \end{aligned}$$

Effective Lagrangian

Integrate out strong sector

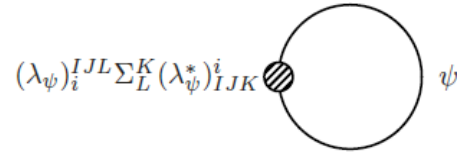
$$\begin{aligned}
 \mathcal{L}_{\text{eff}} \supset & (\bar{q}^c, \bar{e})_{i_4 i_2} \not{p}(\tilde{q}^c, \tilde{e})^{j_4 j_2} \left[\Pi^{\chi\chi}(\lambda_\chi^{10*})_{IJK}^{i_4 i_2}(\lambda_\chi^{10})_{j_4 j_2}^{IJL} \right] \Sigma_L^K \\
 & + (\bar{q}^c, \bar{e})_{i_4 i_2} \not{p}(\tilde{d}^c, \tilde{l})^{j_5} \left[\Pi^{\chi\chi}(\lambda_\chi^{10*})_{IJK}^{i_4 i_2}(\lambda_\chi^5)_{j_5}^{IJL} \right] \Sigma_L^K + \text{h.c.} \\
 & + (\tilde{d}^c, \tilde{l})_{i_5} \not{p}(\tilde{d}^c, \tilde{l})^{j_5} \left[\Pi^{\chi\chi}(\lambda_\chi^{5*})_{IJK}^{i_5}(\lambda_\chi^5)_{j_5}^{IJL} \right] \Sigma_L^K \\
 & + \bar{q}^{i_3 i_2} \not{p} q_{j_3 j_2} \left[\Pi^{tt}(\lambda_t^*)_{i_3 i_2, IJK}(\lambda_t)^{j_3 j_2, IJL} + \Pi^{bb}(\lambda_b^*)_{i_3 i_2}^{IJL}(\lambda_b)^{j_3 j_2}_{IJK} \right] \Sigma_L^K \\
 & + \bar{b}_{i_3}^c \not{p} b^{c j_3} \left[\Pi^{b^c b^c}(\lambda_{b^c}^*)_{IJK}^{i_3}(\lambda_{b^c})_{j_3}^{IJL} \right] \Sigma_L^K \\
 & + (\bar{q}^c, \bar{e})_{i_4 i_2} \not{p} q_{j_3 j_2} \left[\Pi^{\chi t}(\lambda_\chi^{10*})_{IJK}^{i_4 i_2}(\lambda_t)^{j_3 j_2, IJL} \right] \Sigma_L^K + \text{h.c.} \\
 & + (\tilde{d}^c, \tilde{l})_{i_5} \not{p} q_{j_3 j_2} \left[\Pi^{\chi t}(\lambda_\chi^{5*})_{IJK}^{i_5}(\lambda_t)^{j_3 j_2, IJL} \right] \Sigma_L^K + \text{h.c.} \\
 & + q_{i_3 i_2} b^{c j_3} \left[M^{bb^c}(\lambda_b)_{IJK}^{i_3 i_2}(\lambda_{b^c})_{j_3}^{IJL} \right] \Sigma_L^K + \text{h.c.}
 \end{aligned}$$

where $\Sigma = w^\dagger w$ = adjoint spurion (contains D, T and S)

Π, M^{bb^c} = momentum dependent form factors

pNGB potential

Elementary fermion contribution:

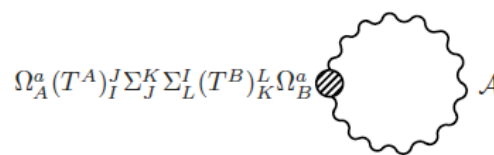
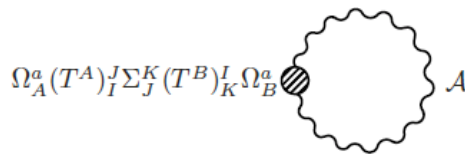


$$\int \frac{d^4 p}{(2\pi)^4} \Pi^\psi(p) = c_1^\psi \frac{g_\rho^2}{16\pi^2} f^4$$



$$V_{\text{matter}} = \frac{g_\rho^2 f^2}{24\pi^2} c_1^\chi |\lambda_\chi|^2 (12 - 9|T|^2 - 7|D|^2 - 7|S|^2) + \frac{g_\rho^2 f^2}{24\pi^2} c_1^t |\lambda_t|^2 (4|T|^2 + 3|D|^2) \\ + \frac{g_\rho^2 f^2}{24\pi^2} c_1^b |\lambda_b|^2 (2|T|^2 + 3|D|^2 + 6|S|^2) + \frac{g_\rho^2 f^2}{24\pi^2} c_1^{bc} |\lambda_{bc}|^2 (3 - 2|T|^2 - 3|D|^2).$$

Elementary gauge boson contribution:



$$\int \frac{d^4 p}{(2\pi)^4} \frac{\Pi_{1,2}^A(p)}{p^2} = c_{1,2}^A \frac{g_\rho^2}{16\pi^2} f^4$$



$$V_{\text{gauge}} = \frac{3g_\rho^2 f^2}{16\pi^2} c_1^A \left(\frac{4}{3} g_3^2 |T|^2 + \frac{3}{4} g_2^2 |D|^2 \right) + \frac{3g_\rho^2 f^2}{16\pi^2} c_2^A \left(\frac{1}{3} g_3^2 |T|^4 + \frac{1}{4} g_2^2 |D|^4 \right)$$

Obtain:

$$V(|D|) = -\frac{\alpha}{f^2}|D|^2 + \frac{\beta}{f^4}|D|^4$$

HIGGS POTENTIAL

Electroweak VEV:

$$v = f \sqrt{\frac{\alpha}{\beta}}$$

must be tuned

Higgs mass:

$$m_h^2 = \frac{2\beta v^2}{f^4} = \frac{3c_2^A g_\rho^2}{8\pi^2} M_W^2$$

W-boson mass

Requires: $c_2^A \sim \frac{64}{g_\rho^2} \sim 0.5 - 4$

where

$$\alpha = \frac{g_\rho^2}{16\pi^2} f^4 \left(\frac{14}{3} c_1^X |\lambda_X|^2 - 2c_1^t |\lambda_t|^2 - 2c_1^b |\lambda_b|^2 + 2c_1^{bc} |\lambda_{bc}|^2 - \frac{9}{4} c_1^A g_2^2 \right)$$

$$\beta = \frac{g_\rho^2}{16\pi^2} f^4 \left(\frac{3}{4} c_2^A g_2^2 \right).$$

Also have $\langle |S| \rangle = \langle |T| \rangle = 0$ with

$$m_T^2 \approx \frac{g_\rho^2}{16\pi^2} f^2 \left(-6c_1^x |\lambda_\chi|^2 + \frac{8}{3} c_1^t |\lambda_t|^2 + \frac{4}{3} c_1^b |\lambda_b|^2 - \frac{4}{3} c_1^{bc} |\lambda_{bc}|^2 + 4c_1^A g_3^2 \right)$$

$$m_S^2 \approx \frac{g_\rho^2}{16\pi^2} f^2 \left(-\frac{14}{3} c_1^x |\lambda_\chi|^2 + 4c_1^b |\lambda_b|^2 \right)$$

→ triplet mass $m_T \sim \frac{g_\rho}{4\pi} \max[|\lambda_\psi|, g_3] f$

singlet mass $m_S \sim \begin{cases} \frac{g_\rho}{4\pi} |\lambda_b| f \sim \frac{g_\rho}{4\pi} \frac{|\lambda_b|}{|\lambda_\chi|} m_\chi & |\lambda_\chi| \lesssim |\lambda_b| \\ \frac{g_\rho}{4\pi} |\lambda_\chi| f \sim \frac{g_\rho}{4\pi} m_\chi & |\lambda_\chi| \gtrsim |\lambda_b| \\ \ll \frac{g_\rho}{4\pi} |\lambda_\chi| f \lesssim m_\chi & |\lambda_\chi| \sim |\lambda_b| \end{cases}$

Possible light singlet

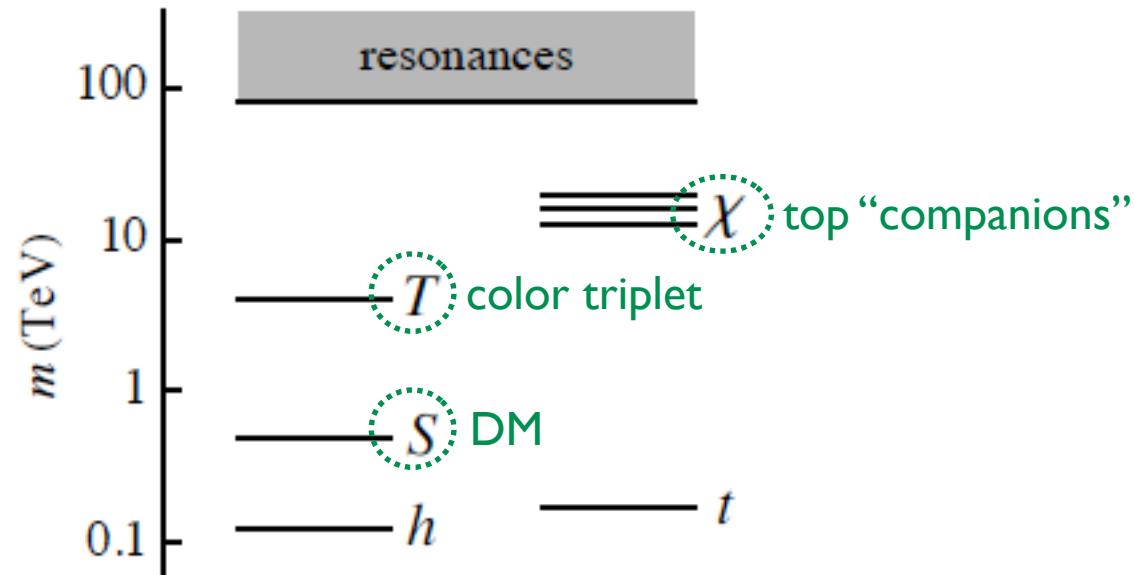
Dark matter stability

Enlarge global group: $U(7) \equiv SU(7) \times U(1)_E$

		$U(1)_q$	$U(1)_l$	$U(1)_{\#}$	$U(1)_L$	$U(1)_B$	Z_3	
NG bosons	T	0	0	-2	0	0	-1	
	D	0	0	-2	0	0	0	
	S	0	7	10	0	$\frac{1}{3}$	1	← Nonzero baryon triality leads to stability!
SM fermions	$q_{(u)}$	-1	6	11	0	$\frac{1}{3}$	0	
	$q_{(d)}$	1	6	11	0	$\frac{1}{3}$	0	
	u^c	1	-6	-9	0	$-\frac{1}{3}$	0	
	d^c	1	-6	-13	0	$-\frac{1}{3}$	0	
	$l_{(\nu)}$	0	0	2	1	0	0	
	$l_{(e)}$	0	2	2	1	0	0	
	N^c	0	0	0	-1	0	0	
	e^c	0	-2	-4	-1	0	0	
top companions	$\tilde{q}^c$	-1	6	9	0	$\frac{1}{3}$	-1	
	$\tilde{e}$	-1	6	9	0	$\frac{1}{3}$	1	
	$\tilde{d}^c$	-1	-1	-3	0	0	1	
	$\tilde{l}$	-1	-1	-3	0	0	0	

The “Unnatural” Composite Higgs model

[James Barnard, TG, Tirtha Sankar Ray, Andrew Spray: 1409.7391]



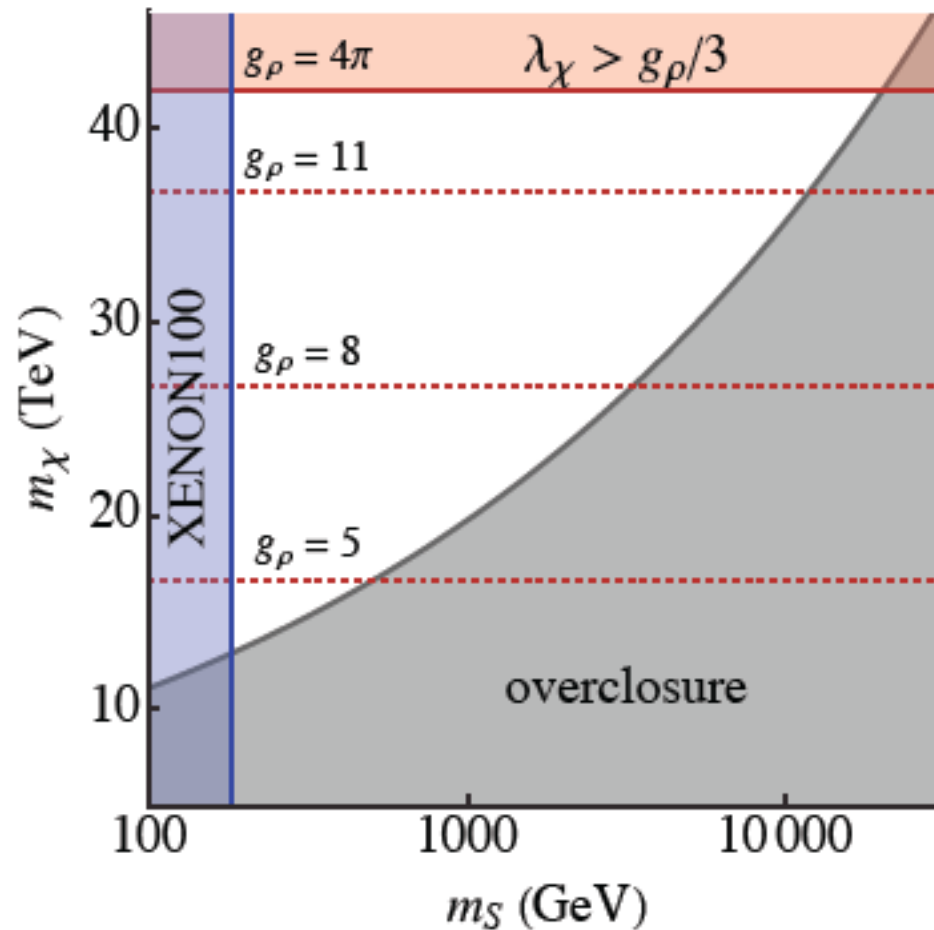
Low-energy spectrum: Standard Model + $S + T + \chi$

What are experimental signals?

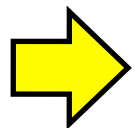
Dark matter constraints

singlet Higgs partner S -- Higgs portal coupling $V \supset \kappa |D|^2 |S|^2$

where $\kappa \sim 0.02 \left(\frac{m_\chi}{f} \right)^4$



$f = 10$ TeV



$180 \text{ GeV} \lesssim m_S \lesssim 10 \text{ TeV}$

$10 \text{ TeV} \lesssim m_\chi \lesssim 40 \text{ TeV}$

Higgs couplings

LHC: 1-5 % precision

ILC: 0.5 - 1% precision

$$f \gtrsim 10 \text{ TeV} \quad \Rightarrow \quad \frac{v^2}{f^2} \lesssim 10^{-4}$$

$$\frac{g_{hWW}}{g_{hWW}^{SM}} \sim \frac{g_{hff}}{g_{hff}^{SM}} \sim \sqrt{1 - \frac{v^2}{f^2}}$$

*Tiny deviations –too small
to be seen at LHC/ILC*

Higgs boson is very SM-like!

Exotic state phenomenology

- *top companions* χ

$$\tilde{q}^c \in (\bar{3}, 2)_{-\frac{1}{6}} \quad \tilde{e} \in (1, 1)_{-1} \quad \tilde{d}^c \in (\bar{3}, 1)_{\frac{1}{3}} \quad \tilde{l} \in (1, 2)_{-\frac{1}{2}}$$

$$f = 10 \text{ TeV} \quad \Rightarrow \quad m_\chi \sim (1-2)f \sim 10-20 \text{ TeV}$$

Decays are collider-prompt

$$e.g. \quad \tilde{q}^c \rightarrow Tq, \quad \tilde{d}^c \rightarrow t^c TS$$

$$e.g. \quad \tilde{e} \rightarrow bTT, \quad \tilde{l} \rightarrow qTS$$

Can be searched for at a future 100 TeV collider!

- *triplet Higgs partner* $T \in (3, 1)_{-\frac{1}{3}}$ (like RH sbottom in SUSY)

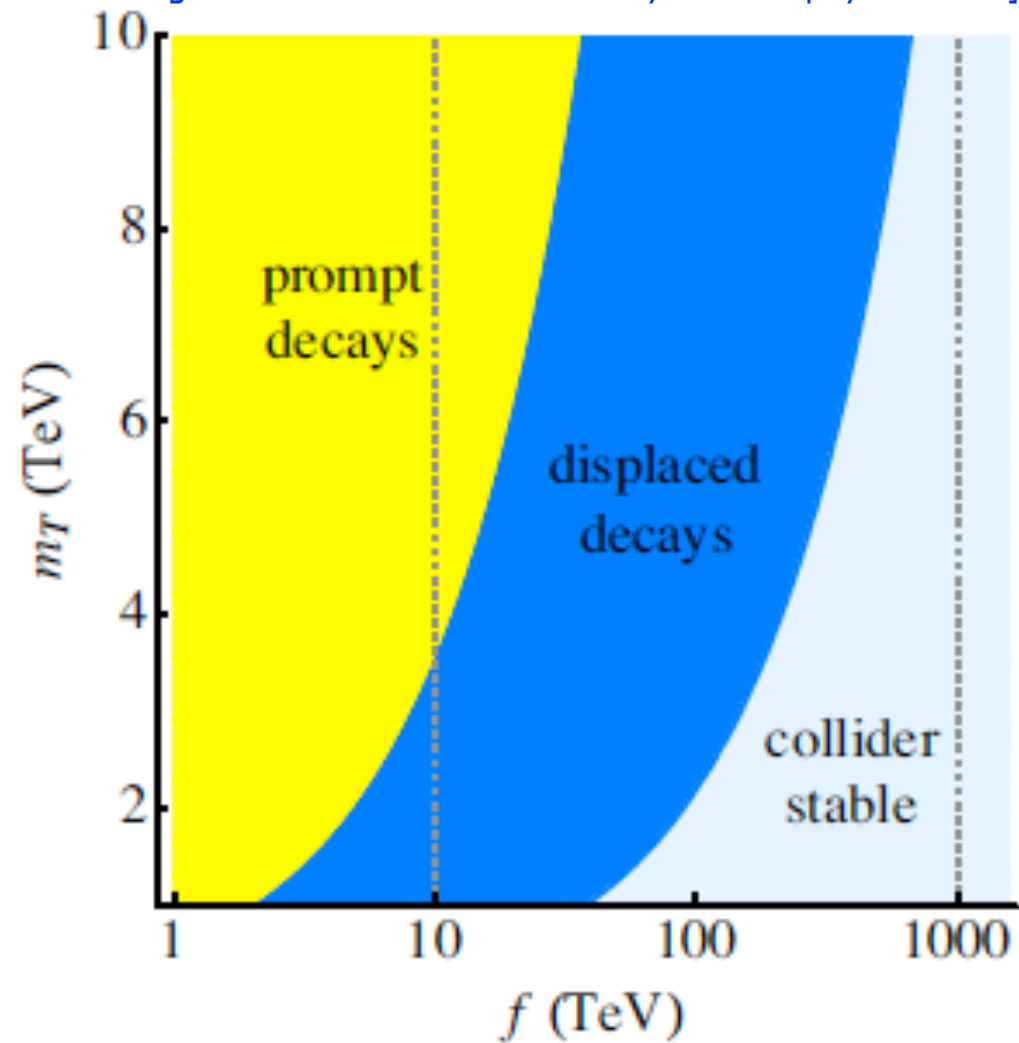
$$f = 10 \text{ TeV} \Rightarrow m_T \sim (1-2) \frac{f}{\pi} \sim 3-5 \text{ TeV}$$

$$\mathcal{L} \supset \frac{c_3^T}{24\pi^2 f^2} |\lambda_{bc}| |\lambda_\nu| |\lambda_\tau| S^2 (T^\dagger t^c b^c) \quad \text{dimension-6 term}$$

$$T \rightarrow tbSS \Rightarrow c\tau \approx \underbrace{0.2 \text{ mm}}_{\text{can produce a displaced vertex!}} \left(\frac{1}{c_3^T} \right)^2 \left(\frac{8}{g_\rho} \right)^3 \left(\frac{3 \text{ TeV}}{m_T} \right)^5 \left(\frac{\overset{f > 10 \text{ TeV} = \text{long-lived decay}}{f}}{10 \text{ TeV}} \right)^4$$

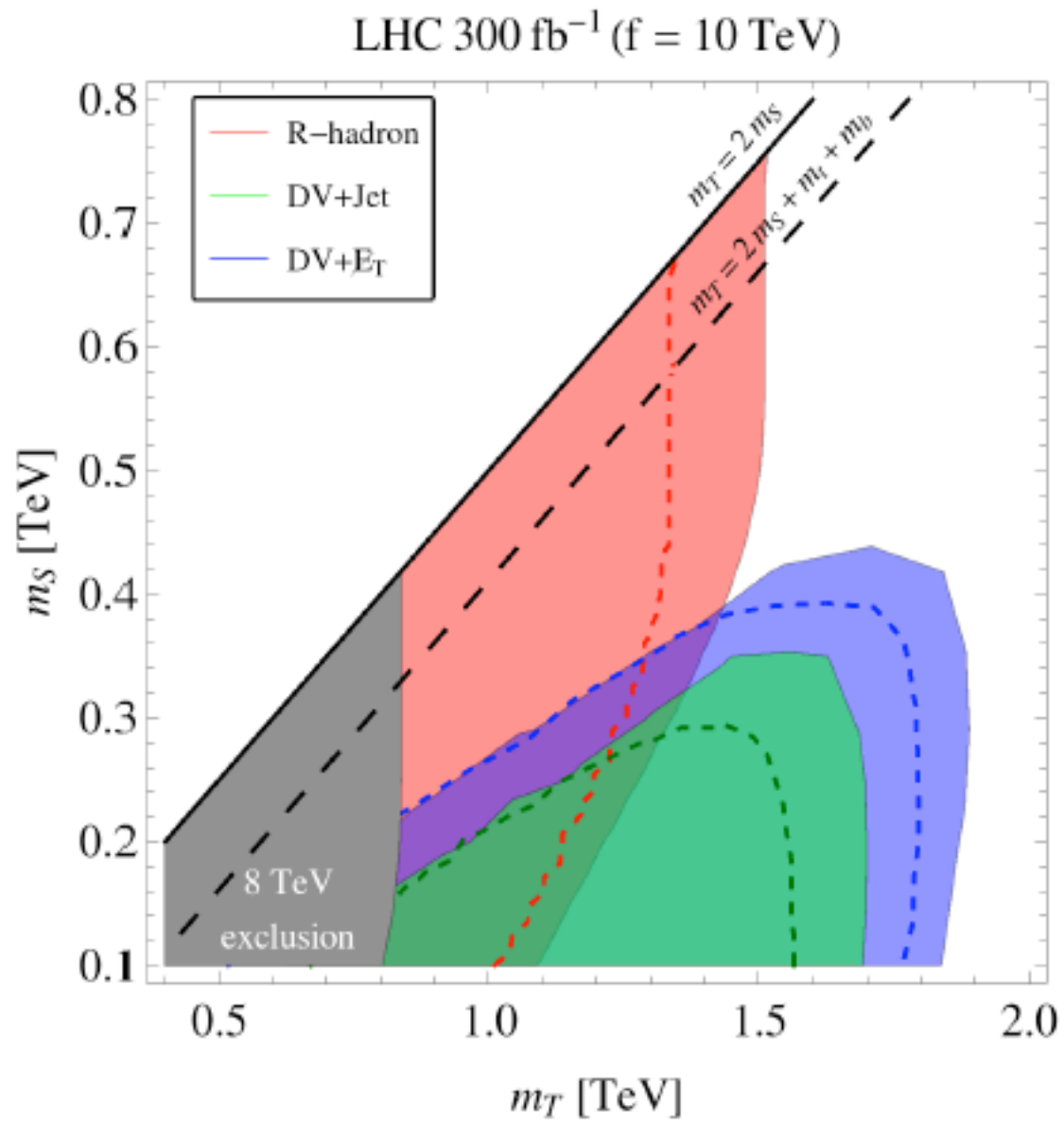
Color triplet decay

[James Barnard, TG, Tirtha Sankar Ray, Andrew Spray: 1409.7391]



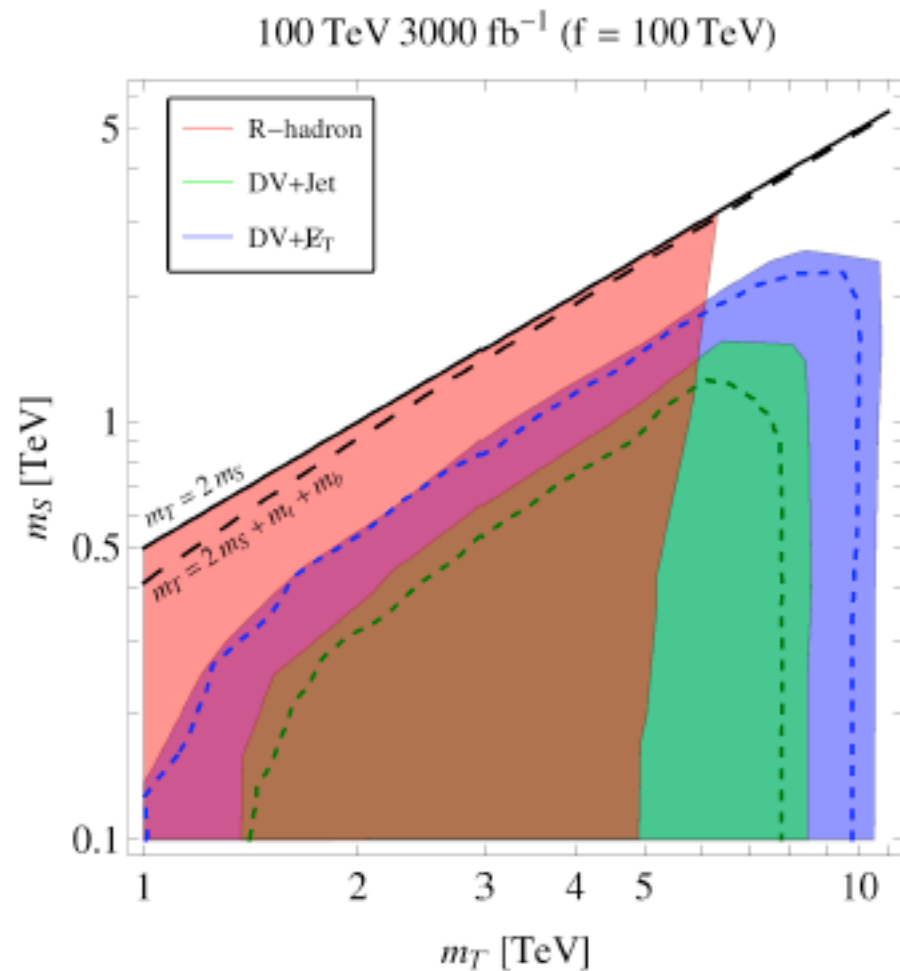
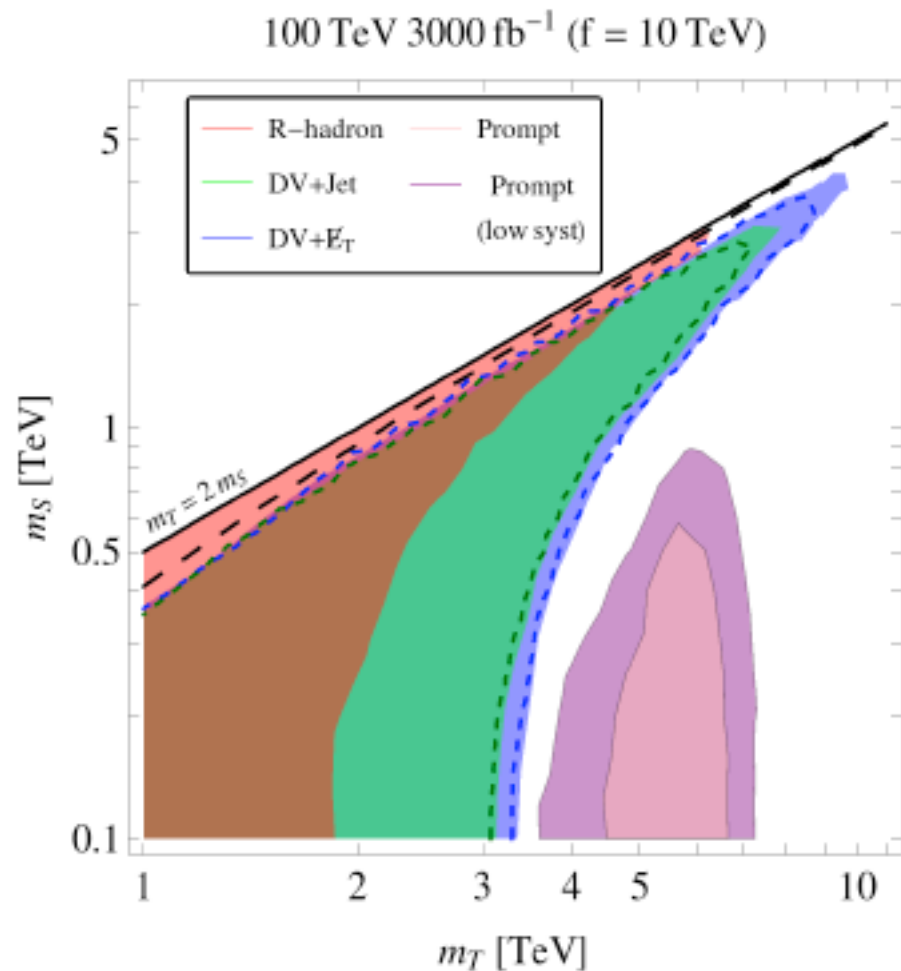
LHC:

[Barnard, Cox, TG, Spray: 1510.06405]



Future 100 TeV collider:

[Barnard, Cox, TG, Spray: 1510.06405]



Summary

- $f \gtrsim 10$ TeV simply eliminates all precision electroweak and flavor constraints
 - *Higgs potential is tuned at 10^{-4} level*
 - *“Unnatural” or “split” composite Higgs*
- SU(7)/SU(6)×U(1) minimal model
 - *Improves gauge coupling unification*
 - *Explains fermion mass hierarchy*
- Higgs partners: S = dark matter, T = color triplet
- Long-lived T decays = sign of unnaturalness!